

# PARTICLE PHYSICS AND COSMOLOGY

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The 2014 European School  
of High Energy Physics

Garderen, the Netherlands

19-21 June 2014

## The 2014 European School of High-Energy Physics

Garderen, the Netherlands 18 June – 1 July 2014

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Field Theory and the Electro-Weak Standard Model  
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Practical Statistics for Particle Physicists  
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Physics Beyond the Standard Model  
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Deadline for Applications: 14 February 2014  
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# OUTLINE

## LECTURE 1

Essential Cosmology: Contents and History of the Universe

## LECTURE 2

WIMP Dark Matter: Candidates and Methods of Detection

## LECTURE 3

Inflation, Gravitinos, and Hidden Sectors

# INTRODUCTION

- Why should HEP physicists care about cosmology?
  - We want to answer age-old questions about our Universe and our place in it
  - We are in a golden age of cosmology, and cosmology and particle physics have become inextricably intertwined
  - Many of the leading motivations for new particle physics come from cosmology: dark matter, dark energy, inflation, baryon asymmetry
  - Cosmology sets new interesting mass scales and can provide upper bounds on masses
  - Cosmology reaches the hard corners of parameter space (high masses, weak interactions)
  - HEP physicists and cosmologists have a lot to learn from each other
  - These topics capture the imagination of the public

# ESSENTIAL COSMOLOGY

- For the first time in history, we now have a complete *picture* of the Universe
- How did this come about?
- We will first review the standard model of cosmology and some of the key observational evidence leading to it
- Little previous knowledge of cosmology is assumed; focus on heuristic derivations, order-of-magnitude estimates, intuitive arguments, and some aspects that (at present) seem to be most linked to particle physics, and particularly high-energy physics. This is a huge topic, many important topics will be neglected.

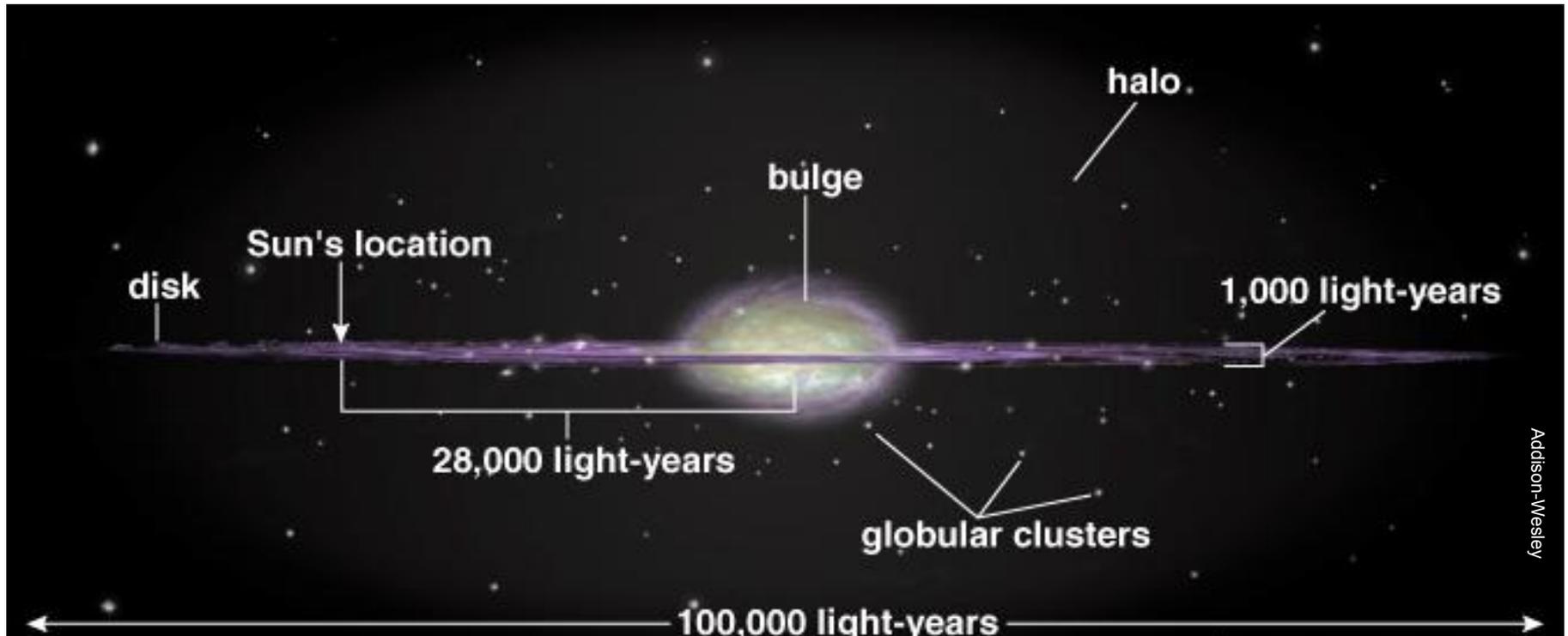
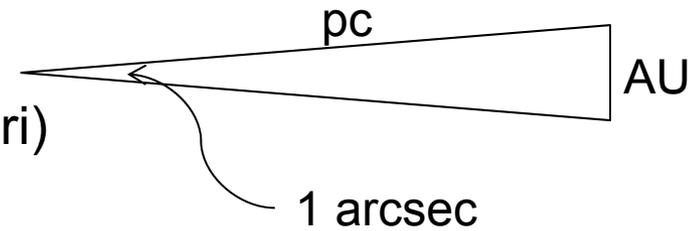
# PARTICLE PHYSICS SCALES

- Natural units:  $h = c = k_B = 1$ 
  - $h = c = 1$  is standard
  - $k_B = 1 \rightarrow 1 \text{ K} = 0.08 \text{ meV}$
- Some useful energy scales
  - $10^{19} \text{ GeV}$ : Planck scale
  - $10^{16} \text{ GeV}$ : GUT scale
  - TeV: weak scale
  - GeV: binding energy of quarks ( $\Lambda_{\text{QCD}}$ )
  - MeV: binding energy of nuclei
  - eV: binding energy of atoms
  - 0.1 meV: CMB temperature now

# ASTROPHYSICS SCALES

- 1 pc = 3.3 ly. Some useful length scales

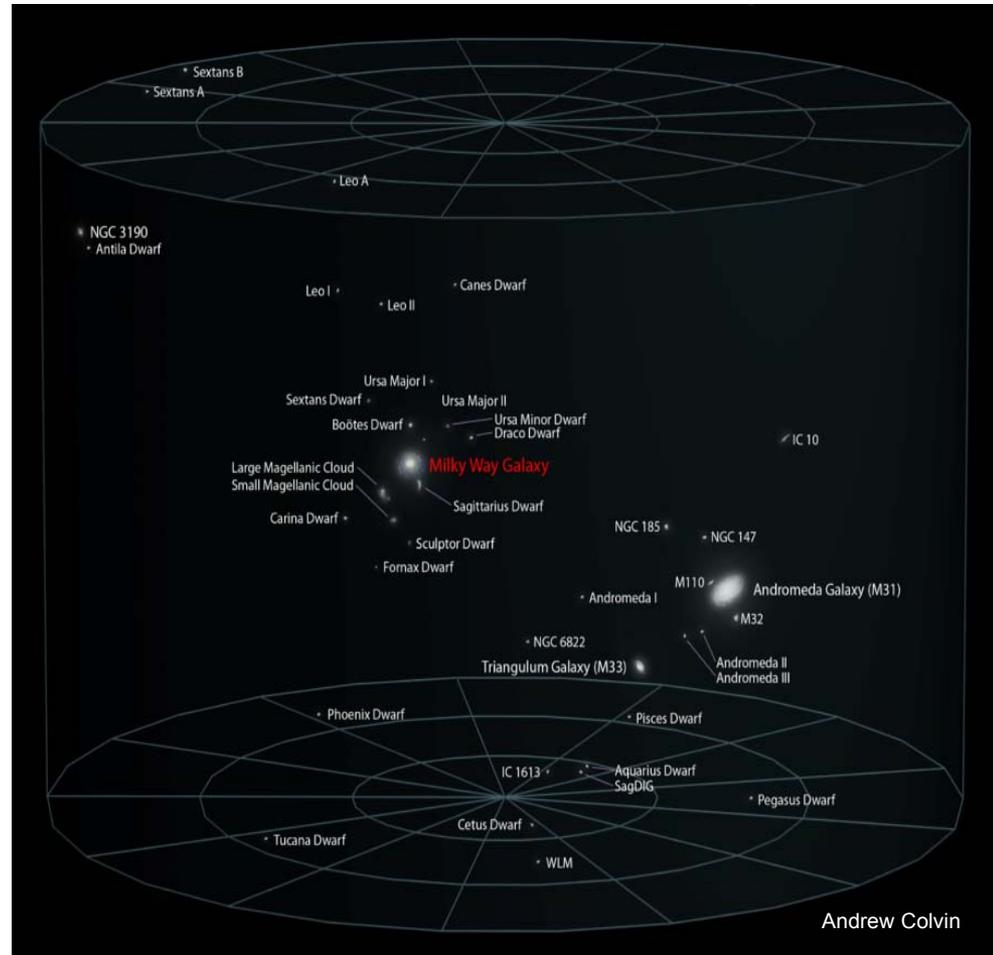
- $10^{-5}$  pc: distance to Sun (AU)
- pc: distance to the next star (Alpha Centauri)
- 10 kpc: distance to Milky Way center



Addison-Wesley

# ASTROPHYSICS SCALES

- Some useful length scales
  - $10^{-5}$  pc: distance to Sun
  - pc: distance to next-nearest star (Alpha Centauri)
  - 10 kpc: distance to Milky Way center
  - 10-100 kpc: distance to nearest dwarf galaxies
  - Mpc: distance to nearest big galaxy (Andromeda)
  - 10 Mpc: size of clusters of galaxies
  - 10 Gpc: size of the observable Universe



# COSMOLOGY BASICS

- The evolution of the Universe is dominated by gravity. We must therefore begin with some basic general relativity.
- Let the spacetime metric  $g_{\mu\nu}$  be a dynamical field. This specifies lengths through

$$ds^2 = g_{\mu\nu}(x) dx^\mu dx^\nu$$

- With a dynamical metric, our theory is specified by the Einstein-Hilbert action

$$S = \int d^4x \sqrt{-g} \left( \frac{R}{16\pi G} + \mathcal{L}_{SM} \right)$$

where  $g = \det(g_{\mu\nu})$ ,  $G = M_{\text{Pl}}^{-2}$ , and  $R = R(g_{\mu\nu}, \partial g_{\mu\nu}, \partial^2 g_{\mu\nu})$  is the scalar curvature.

- Extremizing this action, we find the equations of motion

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = 8\pi G T_{\mu\nu} \quad T_{\mu\nu} \equiv -2 \frac{\delta \mathcal{L}_{SM}}{\delta g^{\mu\nu}} + g_{\mu\nu} \mathcal{L}_{SM}$$

These are the Einstein equations, where  $R_{\mu\nu}$  is the Ricci curvature tensor, again a function of the metric, and  $T_{\mu\nu}$  is the stress-energy tensor and contains all the particle physics.

# COSMOLOGY BASICS

- The Einstein equations are complicated to solve, so we make some approximations, based on observations.
- The Universe appears to be homogeneous and isotropic on scales larger than  $\sim 10$  Mpc.
- So we assume a Friedmann-Lemaitre-Robertson-Walker metric

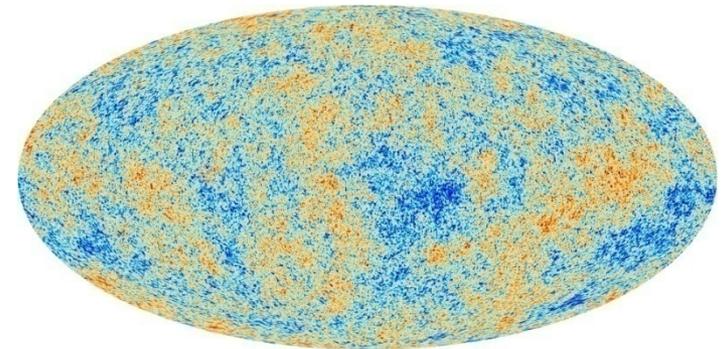
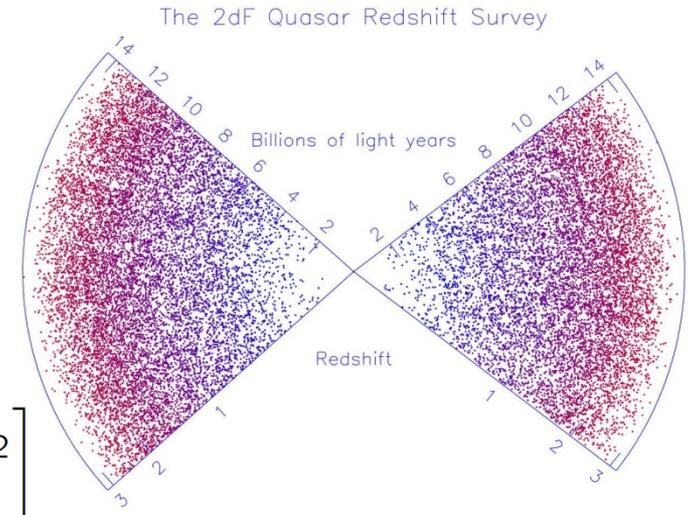
$$ds^2 = dt^2 - a^2(t) \left[ \frac{dr^2}{1 - kr^2} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \right]$$

and stress-energy tensor

$$T^\mu{}_\nu = \text{diag} [\rho(t), -p(t), -p(t), -p(t)]$$

Here  $a(t)$  is the scale factor and  $k$  is a constant that specifies the curvature ( $k = 0$  implies a flat Universe);

$\rho$  is energy density and  $p$  is pressure.



# COSMOLOGY BASICS

- With these simplifications, the Einstein equations become quite manageable.

- The Einstein equations imply the Friedmann equation  $\left(\frac{\dot{a}}{a}\right)^2 + \frac{k}{a^2} = \frac{8\pi G}{3}\rho$ .

We define the Hubble parameter  $H \equiv \frac{\dot{a}}{a}$  and the critical density  $\rho_c \equiv \frac{3H^2}{8\pi G}$ .

- We may parameterize various materials by  $w$ , where  $p = w\rho$ . If  $w$  is constant, stress-energy conservation  $T^{\mu\nu}{}_{;\nu} = 0 \rightarrow \rho \sim a^{-3(1+w)}$

- For example, we can consider 3 kinds of contributions to the energy density:

Matter:  $\rho$  is diluted by expansion ( $w = 0$ )    MD :  $\rho \propto a^{-3} \Rightarrow \dot{a}^2 \propto \frac{1}{a} \Rightarrow a \propto t^{2/3}$

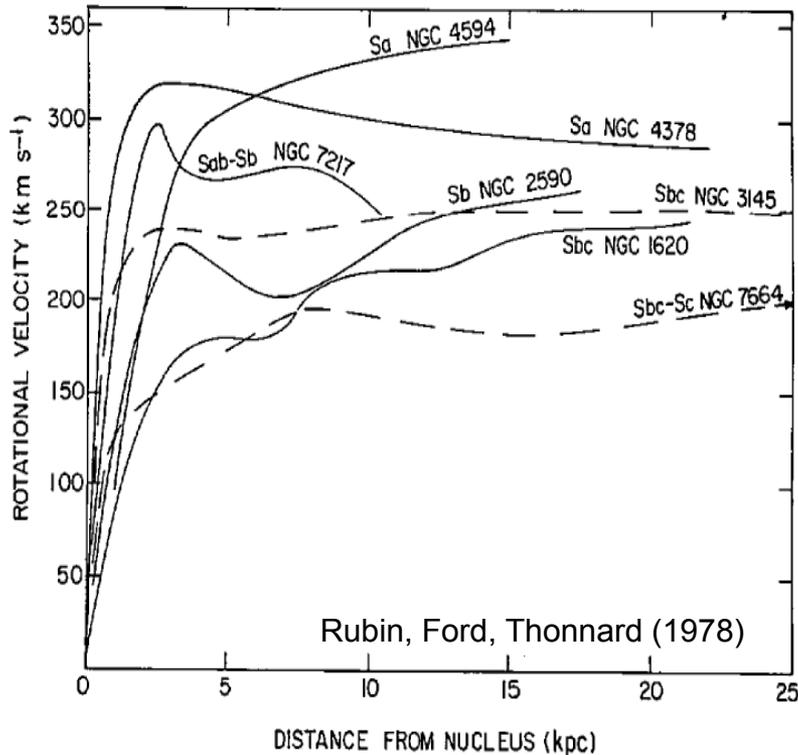
Radiation:  $\rho$  is diluted by expansion  
and redshifting ( $w = 1/3$ )    RD :  $\rho \propto a^{-4} \Rightarrow \dot{a}^2 \propto \frac{1}{a^2} \Rightarrow a \propto t^{1/2}$

Vacuum energy:  $\rho$  is not diluted ( $w = -1$ )    VD :  $\rho \propto a^0 \Rightarrow \dot{a}^2 \propto a^2 \Rightarrow a \propto e^{ct}$

- What do observations tell us about the contents of the Universe now?

# ROTATION CURVES OF GALAXIES

Rubin, Ford (1970); Bosma (1978)



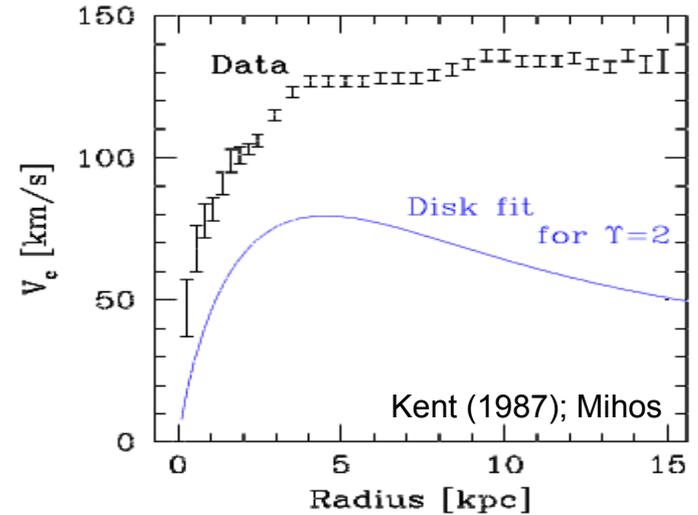
- Rotational velocity  $v_c$  as function of distance from center  $r$ 
  - $v_c \sim O(300) \text{ km/s} \sim O(10^{-3}) c$
  - $r \sim \text{few kpc}$
- Expect  $v_c \sim r^{-1/2}$  beyond luminous region

$$\frac{mv_c^2}{r} = G_N \frac{mM}{r^2}$$

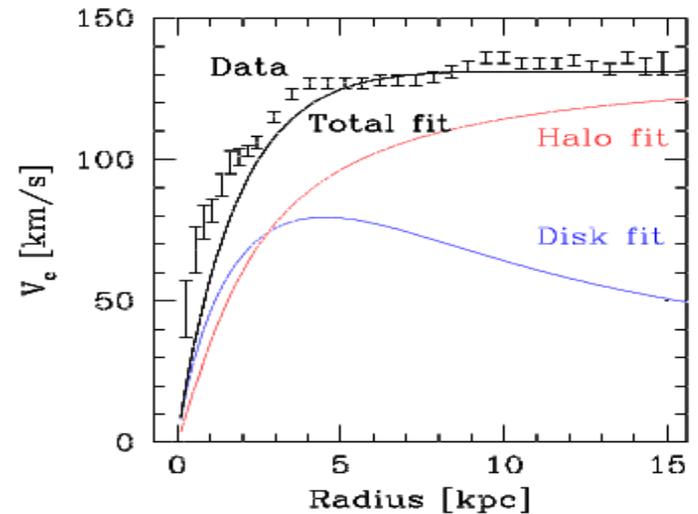
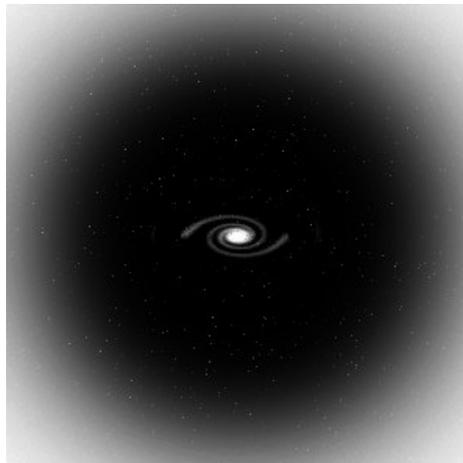
Instead find  $v_c \sim \text{constant}$

- The discrepancy may be resolved by missing mass and is classic (but not the first) evidence for dark matter

# AN EXAMPLE: NGC 2403

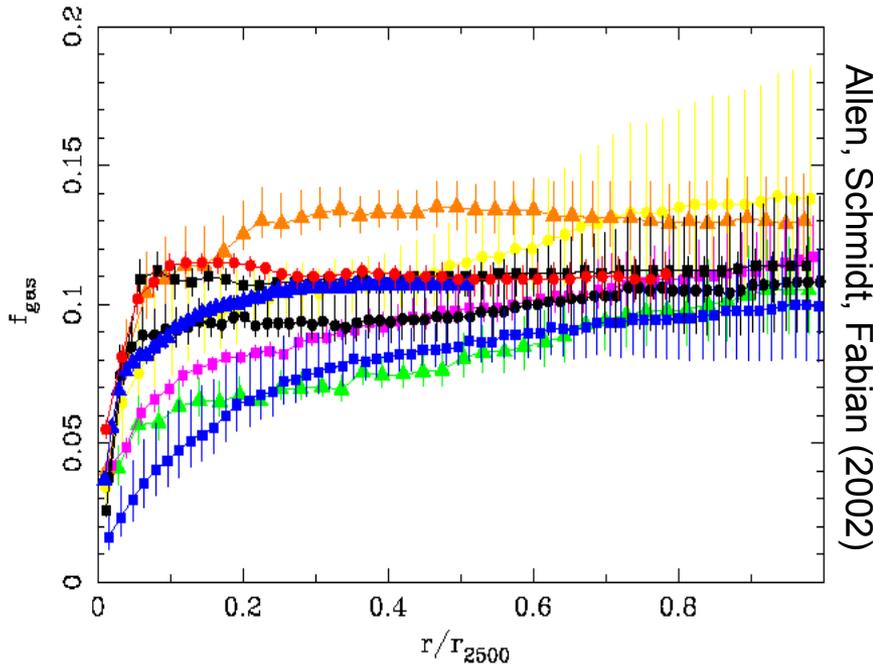


- $v_c$  from HI line
- Fit mass-to-light ratio, halo model; this tells us about  $\rho(r)$



# MISSING MASS IN CLUSTERS OF GALAXIES

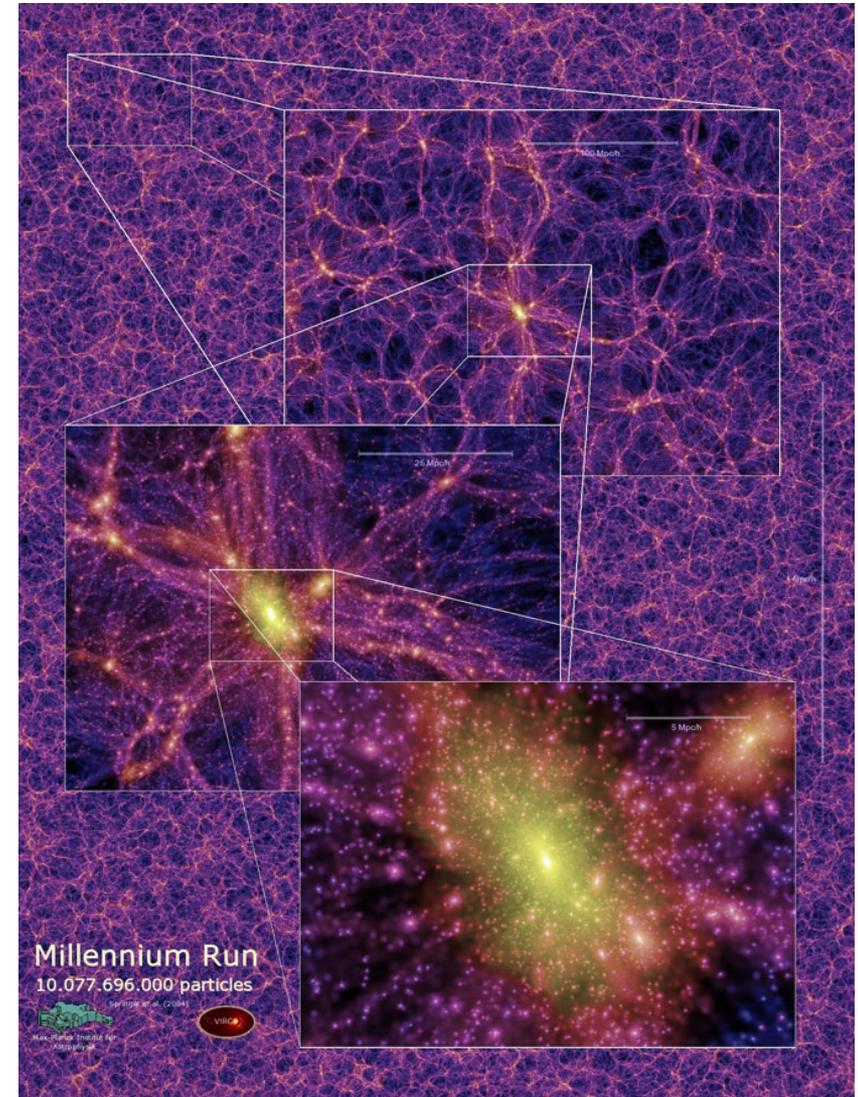
Zwicky (1933)



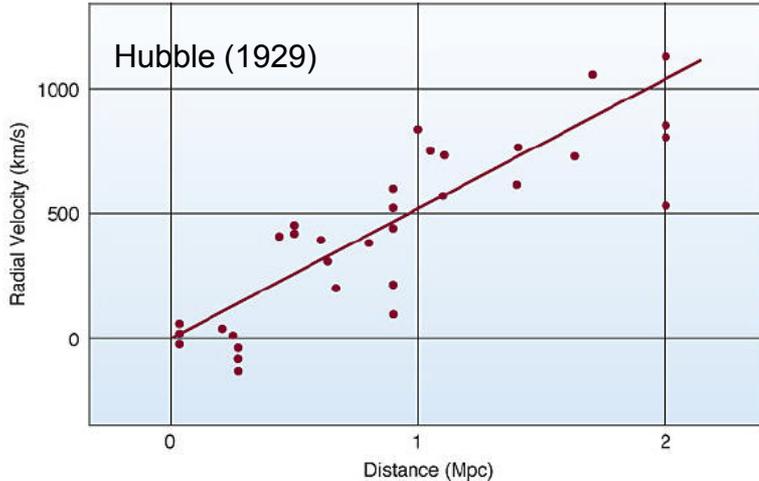
- ~10-1000 galaxies, the largest gravitationally-bound structures
- Intracluster gas mass, total mass constrained by X-rays from bremsstrahlung, lensing, etc.
- Gas mass fraction  $f_{\text{gas}}$  as function of distance from center
  - $f_{\text{gas}} = \rho_B / \rho_M$
  - $r_{2500} \sim \text{Mpc}$
- Extrapolating from clusters to the whole Universe, this constrains  $\Omega_M = \Omega_B \rho_M / \rho_B$ , where  $\Omega = \rho / \rho_c$  is energy density in units of the critical density and  $\Omega_B$  is determined independently

# DARK MATTER DISTRIBUTION

- Evidence of dark matter from many other observations: weak lensing, strong lensing, Bullet Cluster, ...
- Simulations and observations lead to a consistent picture on large scales
- DM is cold, it clumps and leads to structure formation; every galaxy is surrounded by a dark matter halo
- Local DM properties  
 $\rho \sim 0.2 - 0.5 \text{ GeV/cm}^3$ ,  
overdense by factor of  $\sim 10^5$   
 $v \sim 10^{-3} c$  for many DM candidates,  
independent of mass (virial theorem)



# EXPANSION OF THE UNIVERSE



- Galaxies that are far from us are receding from us, and the recessional velocity is roughly proportional to the distance
- This is Hubble's Law, and the constant of proportionality is Hubble's constant

$$v = H d$$

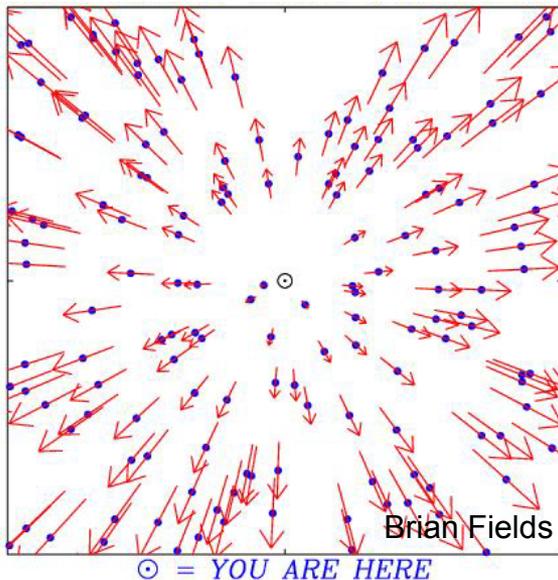
- The current value of the Hubble parameter is

$$H_0 = h \text{ 100 km/s/Mpc}$$

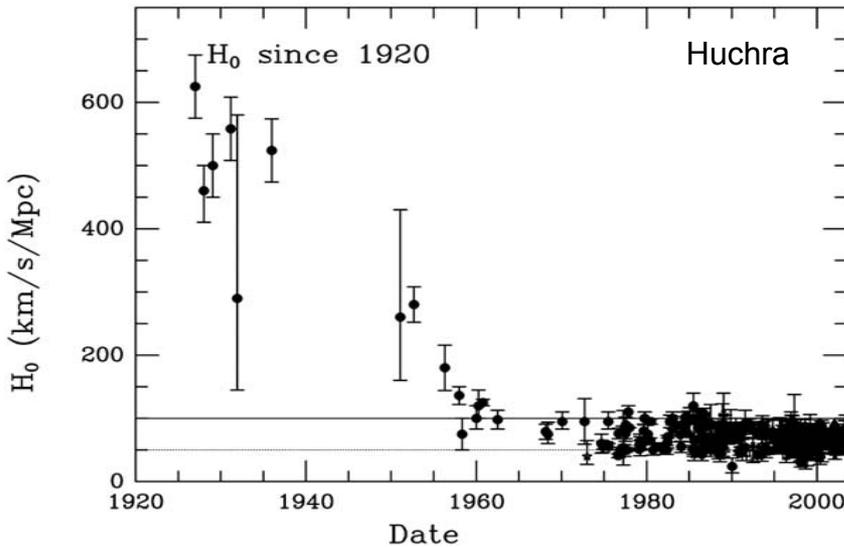
$$h = 0.705 \pm 0.015 \quad (h^2 \approx 1/2)$$

- This means that light from distant galaxies is redshifted

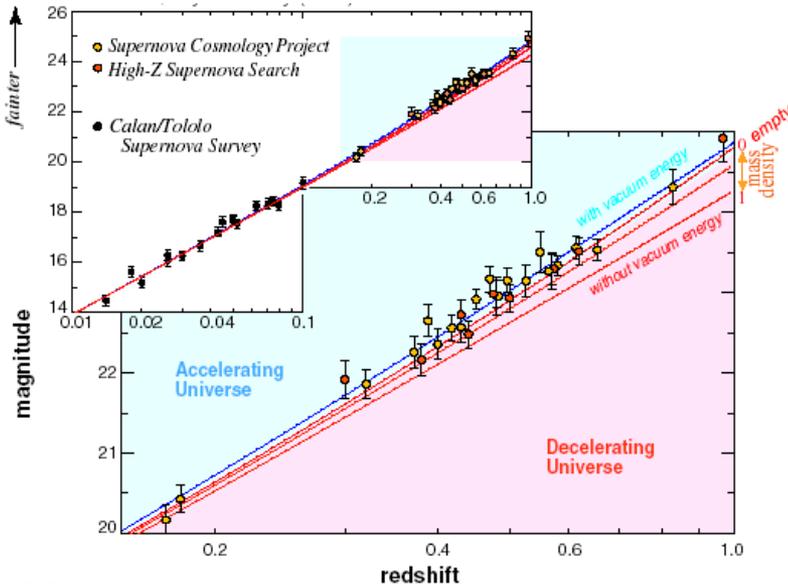
$$\lambda_{\text{obs}} / \lambda_{\text{emit}} = 1 + z$$



# EXPANSION OF THE UNIVERSE



- The original evidence for the expanding universe has now been extended to far larger distances with Type Ia supernovae
- Note the evolution of the measurement of  $H_0$  -- a lesson in underestimated systematics
- The universe's expansion is currently accelerating!
- Measurement of this expansion history constrains the acceleration of expansion:

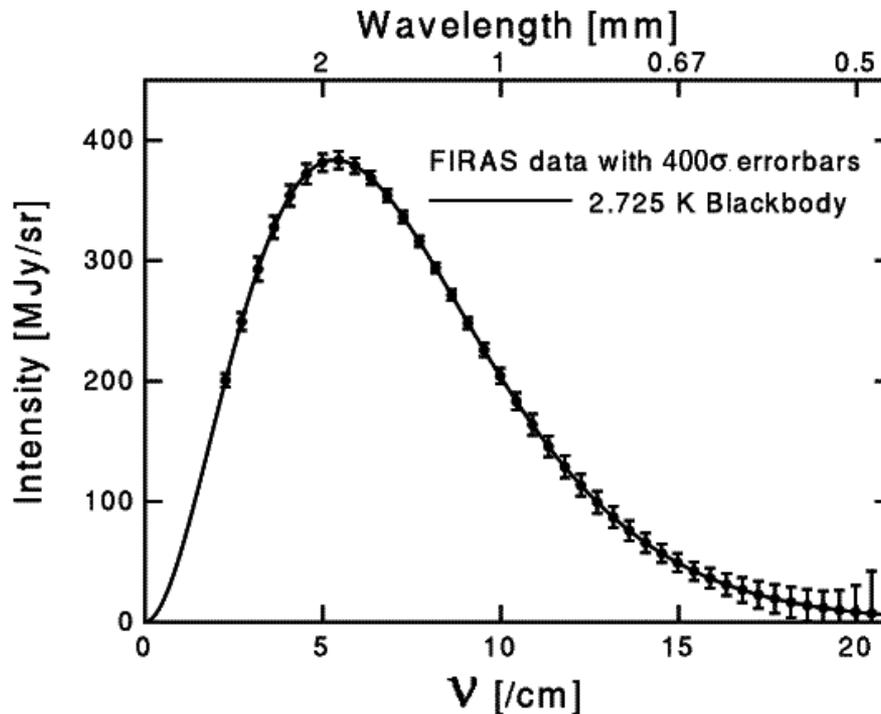


$$\Omega_{\Lambda} - \Omega_{\text{M}}$$

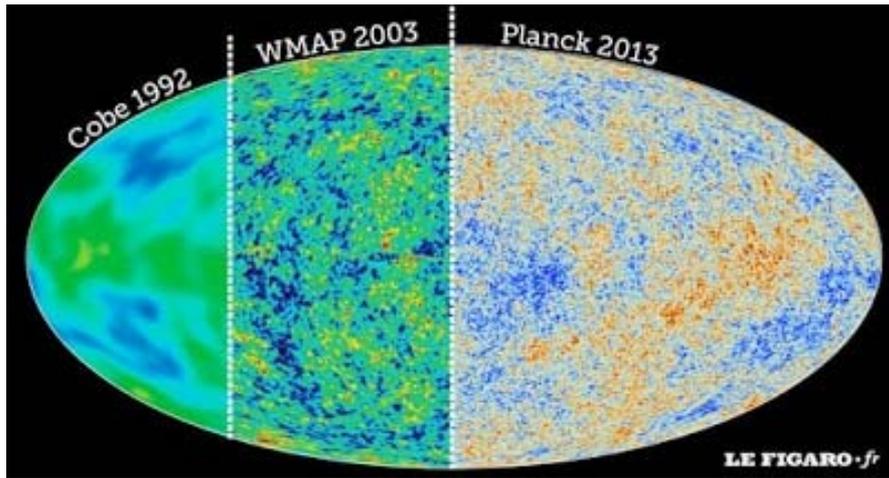
“Attractive matter vs. repulsive dark energy”

# COSMIC MICROWAVE BACKGROUND

- The Universe is filled with an essentially perfect black body spectrum
- The temperature is 2.725 K in all directions, implying the Universe is highly isotropic on large scales



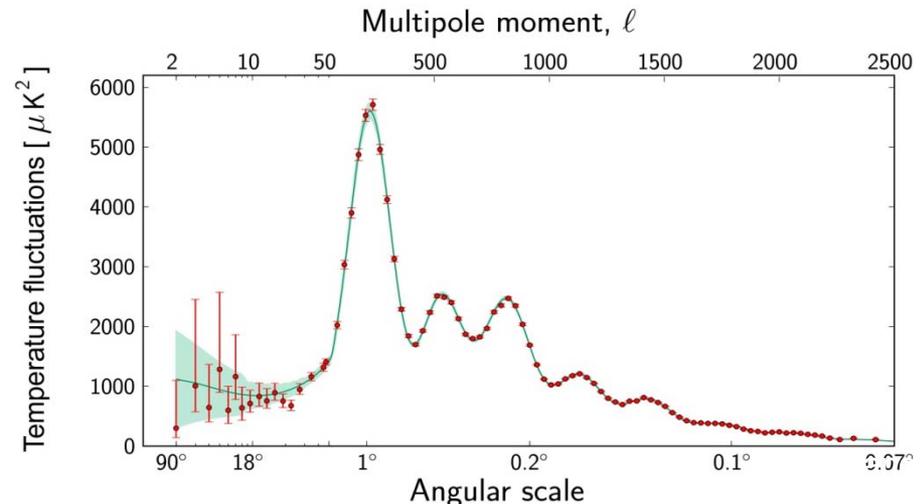
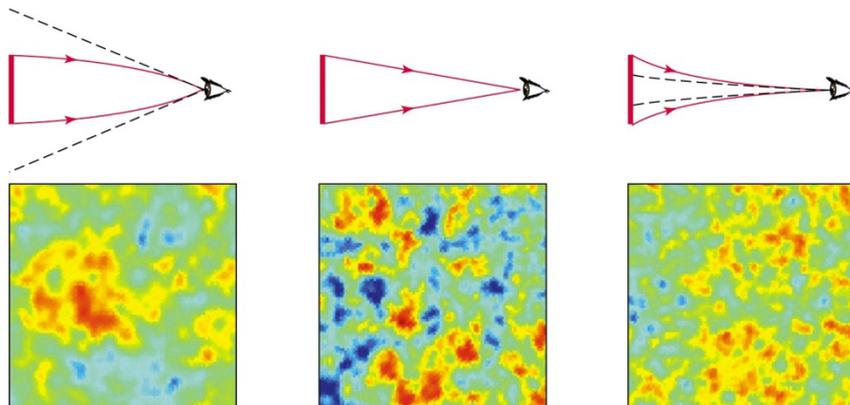
# COSMIC MICROWAVE BACKGROUND



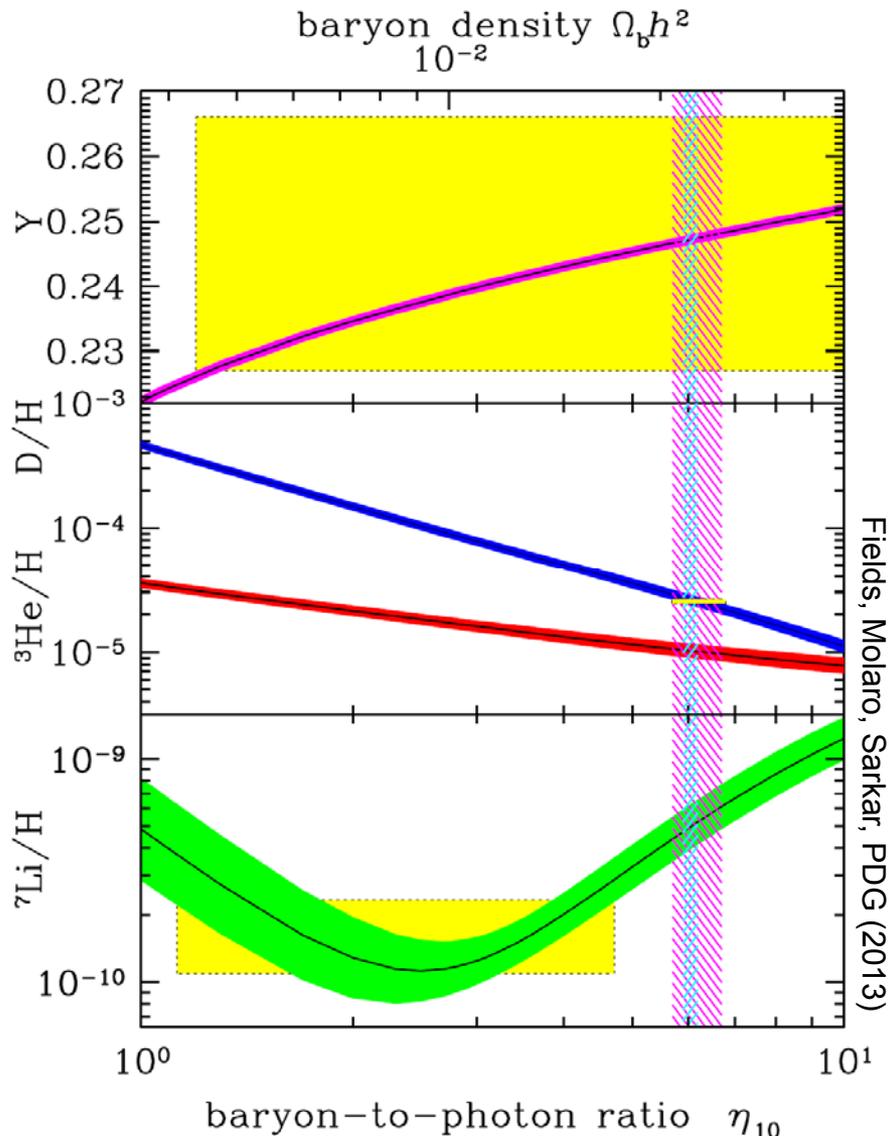
- There is, however, a tiny anisotropy of  $\delta T/T \sim 10^{-5}$
- Dramatic improvements from COBE to WMAP to Planck
- Angular size of the hot and cold spots constrains the geometry:

$$\Omega_{\Lambda} + \Omega_M$$

“total energy density”

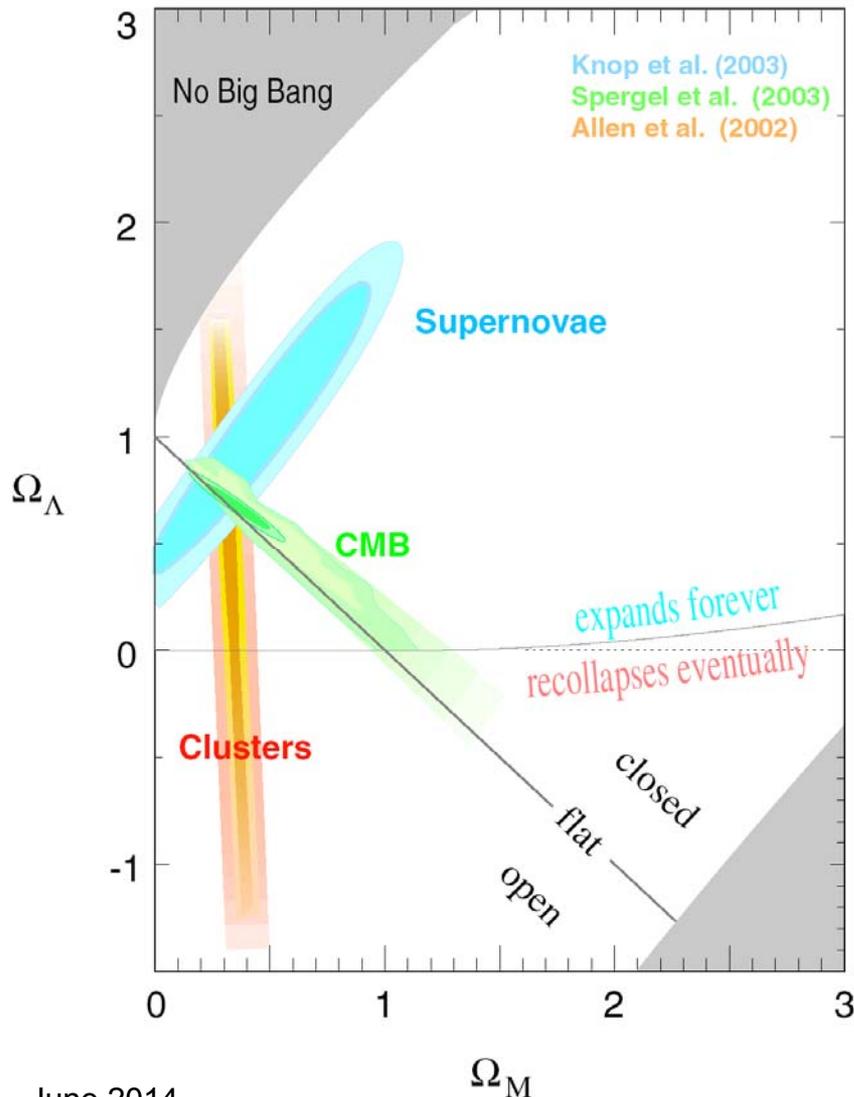


# BIG BANG NUCLEOSYNTHESIS



- At  $T \sim 1$  MeV, around the binding energy of nuclei, the universe cooled enough for light elements to start forming
- The abundance of each light species is a function of a single parameter,  $\eta$ , the baryon-to-photon ratio
- BBN and CMB determinations are consistent (except possibly for Li) for a single choice of  $\eta$  and constrain the density in baryons:  $\Omega_B$

# SYNTHESIS



- Remarkable agreement

Dark Matter:  $23\% \pm 4\%$

Dark Energy:  $73\% \pm 4\%$

Baryons:  $4\% \pm 0.4\%$

[vs:  $0.2\%$  for  $\Sigma m = 0.1$  eV]

- Remarkable precision

- Remarkable results

# STANDARD COSMOLOGICAL HISTORY

- For many applications, temperature is a better clock than time. We would like to find the time-temperature correspondence.
- For radiation,  $\rho \propto a^{-4}$
- But by dimensional analysis,  $\rho \propto T^4 \Rightarrow T \propto \frac{1}{a}$
- The relations in the matter- and radiation-dominated eras are therefore

$$\text{MD} : T \propto t^{-2/3}$$

$$\text{RD} : T \propto t^{-1/2}$$

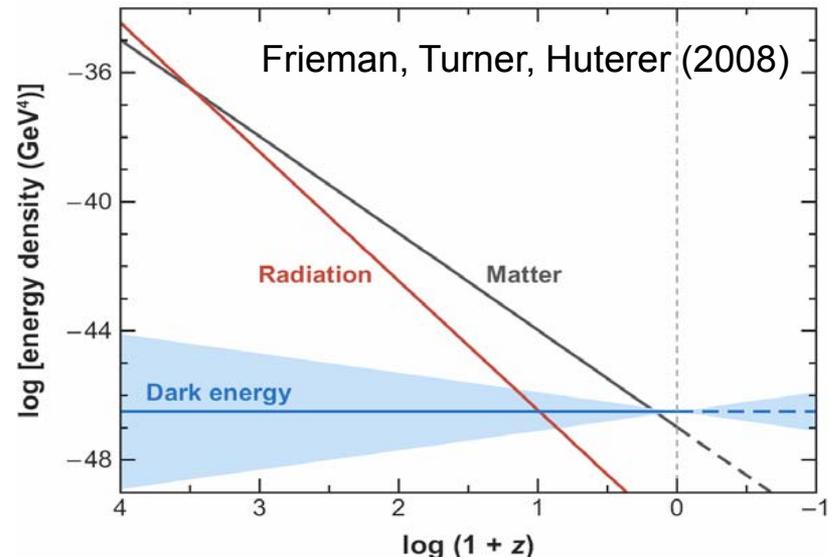
# WHAT DOMINATES WHEN?

- We know  $\Omega_\Lambda \approx 0.73$ ,  $\Omega_M \approx 0.27$ . We can also determine

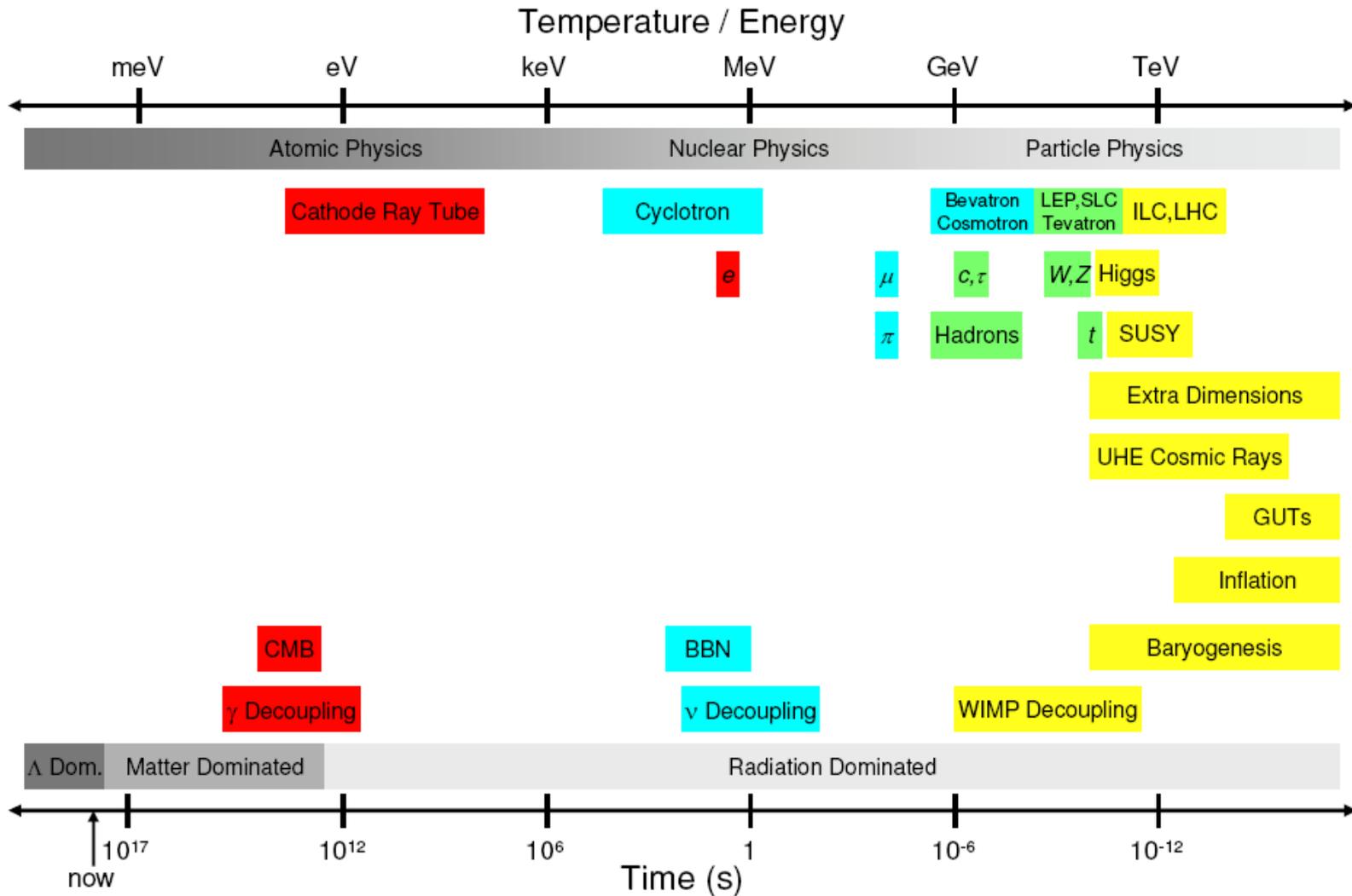
$$\Omega_{\text{CMB}} \equiv \frac{\rho_{\text{CMB}}}{\rho_c} \sim \frac{T_{\text{CMB}}^4}{\frac{3H^2}{8\pi G}} \sim \frac{(2.7 \text{ K})^4 (14 \text{ Gyr})^2}{(10^{19} \text{ GeV})^2}$$

$$\sim \frac{(10^{-4} \text{ eV})^4 (14\pi \times 10^{16} \text{ s})^2}{(10^{-16} \text{ eV s})^2 (10^{28} \text{ eV})^2} \sim 10^{-4}$$

- Matter-radiation equality
  - $T \sim 10^4 T_0 \sim \text{eV}$
  - $t \sim 10^{-6} t_0 \sim 10^{12} \text{ s}$
- Vacuum-matter equality
  - very recent past



# THERMAL HISTORY OF THE UNIVERSE



# DECOUPLING

- Decoupling of particle species is an essential concept for particle cosmology. It is described by the Boltzmann equation

$$\frac{dn}{dt} = -3Hn - \langle \sigma v \rangle [n^2 - n_{\text{eq}}^2]$$

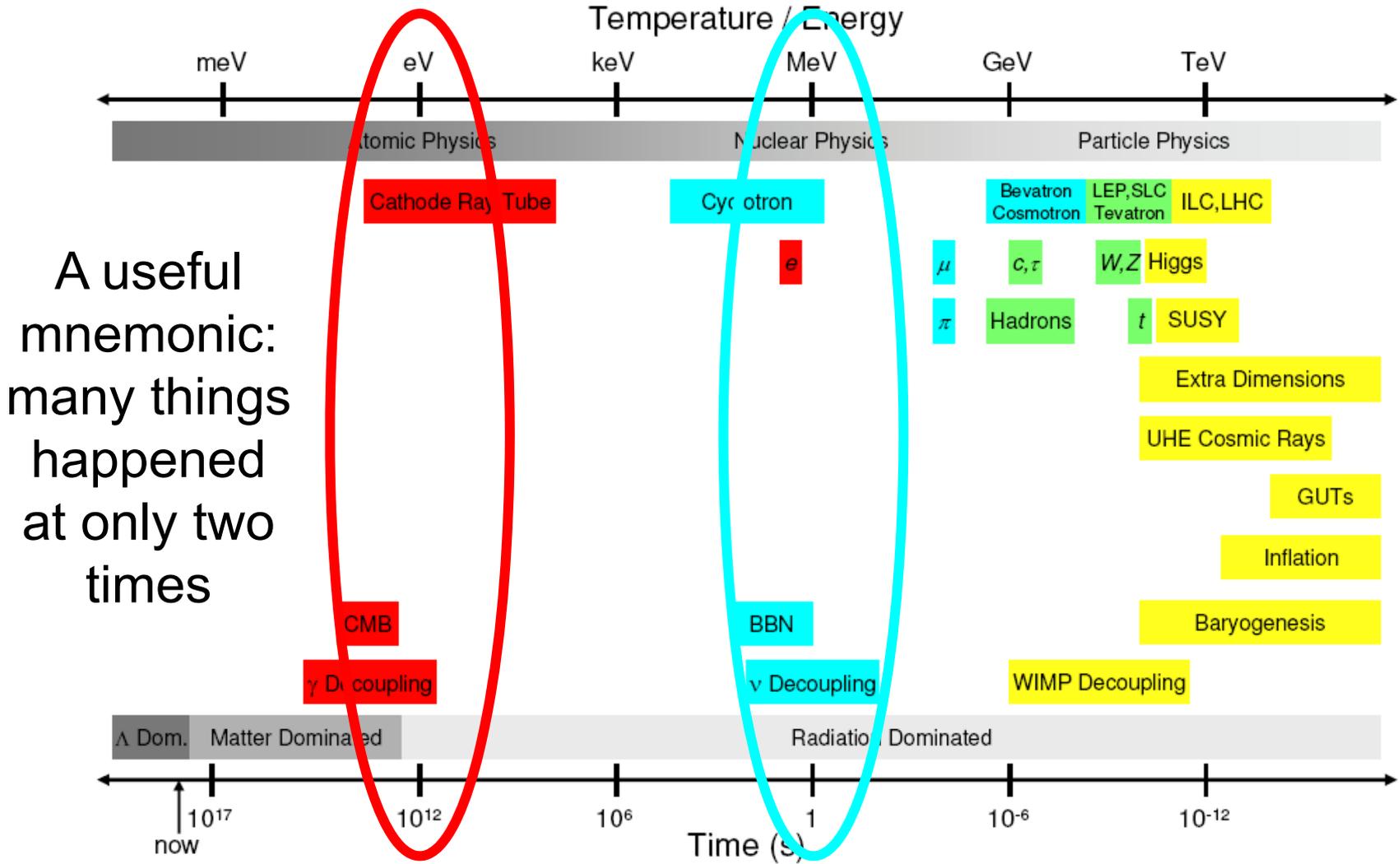
$\uparrow$  Dilution from expansion       $\uparrow$   $XX \rightarrow f\bar{f}$        $\swarrow$   $f\bar{f} \rightarrow XX$

- Particles decouple (or freeze out) when  $n_{\text{eq}} \langle \sigma v \rangle \sim H$
- An example: neutrino decoupling. By dimensional analysis,

$$n_{\text{eq}} \sim T^3 \quad \langle \sigma v \rangle \sim G_F^2 T^2 \quad H \sim T^2 / M_{\text{Pl}}$$

$$T^3 \sim M_W^4 / M_{\text{Pl}} \Rightarrow T \sim \text{MeV}$$

# THERMAL HISTORY OF THE UNIVERSE



# PROBLEMS

The standard model of cosmology answers many questions, but also highlights many others:

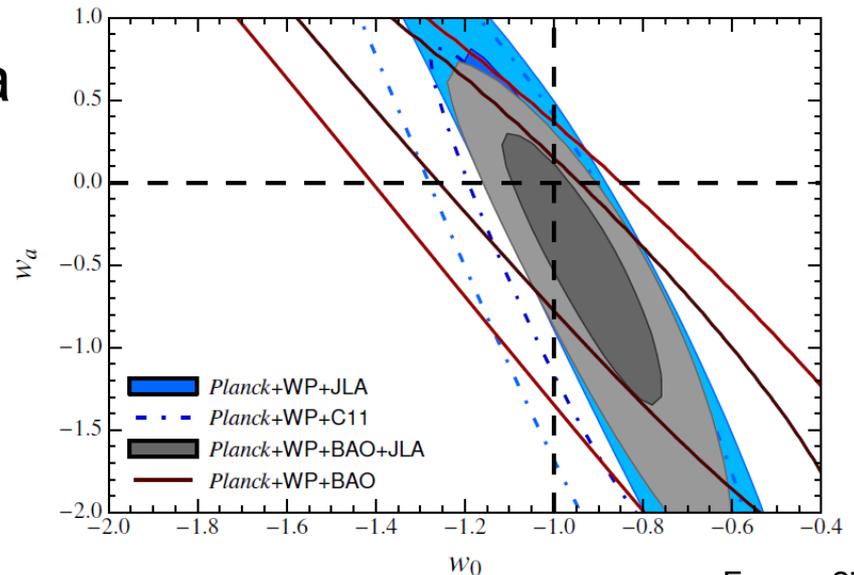
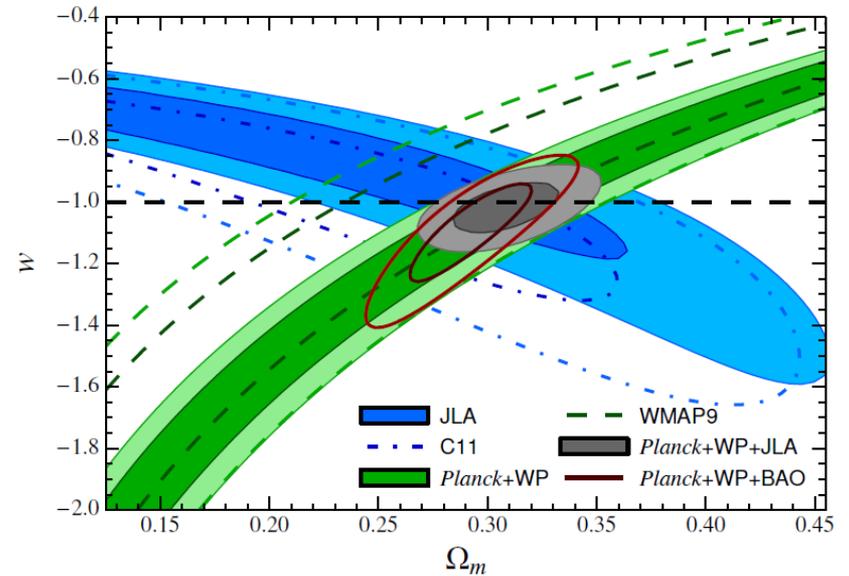
- What is dark matter?
- What is the (small-scale) distribution of dark matter?
- How did structure form?
- What is dark energy?
- Why is the cosmological constant so small?
- Why matter and no anti-matter?
- Why are all energy densities roughly comparable now?
- How did the universe begin?
- ...

Particle physics is required to answer all of these, not least because it is required to understand the hot early Universe

# DARK ENERGY

- The properties of dark energy are now investigated by many methods
  - Supernovae
  - CMB
  - Weak lensing
  - Baryon acoustic oscillations
  - Galaxy cluster abundance
- The results are consistent with a cosmological constant, vacuum energy with  $w = -1$  constant throughout the Universe's history

$$w(z) = w_0 + w_a \frac{z}{1+z}$$



# DARK ENERGY

- $\Omega_\Lambda \approx 0.73 \rightarrow \rho_\Lambda \sim (\text{meV})^4$ : tiny, but all fields contribute

- Quantum mechanics:  
 $\pm \frac{1}{2} \hbar \omega, \quad \omega^2 = k^2 + m^2$

- Quantum field theory:  
 $\pm \frac{1}{2} \int^E d^3k \hbar \omega \sim \pm E^4,$

where  $E$  is the energy scale where the theory breaks down

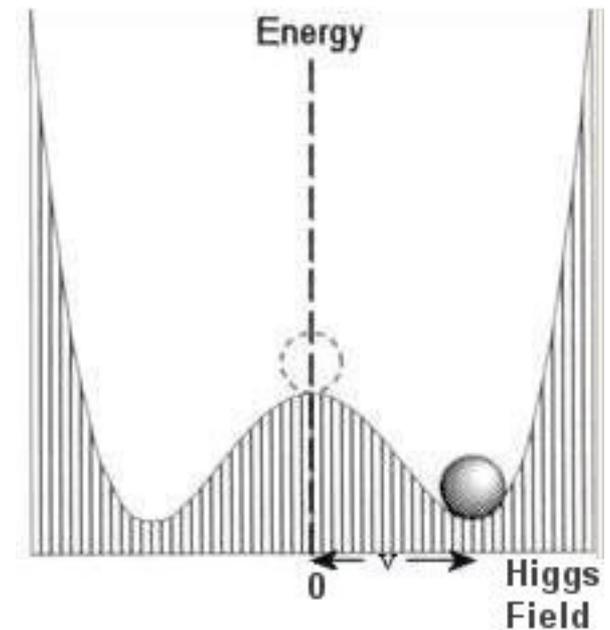
- We expect

$$(M_{\text{Planck}})^4 \sim 10^{120} \rho_\Lambda$$

$$(M_{\text{GUT}})^4 \sim 10^{108} \rho_\Lambda$$

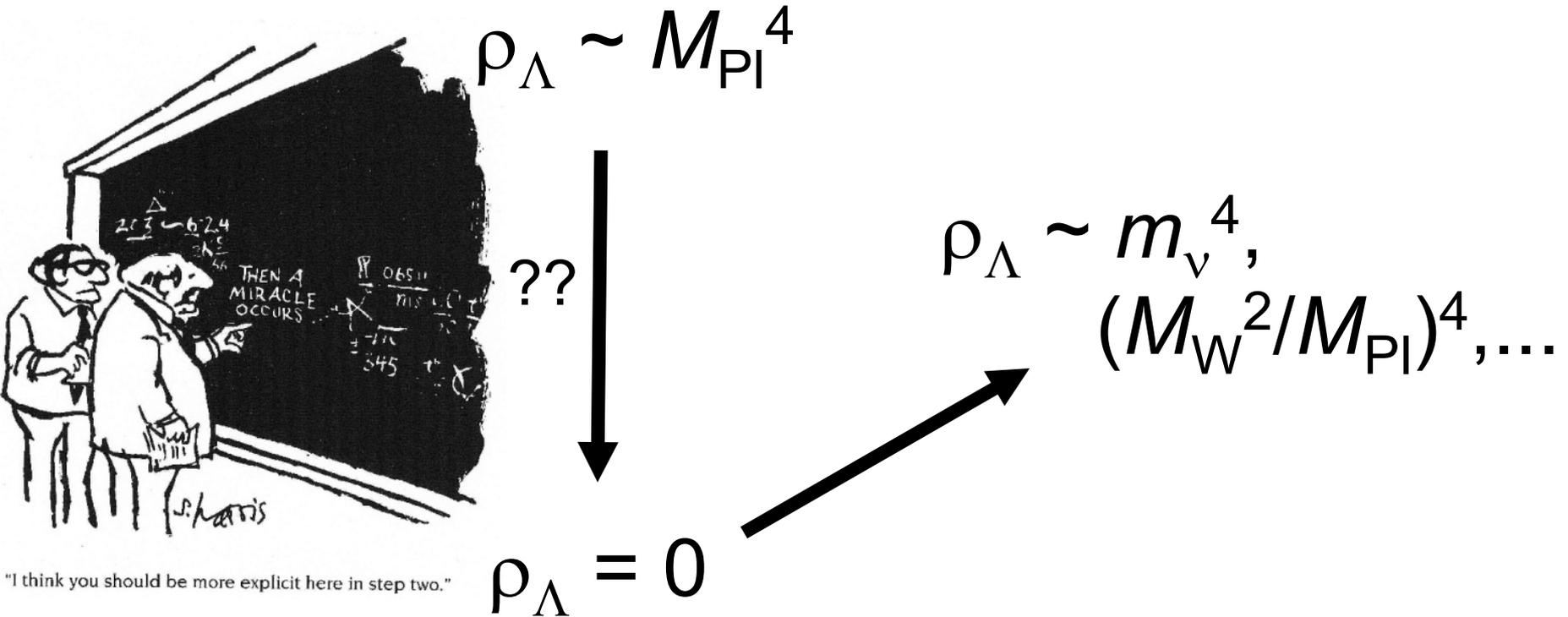
$$(M_{\text{SUSY}})^4 \sim 10^{60} - 10^{90} \rho_\Lambda$$

$$(M_{\text{weak}})^4 \sim 10^{60} \rho_\Lambda$$



# ONE APPROACH

- Small numbers  $\leftrightarrow$  broken symmetry



# ANOTHER APPROACH

$$\rho_{\Lambda} \sim M_{\text{Pl}}^4$$

Many densely-spaced vacua (string landscape, eternal inflation, etc.)

Anthropic principle:  
 $-1 < \Omega_{\Lambda} < 100$

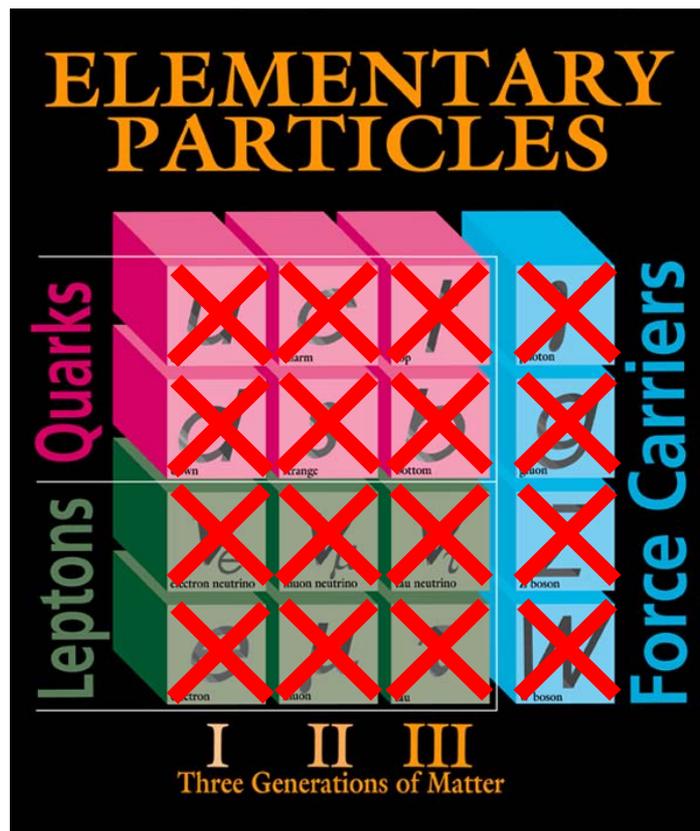
Weinberg (1989)



# DARK ENERGY PROSPECTS

- These approaches are very different. Their only similarity is that the more you think about either one, the more you think the other one must be more promising
- The discrepancy between the expected and measured values of  $\Omega_\Lambda$  is the greatest hierarchy problem in particle physics, not just because it is numerically large, but because we think we understand meV-scale physics
- Ways forward
  - Constrain DE properties, see if it deviates from a cosmological constant or indicates a deviation from GR
  - Make a breakthrough in understanding quantum gravity
  - Learn something unexpected about fundamental scalars

# DARK MATTER



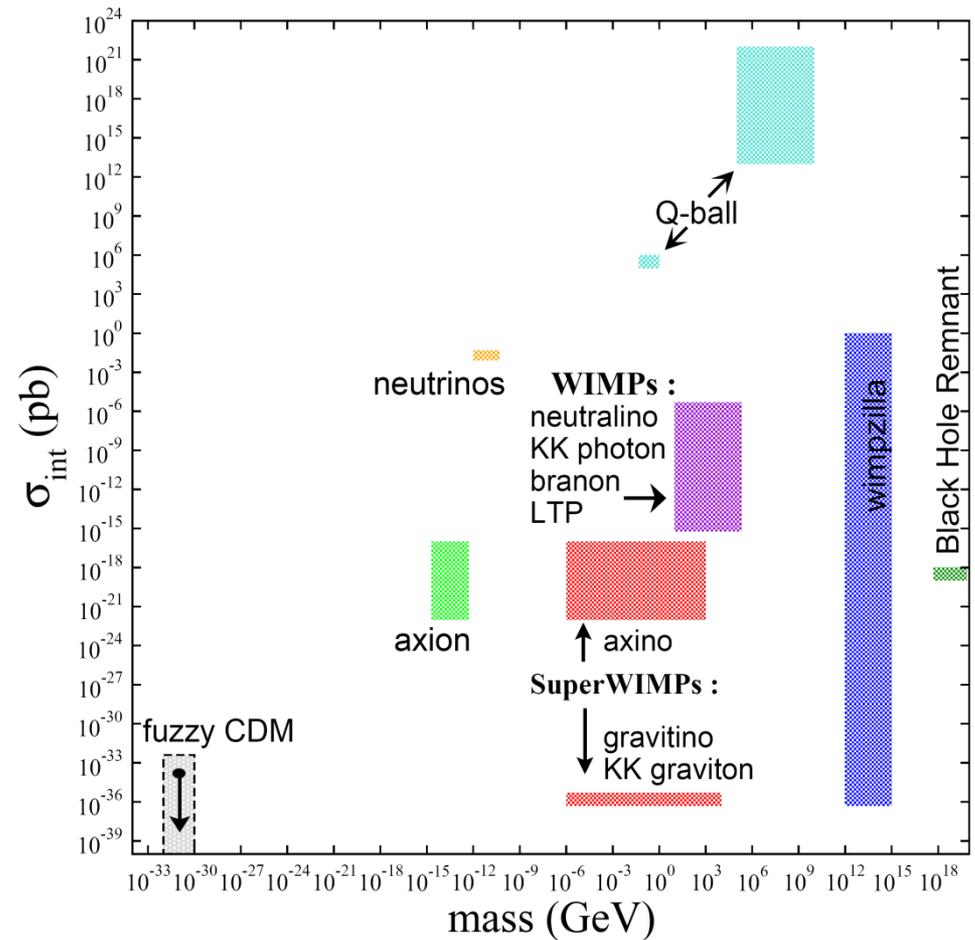
Known DM properties

- Gravitationally interacting
- Not short-lived
- Not hot
- Not baryonic

Unambiguous evidence for new particles

# DARK MATTER CANDIDATES

- There are many
- Masses and interaction strengths span many, many orders of magnitude, but the gauge hierarchy problem especially motivates particles with weak-scale masses



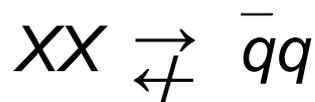
HEPAP/AAAC DMSAG Subpanel (2007)

# FREEZE OUT: QUALITATIVE

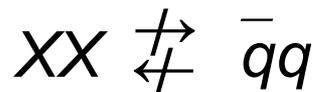
(1) Assume a new heavy particle  $X$  is initially in thermal equilibrium:



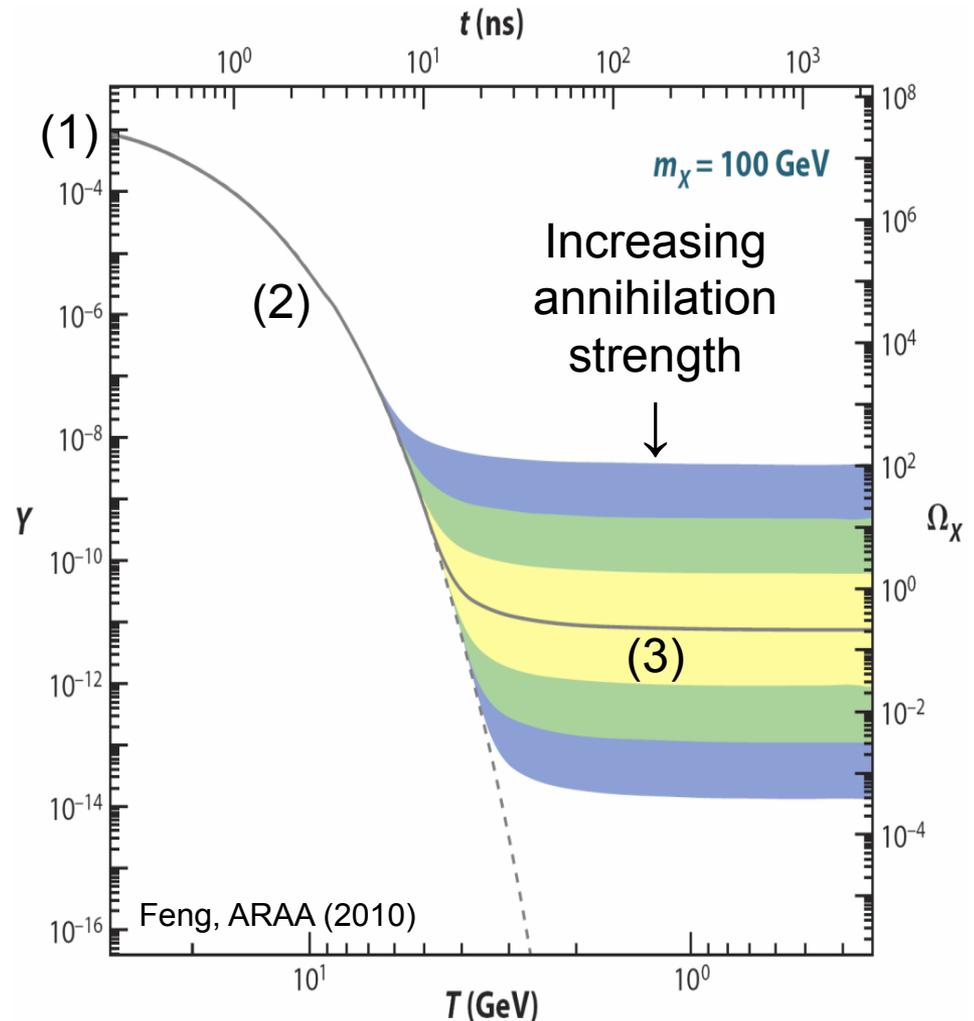
(2) Universe cools:



(3) Universe expands:



Zeldovich et al. (1960s)



# FREEZE OUT: MORE QUANTITATIVE

- The Boltzmann equation:

$$\frac{dn}{dt} = -3Hn - \langle \sigma v \rangle [n^2 - n_{\text{eq}}^2]$$

$\uparrow$  Dilution from expansion

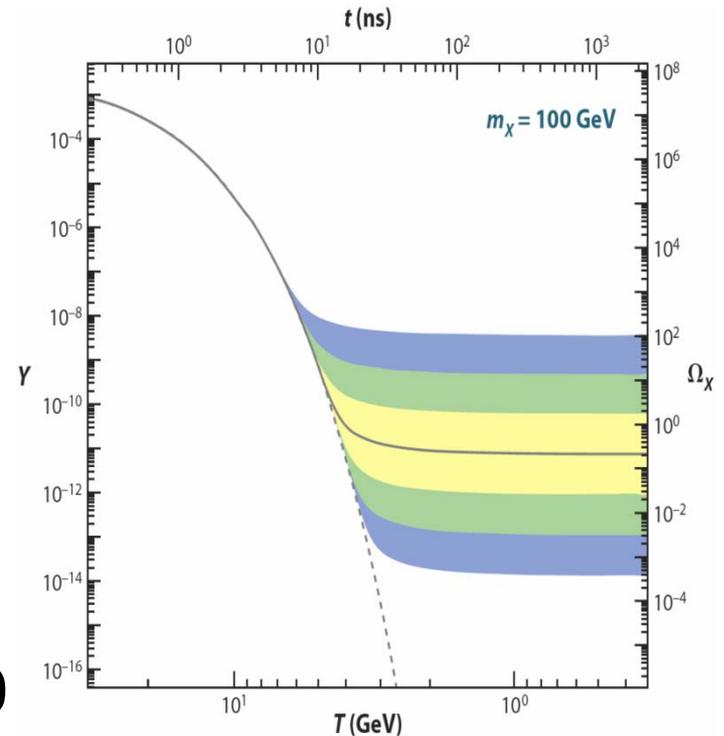
$\uparrow$   $\chi\chi \rightarrow f\bar{f}$        $f\bar{f} \rightarrow \chi\chi$

- $n \approx n_{\text{eq}}$  until interaction rate drops below expansion rate:

$$n_{\text{eq}} \langle \sigma v \rangle \sim H$$

$\uparrow$   $\uparrow$   $\uparrow$   
 $(mT)^{3/2} e^{-m/T}$   $m^{-2}$   $T^2/M_{\text{Pl}}$

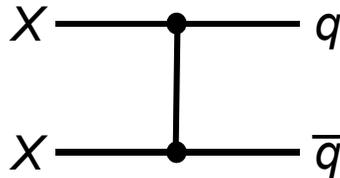
- Might expect freeze out at  $T \sim m$ , but the universe expands *slowly*!  
First guess:  $m/T \sim \ln(M_{\text{Pl}}/m_W) \sim 40$



# THE WIMP MIRACLE

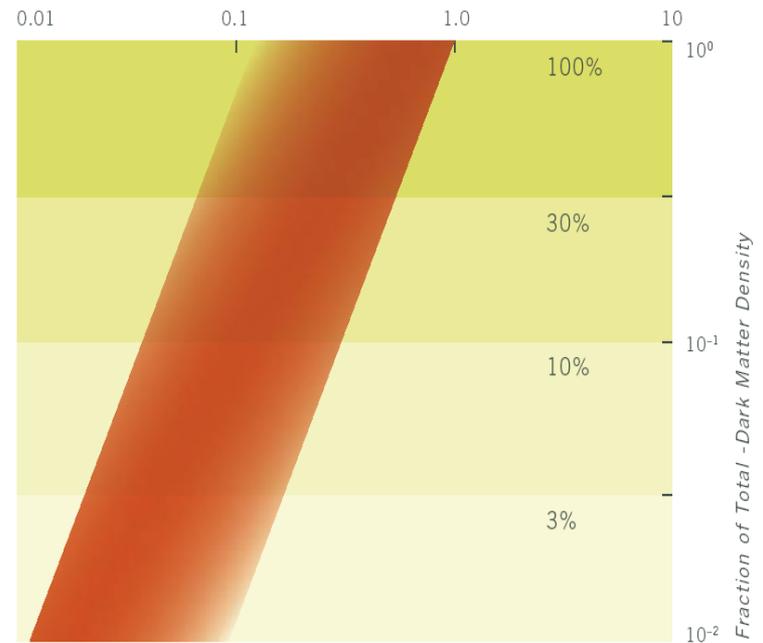
- The relation between  $\Omega_X$  and annihilation strength is wonderfully simple:

$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4}$$



- $m_X \sim 100 \text{ GeV}$ ,  $g_X \sim 0.6 \rightarrow \Omega_X \sim 0.1$

Mass of Dark Matter Particle from Supersymmetry (TeV)

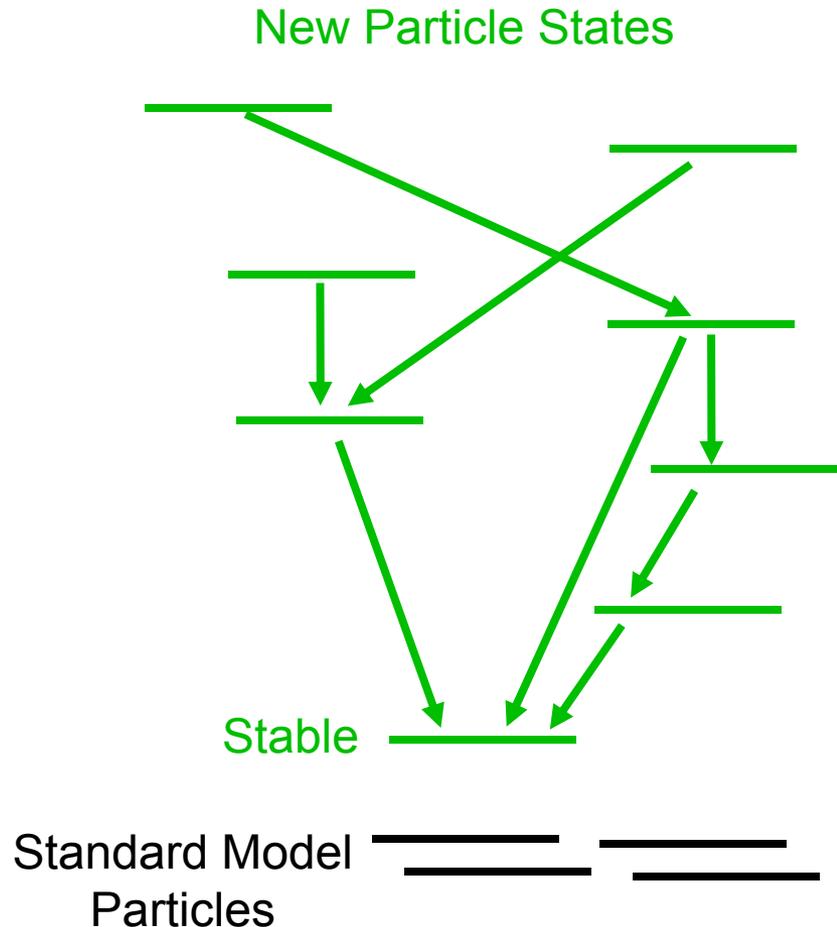


LHC/ILC HEPAP, Matchev et al. (2005)

- Remarkable coincidence: particle physics independently predicts particles with the right density to be dark matter

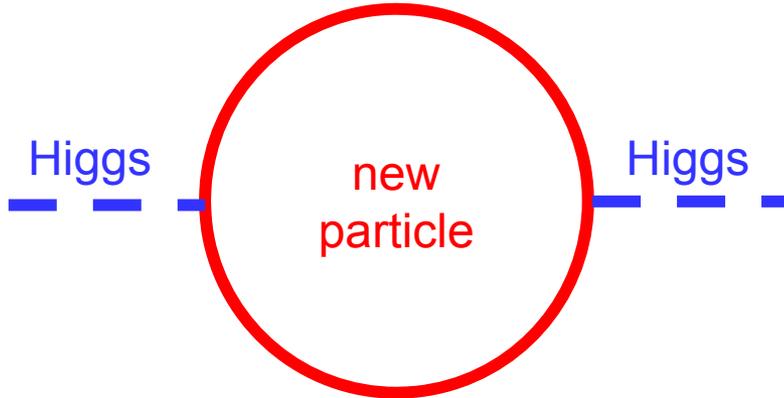
# WIMP STABILITY

- The WIMP Miracle is very well appreciated, and it is a quantitative feature. But its success relies on some less well-advertised qualitative features
- First, the WIMP must be stable
- How natural is this? *A priori*, not very: the only stable particles we know about are very light

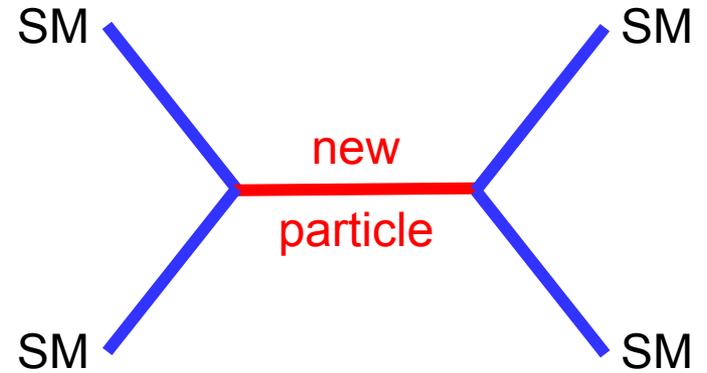


# LEP'S COSMOLOGICAL LEGACY

Gauge Hierarchy requires



Precision EW excludes



In some cases, there are even stronger reasons to exclude these 4-particle interactions (e.g., proton decay in SUSY)

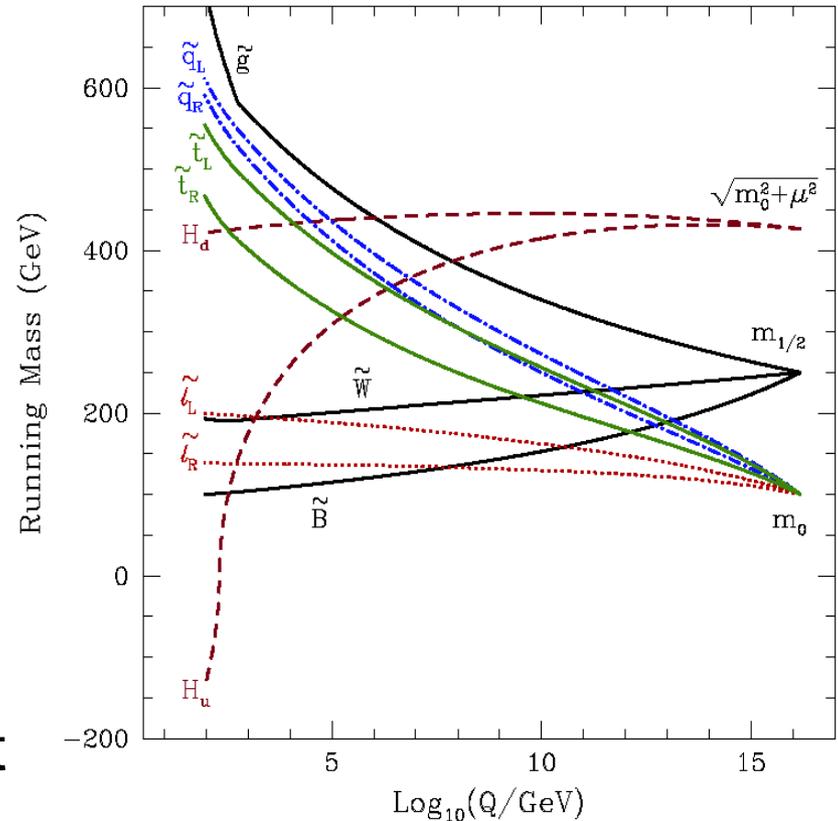
- Simple solution: impose a discrete parity, so all interactions require *pairs* of new particles. This also makes the lightest new particle stable:

LEP constraints  $\leftrightarrow$  Discrete Symmetry  $\leftrightarrow$  Stability

Cheng, Low (2003); Wudka (2003)

# WIMP NEUTRALITY

- WIMPs must also be neutral
- How natural is this? Again, *a priori*, not very: what is the chance that the lightest new particle happens to be neutral?
- In fact, in many cases (SUSY, extra dims, ...), masses are “proportional” to couplings, so neutral particles are the lightest



Bottom line: WIMPs, new particles that are *stable* and *neutral* with  $\Omega \sim 0.1$ , appear in many models of new particle physics

# LECTURE 1 SUMMARY

- The revolution in cosmology has produced remarkable progress
- This progress also highlights puzzles that require particle physics answers
- Cosmology and particle physics both point to the weak scale for new particles
- Next time: what are the opportunities for probing the weak scale with dark matter searches?

# OUTLINE

## LECTURE 1

Essential Cosmology: Contents and History of the Universe

## LECTURE 2

WIMP Dark Matter: Candidates and Methods of Detection

## LECTURE 3

Inflation, Gravitinos, and Hidden Sectors

# WIMP EXAMPLES

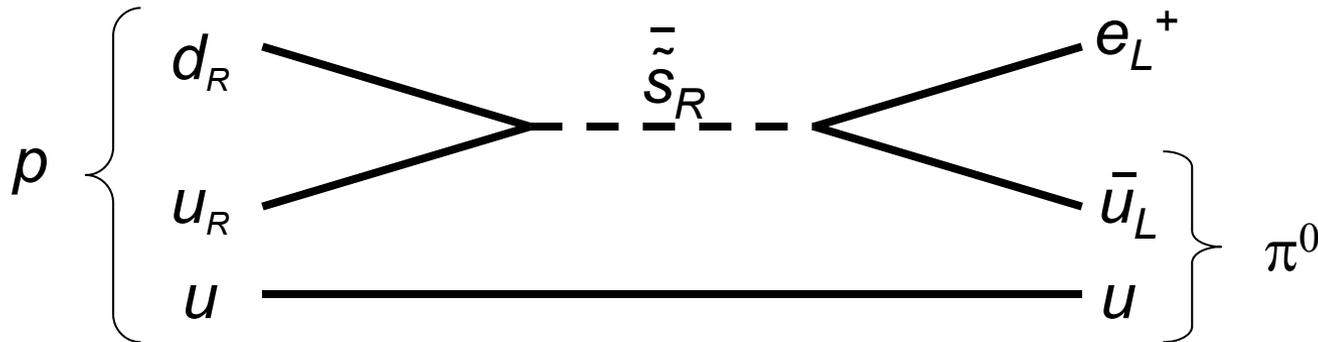
- Weakly-interacting massive particles: many examples, broadly similar, but different in detail
- The prototypical WIMP: neutralinos in supersymmetry  
Goldberg (1983); Ellis et al. (1983)
- KK  $B^1$  (“KK photons”) in universal extra dimensions  
Servant, Tait (2002); Cheng, Feng, Matchev (2002)

# NEUTRAL SUSY PARTICLES

Spin	U(1) $M_1$	SU(2) $M_2$	Up-type $\mu$	Down-type $\mu$	$m_{\tilde{\nu}}$	$m_{3/2}$
2						G graviton
3/2		Neutralinos: $\{\chi \equiv \chi_1, \chi_2, \chi_3, \chi_4\}$				$\tilde{G}$ gravitino
1	$B$	$W^0$	↑			
1/2	$\tilde{B}$ Bino	$\tilde{W}^0$ Wino	$\tilde{H}_u$ Higgsino	$\tilde{H}_d$ Higgsino	$\nu$	
0			$H_u$	$H_d$	$\tilde{\nu}$ sneutrino	

# R-PARITY AND STABLE LSPS

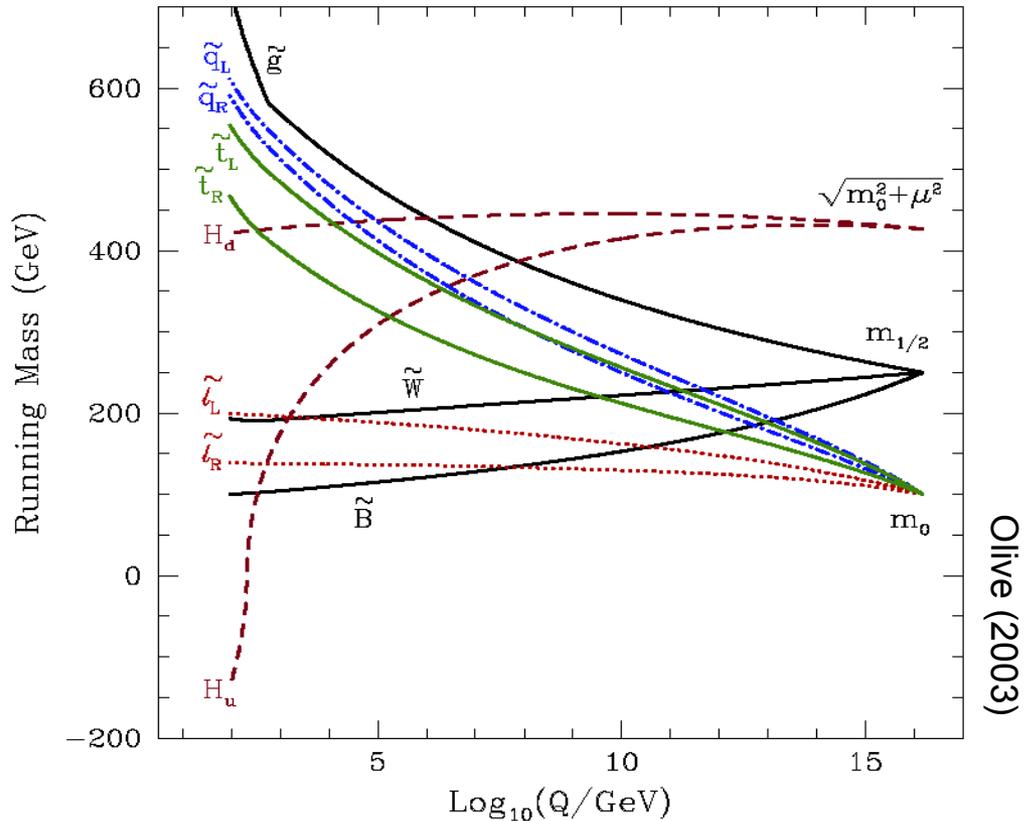
- One problem: proton decay



- Forbid this with R-parity conservation:  $R_p = (-1)^{3(B-L)+2S}$ 
  - SM particles have  $R_p = 1$ , SUSY particles have  $R_p = -1$
  - Require  $\Pi R_p = 1$  at all vertices
- Consequence: the lightest SUSY particle (LSP) is stable!

# WHAT'S THE LSP?

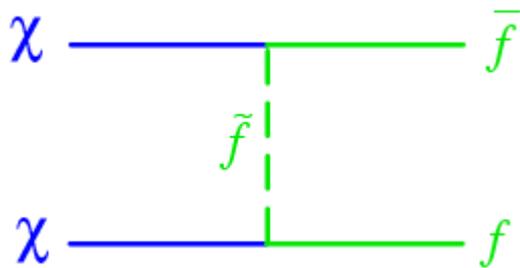
- High-scale  $\rightarrow$  weak scale through RGEs
- Gauge couplings increase masses; Yukawa couplings decrease masses
- “typical” LSPs:  $\chi$ ,  $\tilde{\tau}_R$



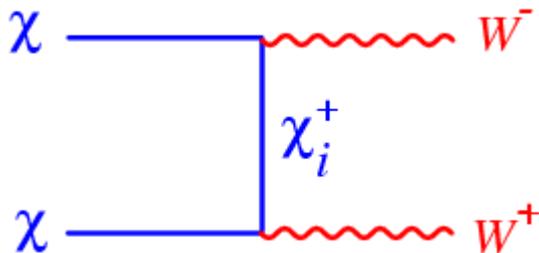
Particle physics alone  $\rightarrow$  neutral, stable, cold dark matter

# RELIC DENSITY

- Neutralinos annihilate through *many* processes. [→]  
But there are typically two dominant classes:



- $\chi$  are Majorana fermions, so Pauli exclusion  $\rightarrow S_{in} = 0$ ,  $L$  conservation  $\rightarrow$ 
  - $P$ -wave suppression:  $\sigma v \sim \sigma_0 + \sigma_1 v^2$ ,  
 $mv^2/2 = 3T/2 \rightarrow v^2 \sim 3T/m \sim 0.1$
  - $m_f/m_W$  suppression



- Gauge boson diagrams suppressed for  $\chi \approx$  Bino

Bottom line: annihilation is typically suppressed,  $\Omega_{DM} h^2$  is typically high

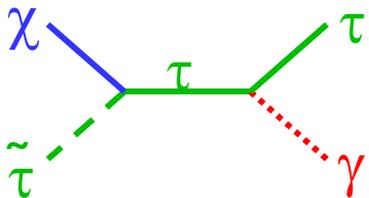
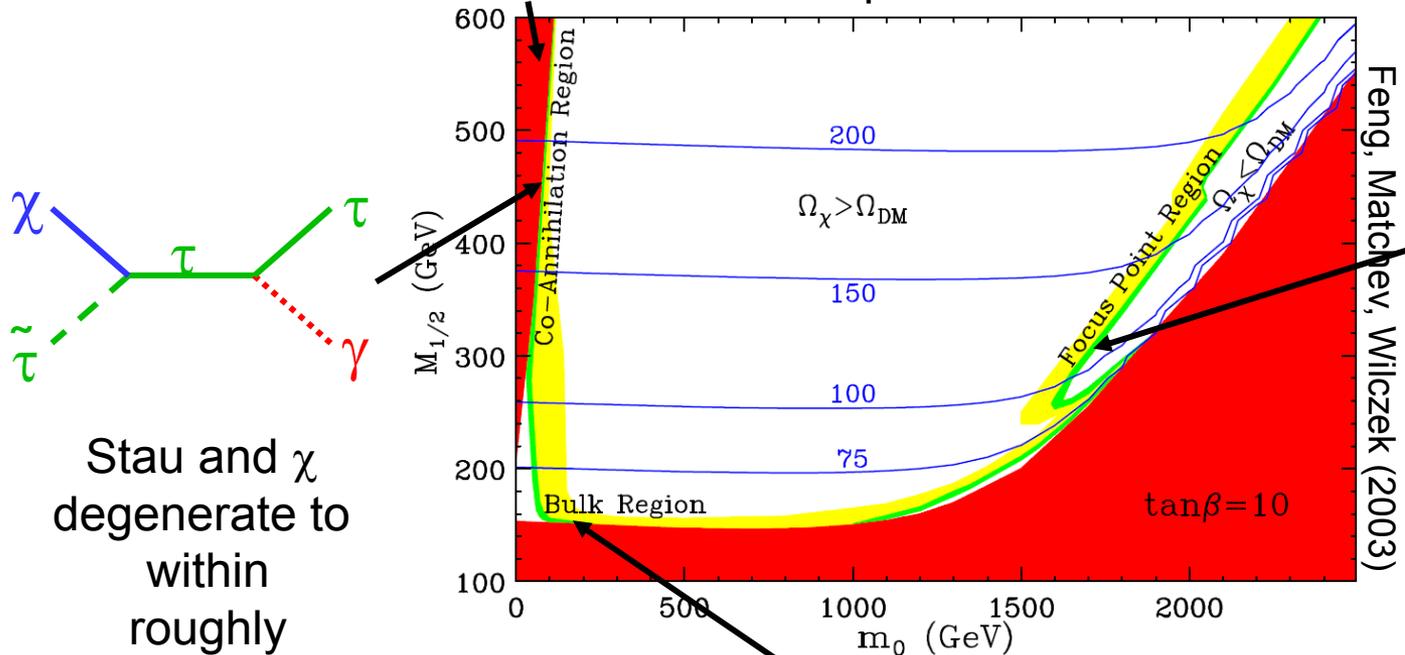


# COSMOLOGICALLY-PREFERRED SUSY

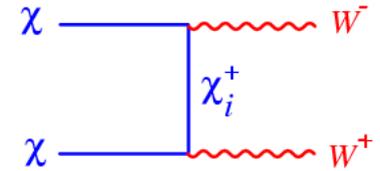
Typically get too much DM, but there are mechanisms for reducing it

Excluded:  
Stau LSP

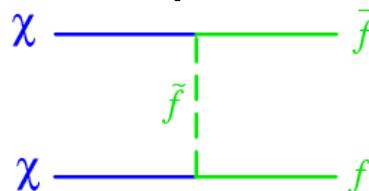
Yellow: pre-WMAP  
Green: post-WMAP



Stau and  $\chi$   
degenerate to  
within  
roughly  
 $T \sim m/25$



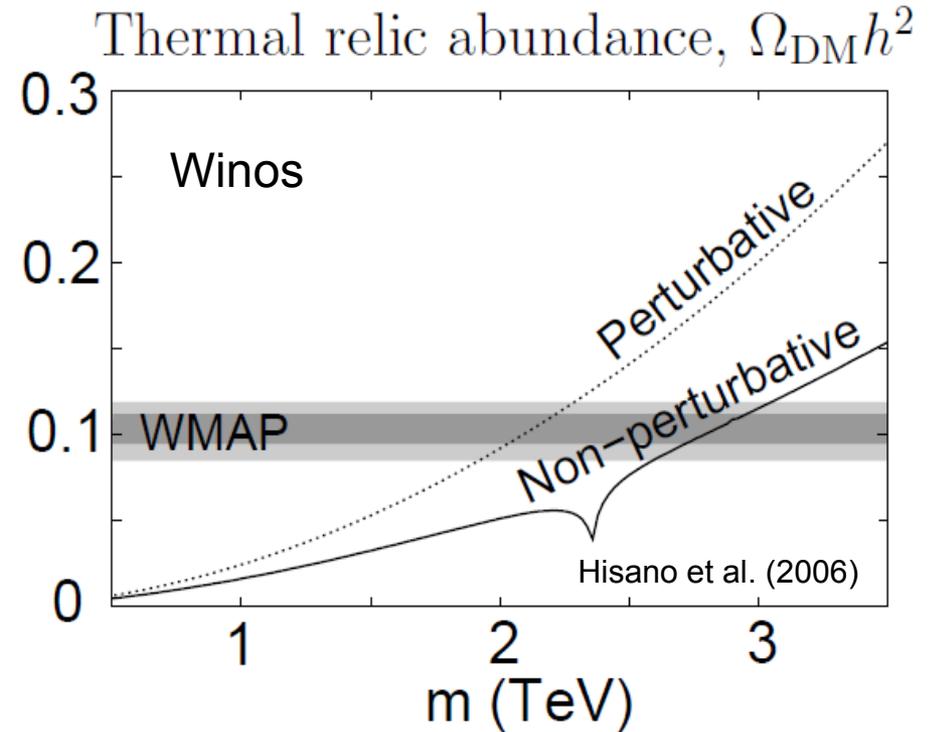
Higgsino-Bino  
Neutralinos



Light sfermions

# COSMOLOGICALLY-PREFERRED SUSY

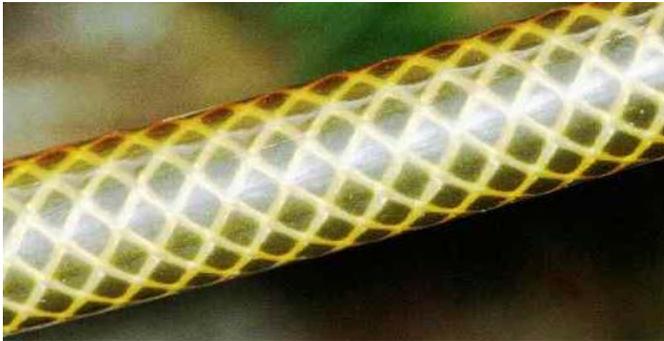
- After LHC8, there remain several neutralino candidates with the right relic density
  - Co-annihilating DM
    - $\chi$ ,  $\tilde{\tau}_R$  degenerate,  $m < 600$  GeV
  - Focus-point DM
    - Bino-Higgsino mixture,  $m < 1$  TeV
  - Wino-like DM
    - $m \sim 2.7$ -3 TeV
- Note: in this context, cosmology provides upper bounds!
- The Wino scenario is probably excluded by indirect detection, but the other two remain viable, provide interesting targets for LHC13 and future colliders



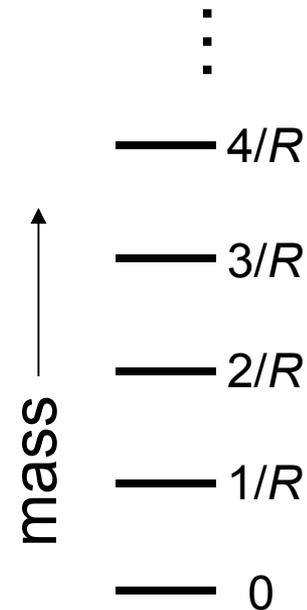
$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4}$$

# KK DARK MATTER

- Consider 1 extra spatial dimensions curled up in a small circle



- Particles moving in extra dimensions appear as a set of copies of normal particles.



# KK-PARITY

Appelquist, Cheng, Dobrescu (2001)

- Problem: many extra 4D fields; some with mass  $n/R$ , but some are massless! E.g., 5D gauge field:

$$V_\mu(x^\mu, y) = \underbrace{V_\mu(x^\mu)}_{\text{good}} + \sum_n V_\mu^n(x^\mu) \cos(ny/R) + \sum_m V_\mu^m(x^\mu) \sin(my/R)$$

$$V_5(x^\mu, y) = \underbrace{V_5(x^\mu)}_{\text{bad}} + \sum_n V_5^n(x^\mu) \cos(ny/R) + \sum_m V_5^m(x^\mu) \sin(my/R)$$

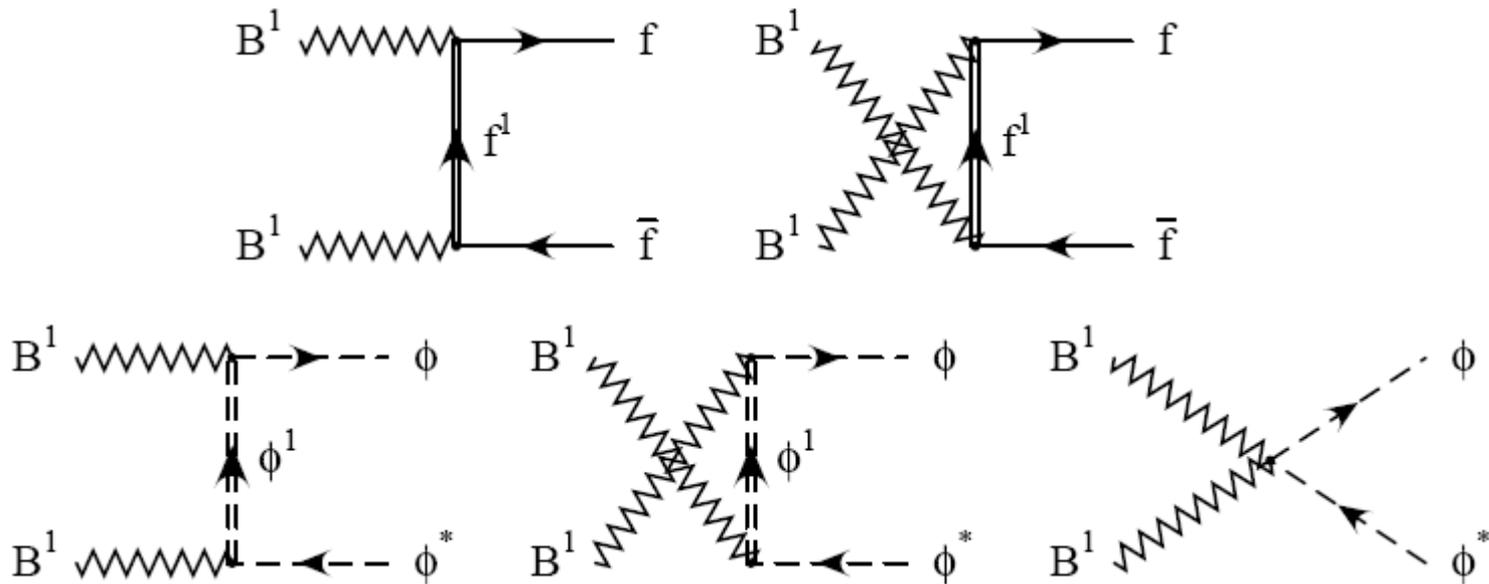
- Solution: compactify on  $S^1/Z_2$  orbifold

$$y \rightarrow -y : \quad V_\mu \rightarrow V_\mu \quad V_5 \rightarrow -V_5$$

- Consequence: KK-parity  $(-1)^{KK}$  conserved: interactions require an even number of odd KK modes
- 1<sup>st</sup> KK modes must be pair-produced at colliders
- LKP (lightest KK particle) is stable – dark matter!

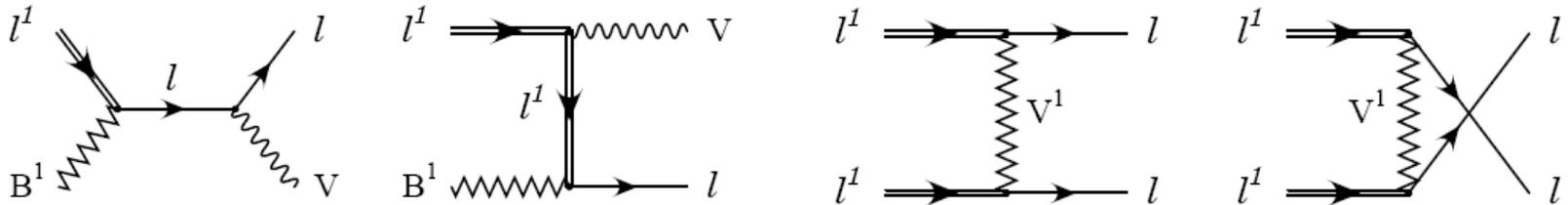
# B<sup>1</sup> ANNIHILATION

- The level-1 KK hypercharge gauge boson B<sup>1</sup> is often the LKP, is neutral, and so is a natural DM candidate
- It's a massive gauge boson, annihilates through S-wave processes, so preferred masses are larger than for Binos

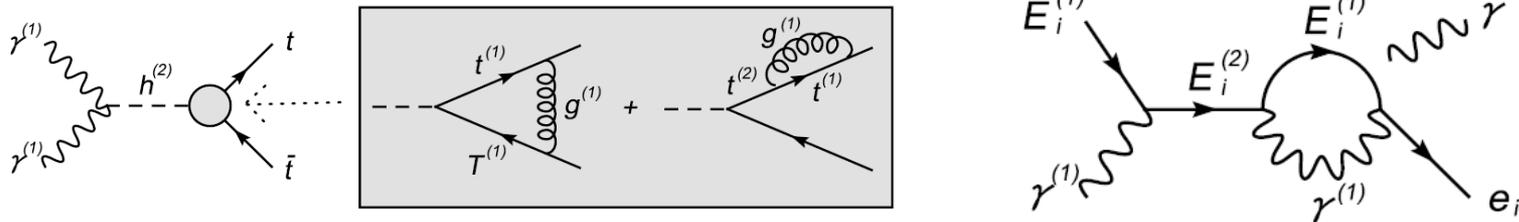


# MORE $B^1$ ANNIHILATION

- Minimal UED has a compressed spectrum, so co-annihilation is natural. In contrast to SUSY, these typically add to the relic density

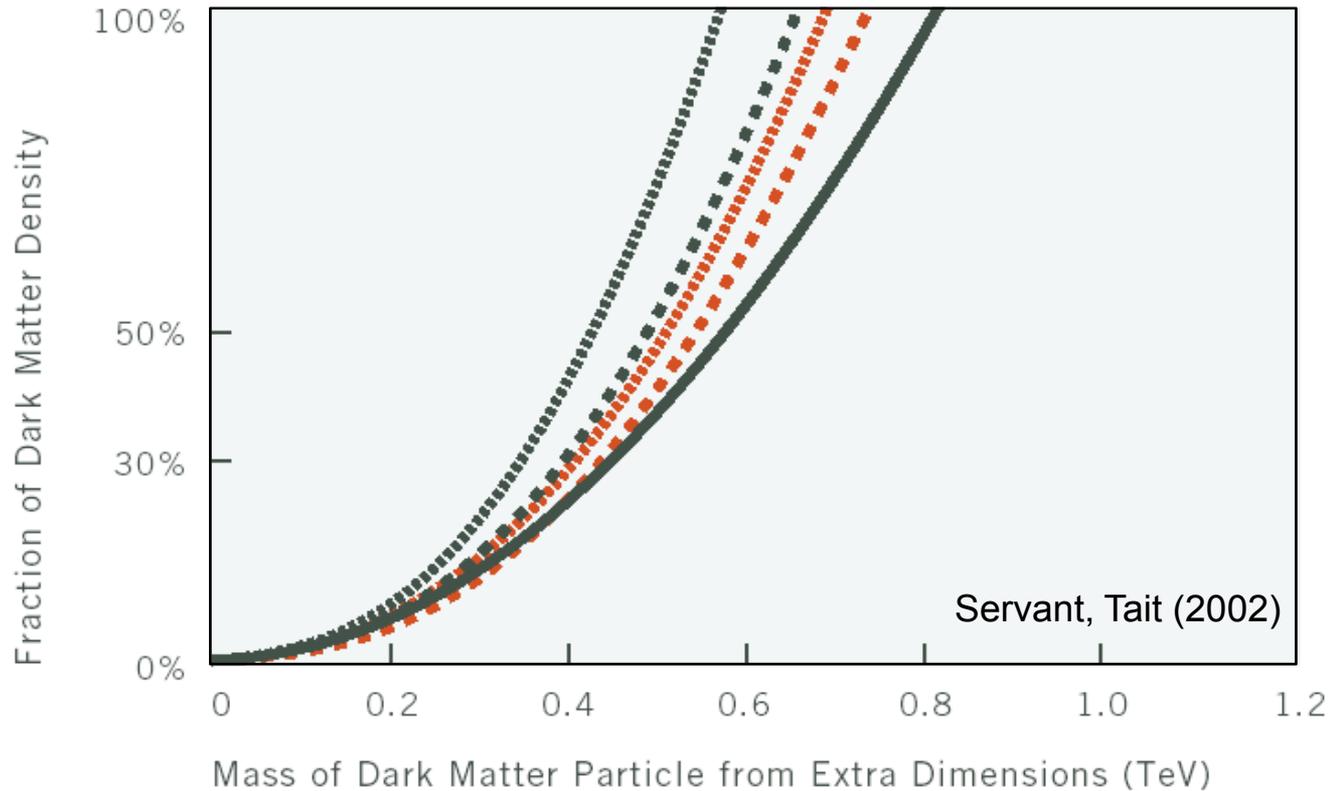


- Level-2 KK resonances



Servant, Tait (2002); Burnell, Kribs (2005)  
 Kong, Matchev (2005); Kakizaki, Matsumoto, Sato, Senami (2005)

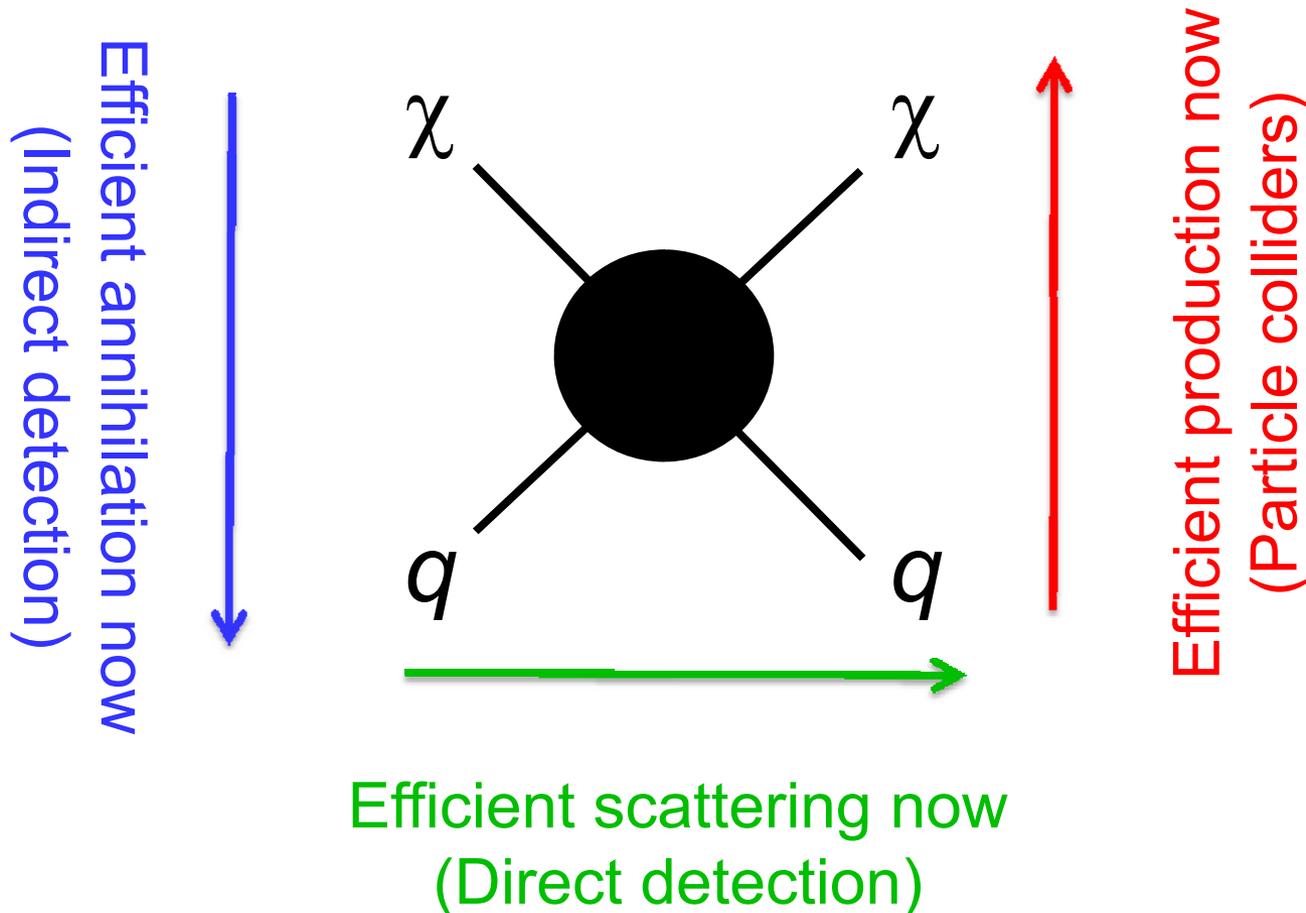
# KK DARK MATTER RELIC DENSITY



Prediction for  $\Omega_{B^{(1)}} h^2$       The solid line is the case for  $B^{(1)}$  alone, and the dashed and dotted lines correspond to the case in which there are one (three) flavors of nearly degenerate  $e_R^{(1)}$ . For each case, the black curves (upper of each pair) denote the case  $\Delta = 0.01$  and the red curves (lower of each pair)  $\Delta = 0.05$ .

# WIMP DETECTION

Correct relic density  $\rightarrow$  Efficient annihilation then



# DIRECT DETECTION

- WIMP properties
  - If mass is 100 GeV, local density is  $\sim 1$  per liter
  - velocity  $\sim 10^{-3} c$

DM

$e, \gamma$

Look for normal matter recoiling from WIMP collisions in detectors deep underground

Dark matter elastically scatters off nuclei

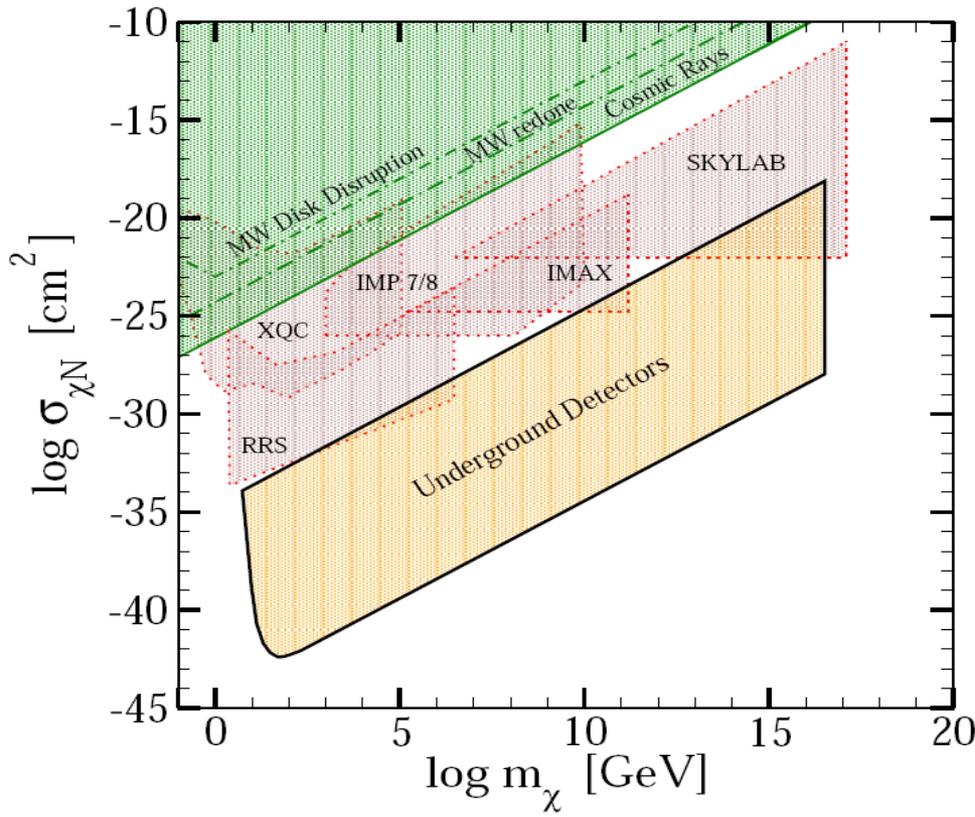
Nuclear recoils detected by phonons, scintillation, ionization, ...

Attisha

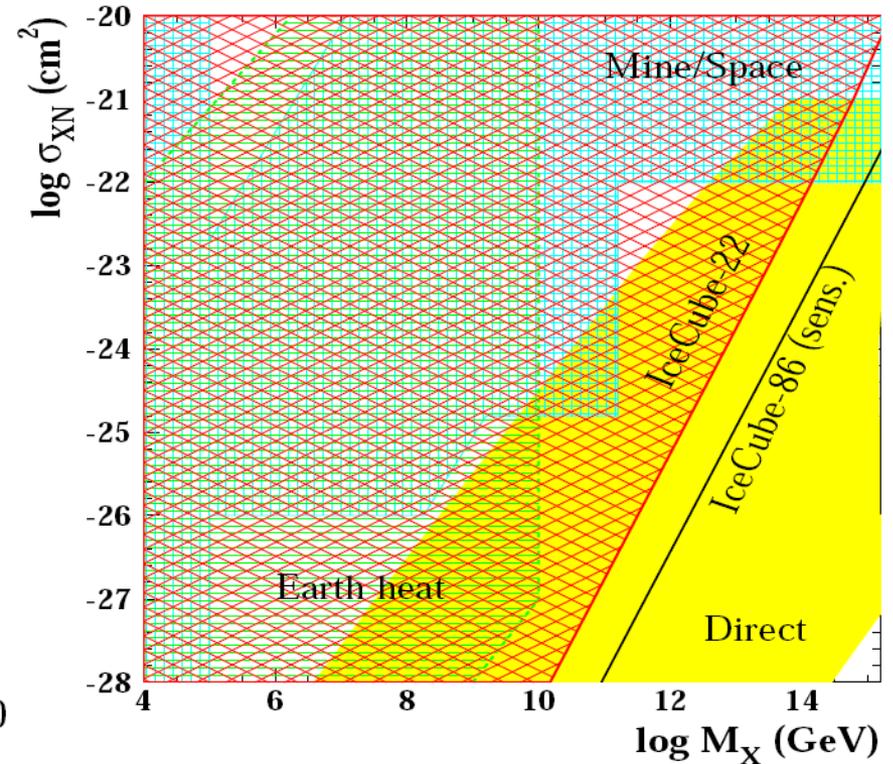
# THE BIG PICTURE: UPPER BOUND

- What is the upper bound?

- Strongly-interacting window is now closed



Mack, Beacom, Bertone (2007)

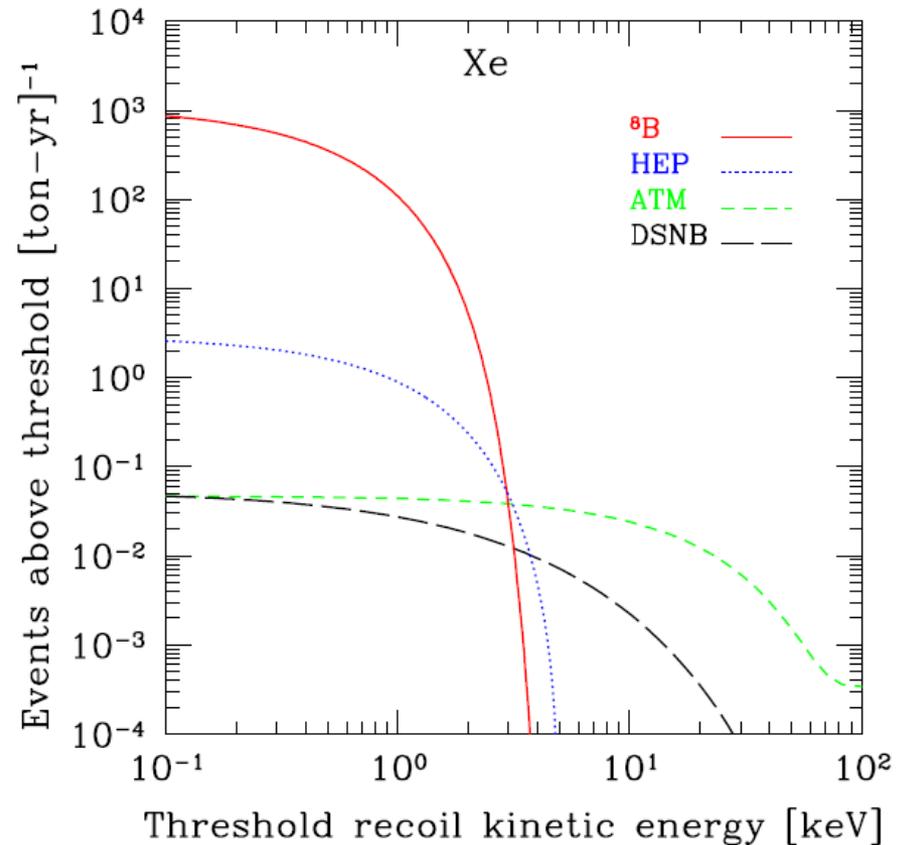


Albuquerque, de los Heros (2010)

# THE BIG PICTURE: LOWER BOUND

- Is there (effectively) a lower bound?
- Solar, atmospheric, and diffuse supernova background neutrinos provide a difficult background
- The limits of background-free, non-directional direct detection searches (and also the metric prefix system!) will be reached by  $\sim 10$  ton experiments probing

$$\sigma \sim 1 \text{ yb} (10^{-3} \text{ zb}, 10^{-12} \text{ pb}, 10^{-48} \text{ cm}^2)$$



Strigari (2009); Gutlein et al. (2010)

# SPIN-INDEPENDENT VS. SPIN-DEPENDENT SCATTERING

- Consider neutralinos with quark interactions

$$\mathcal{L} = \sum_{q=u,d,s,c,b,t} \left( \alpha_q^{\text{SD}} \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q + \alpha_q^{\text{SI}} \bar{\chi} \chi \bar{q} q \right)$$

- DM particles now have  $v \sim 10^{-3} c$ . In the non-relativistic limit, the first terms reduce to a spin-spin interactions, and so are called spin-dependent interactions
- The second terms are spin-independent interactions; focus on these here

# SPIN-INDEPENDENT THEORY

- Theories give DM-quark interactions, but experiments measure DM-nucleus cross sections

$$\sigma_{\text{SI}} = \frac{4}{\pi} \mu_N^2 \sum_q \alpha_q^{\text{SI}2} \left[ Z \frac{m_p}{m_q} f_{T_q}^p + (A - Z) \frac{m_n}{m_q} f_{T_q}^n \right]^2,$$

where  $\mu_N = \frac{m_\chi m_N}{m_\chi + m_N}$  is the reduced mass, and  $f_{T_q}^{p,n} = \frac{\langle p, n | m_q \bar{q}q | p, n \rangle}{m_{p,n}}$

is the fraction of the nucleon's mass carried by quark  $q$ , with

$$\begin{aligned} f_{T_u}^p &= 0.020 \pm 0.004 & f_{T_u}^n &= 0.014 \pm 0.003 & f_{T_s}^p &= 0.118 \pm 0.062 & f_{T_s}^n &= 0.118 \pm 0.062 \\ f_{T_d}^p &= 0.026 \pm 0.005 & f_{T_d}^n &= 0.036 \pm 0.008 & f_{T_{c,b,t}}^{p,n} &= \frac{2}{27} f_{T_G}^{p,n} = \frac{2}{27} (1 - f_{T_u}^{p,n} - f_{T_d}^{p,n} - f_{T_s}^{p,n}) \end{aligned}$$

The last one accounts for gluon couplings through heavy quark loops.

- This may be parameterized by  $\sigma_A = \frac{\mu_A^2}{M_*^4} [f_p Z + f_n (A - Z)]^2$ ,

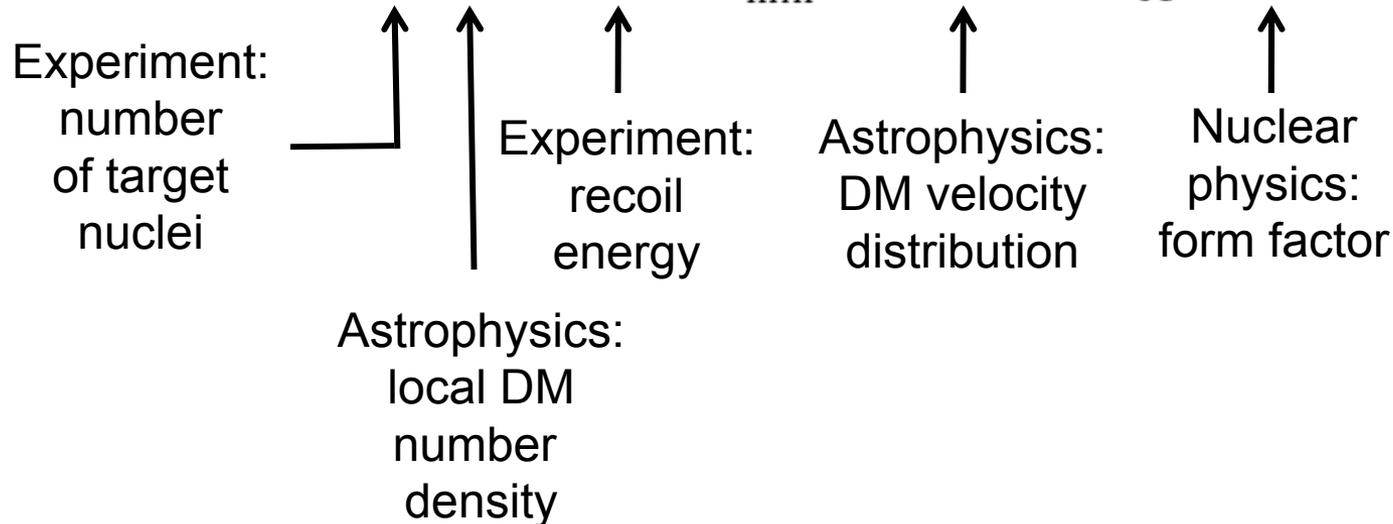
where  $f_{p,n}$  are the nucleon level couplings. Note that  $f_p$  and  $f_n$  are not necessarily equal.

# SPIN-INDEPENDENT EXPERIMENT

- The rate observed in a detector is  $R = \sigma_A I_A$ , where

$$\sigma_A = \frac{\mu_A^2}{M_*^4} [f_p Z + f_n (A - Z)]^2$$

$$I_A = N_T n_X \int dE_R \int_{v_{\min}}^{v_{\text{esc}}} d^3v f(v) \frac{m_A}{2v\mu_A^2} F_A^2(E_R)$$

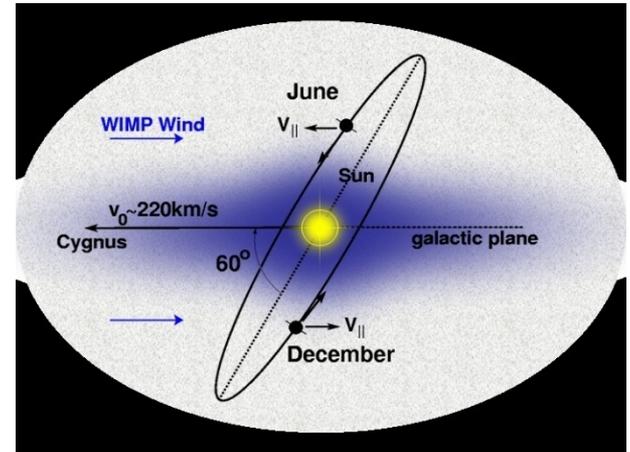


- Results are typically reported assuming  $f_p = f_n$ , so  $\sigma_A \sim A^2$ , and scaled to a single nucleon

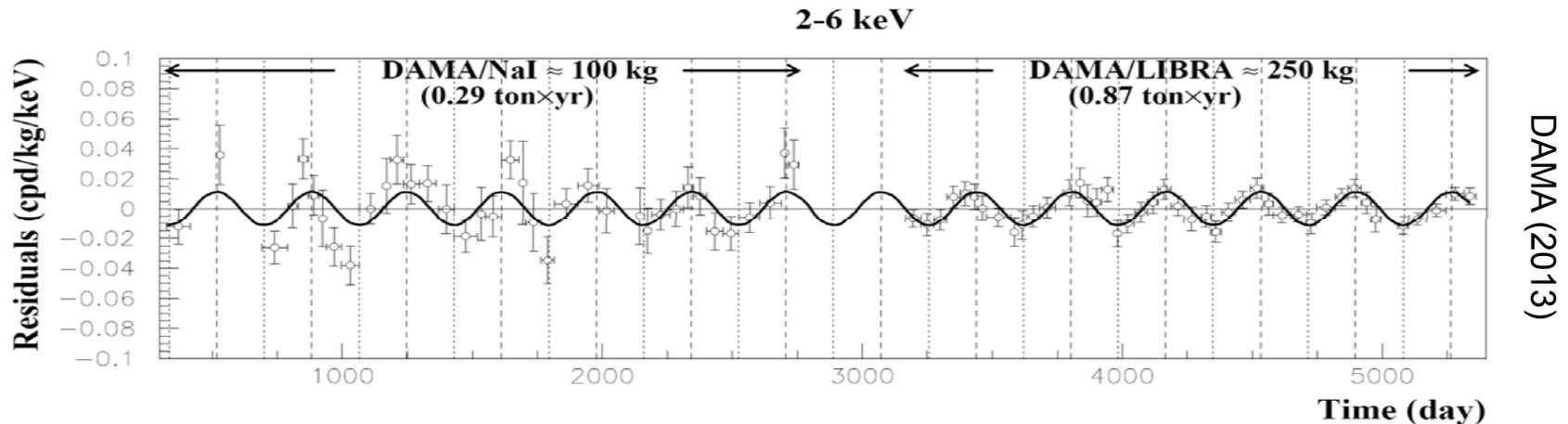
# CURRENT STATUS

There are claimed signals: Collision rate should change as Earth's velocity adds with the Sun's  $\rightarrow$  annual modulation

Drukier, Freese, Spergel (1986)



DAMA:  $9\sigma$  signal with  $T \sim 1$  year, max  $\sim$  June 2

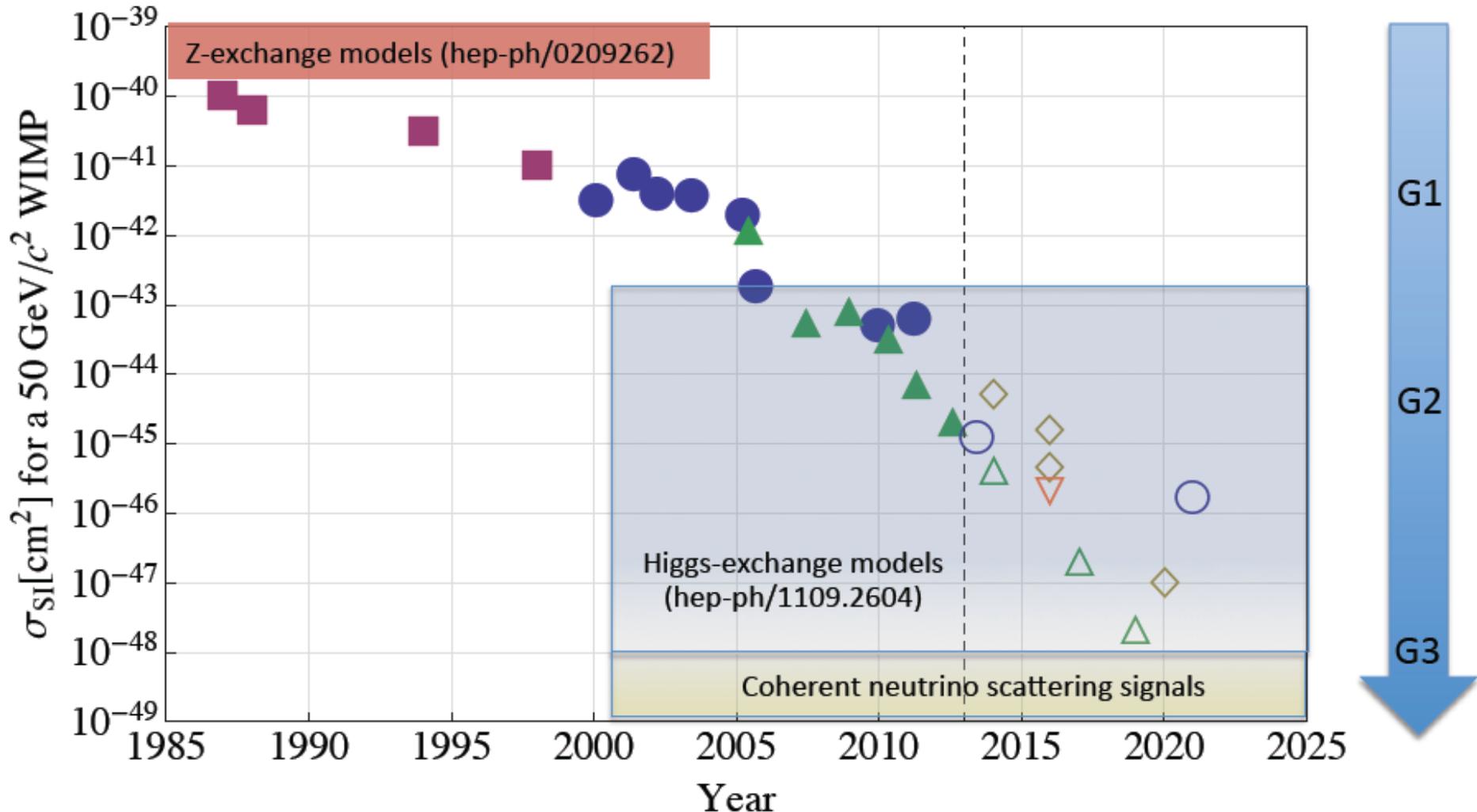


DAMA signal now supplemented by others



# MOORE'S LAW FOR DARK MATTER

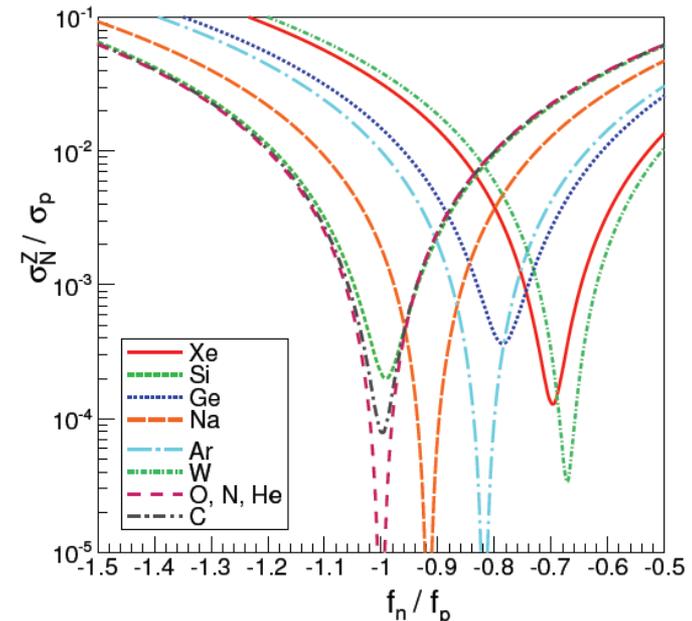
Evolution of the WIMP–Nucleon  $\sigma_{SI}$



# ISOSPIN-VIOLATING DARK MATTER

- The direct detection anomalies have motivated many DM ideas. As an example, consider a particularly simple model with HEP implications: IVDM
- Recall that DM scattering off nuclei is
  - $\sigma_A \sim [f_p Z + f_n (A-Z)]^2$
- Typically assume
  - $f_n = f_p, \sigma_A \sim A^2$
- IVDM relaxes this assumption, introduces 1 new parameter:  $f_n / f_p$

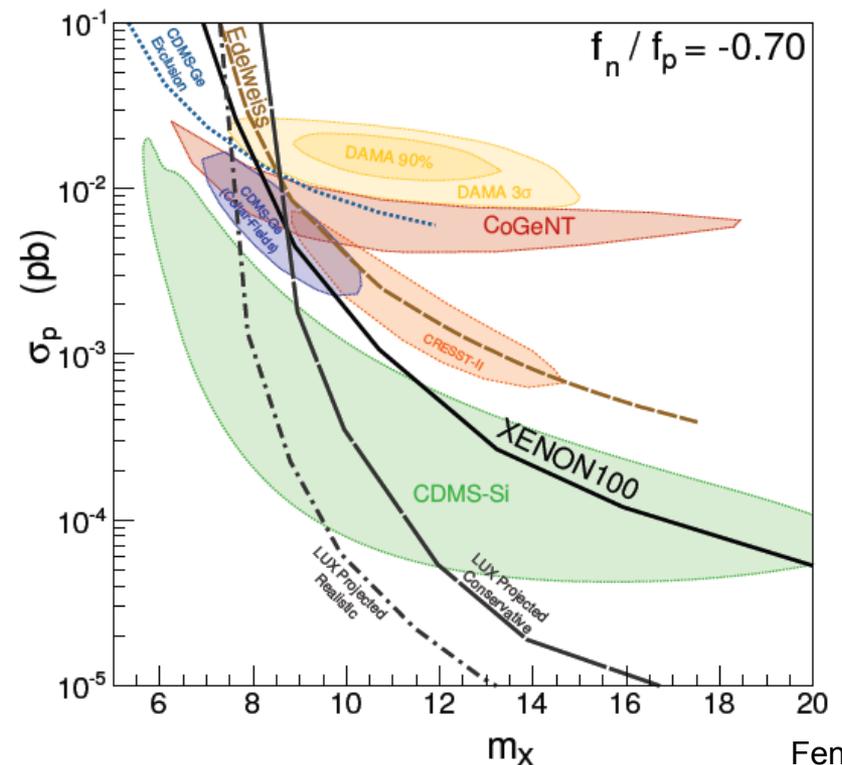
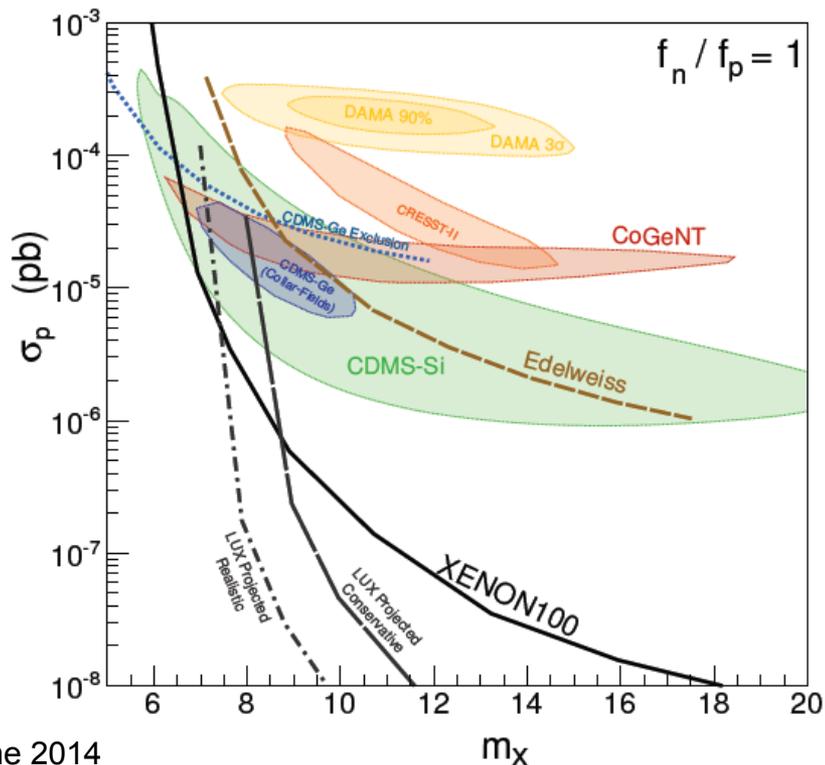
- Can decouple any given isotope by a suitable choice of  $f_n / f_p$ .
- Crucially important to account for isotope distributions



Feng, Kumar, Marfatia, Sanford (2013)

# IVDM IMPLICATIONS

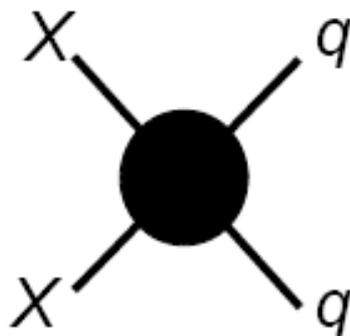
- LUX/XENON and DAMA are irreconcilable, but LUX/XENON and CDMS are consistent for  $f_n/f_p = -0.7$  (roughly  $f_u/f_d = -1$ )
- Compared to the usual isospin-conserving case  $f_n/f_p = 1$ , larger DM couplings to up and down quarks are allowed, and are even required to explain anomalies; strong implications for LHC



# INDIRECT DETECTION

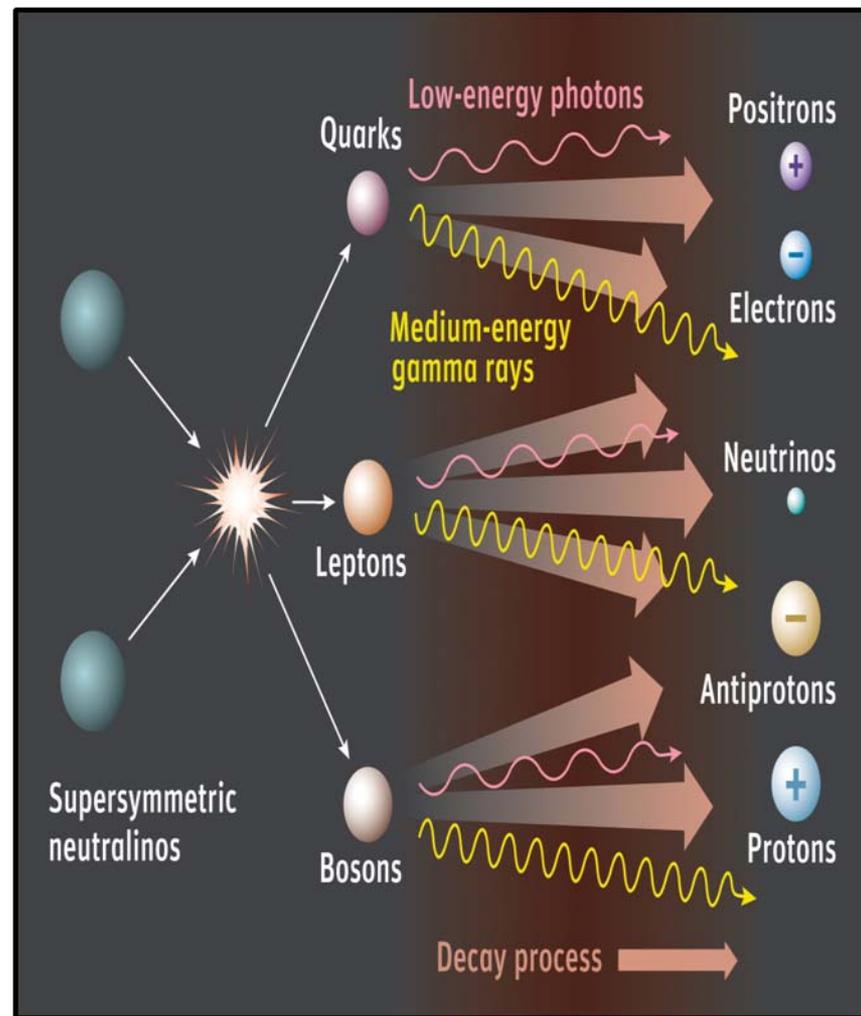
- Dark matter may pair annihilate in our galactic neighborhood to

- Photons
- Neutrinos
- Positrons
- Antiprotons
- Antideuterons



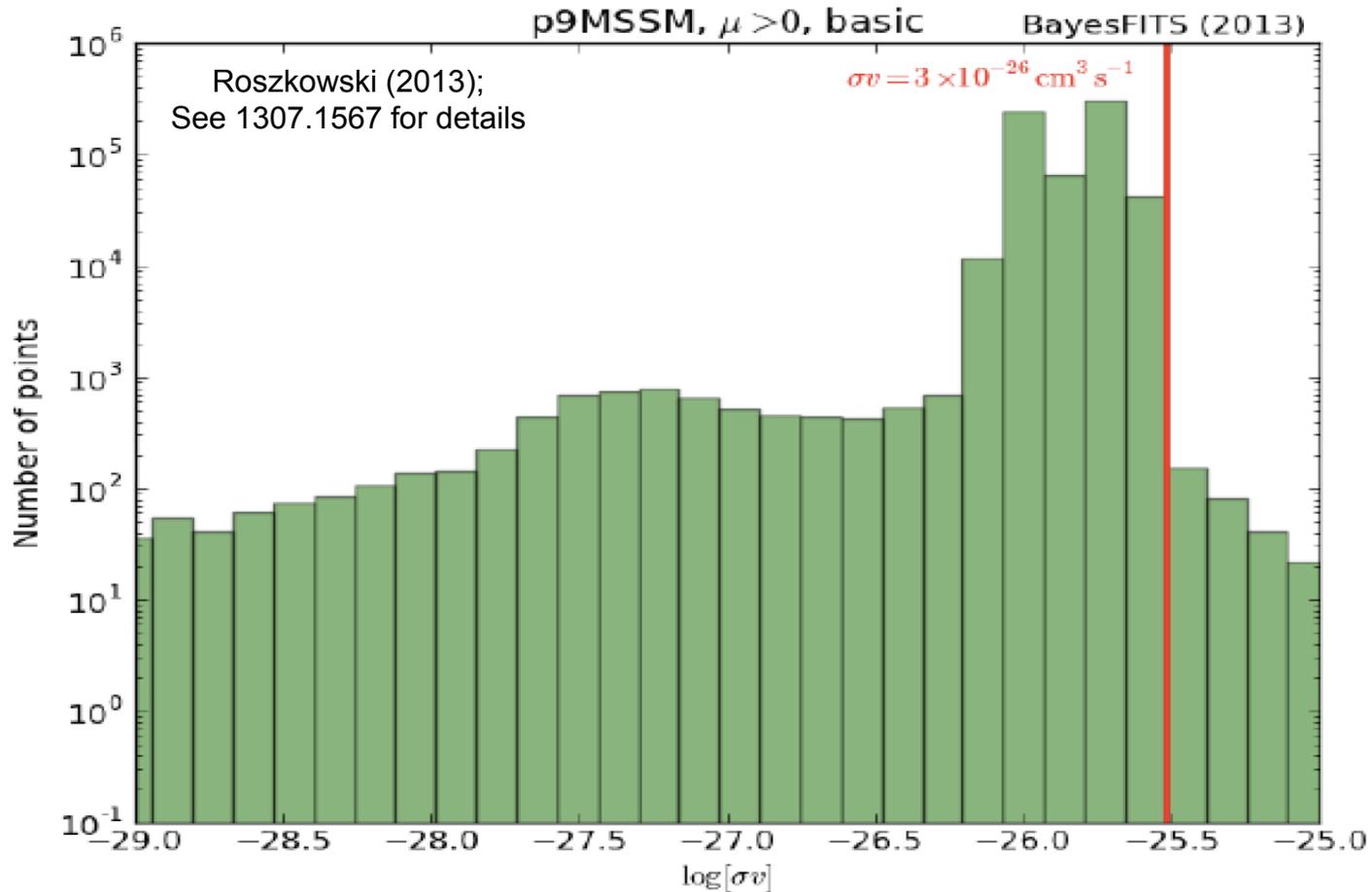
- The relic density provides a target annihilation cross section

$$\langle \sigma_A v \rangle \sim 3 \times 10^{-26} \text{ cm}^3/\text{s}$$



# ROBUSTNESS OF THE TARGET CROSS SECTION

Relative to direct, indirect rates typically have smaller particle physics uncertainties (but larger astrophysical uncertainties)



# INDIRECT DETECTION

## FILL IN THE BLANKS:

Dark matter annihilates in \_\_\_\_\_ to  
a place

\_\_\_\_\_, which are detected by \_\_\_\_\_ .  
particles an experiment

# PHOTONS

Dark Matter annihilates in the GC / dwarf galaxies to  
a place  
photons, which are detected by Fermi, VERITAS, ....  
some particles an experiment

The flux factorizes: 
$$\frac{d\Phi_\gamma}{d\Omega dE} = \sum_i \underbrace{\frac{dN_\gamma^i}{dE} \sigma_i v}_{\text{Particle Physics}} \underbrace{\frac{1}{4\pi m_\chi^2} \int_\psi \rho^2 dl}_{\text{Astro-Physics}}$$

## Particle physics: two kinds of signals

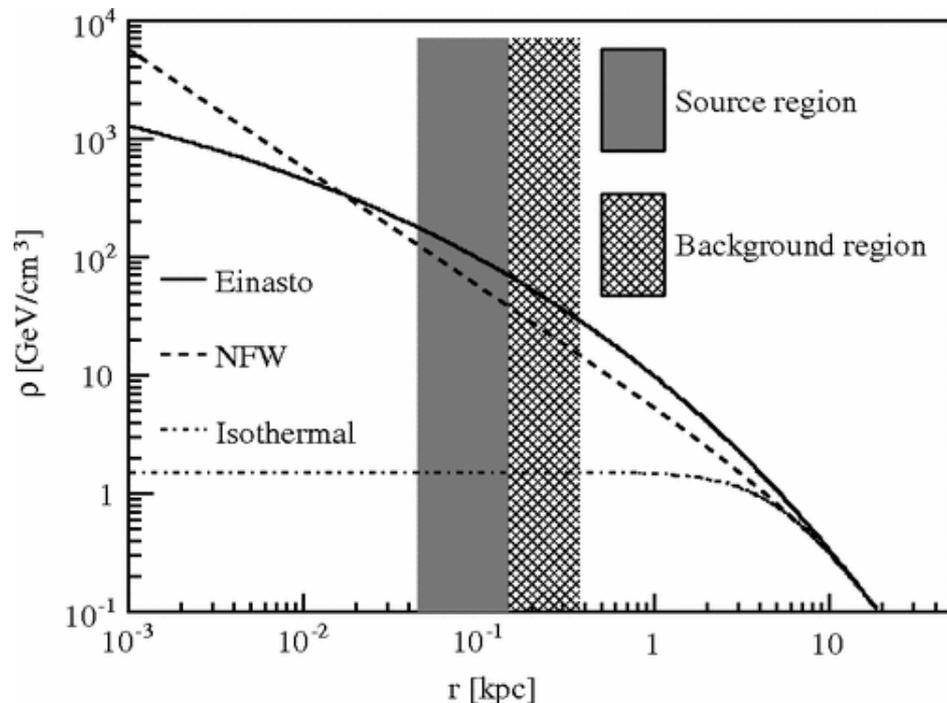
- Lines from  $XX \rightarrow \gamma\gamma, \gamma Z$ : loop-suppressed rates, but distinctive signal
- Continuum from  $XX \rightarrow ff \rightarrow \gamma$ : tree-level rates, but a broad signal

# HALO PROFILES

Astrophysics: two kinds of sources

- Galactic Center: close, large signal, but large backgrounds
- Dwarf Galaxies: farther and smaller, so smaller signal, but DM dominated, so smaller backgrounds

In both cases, halo profiles are not well-determined at the center, introduces an uncertainty in flux of up to  $\sim 100$



# PHOTONS: CURRENT EXPERIMENTS

Veritas, Fermi-LAT, HAWC, and others



# PHOTONS: FUTURE EXPERIMENTS

## Cerenkov Telescope Array

### Low-energy section:

4 x 23 m tel. (LST)  
(FOV: 4-5 degrees)  
energy threshold  
of some 10s of GeV

### Core-energy array:

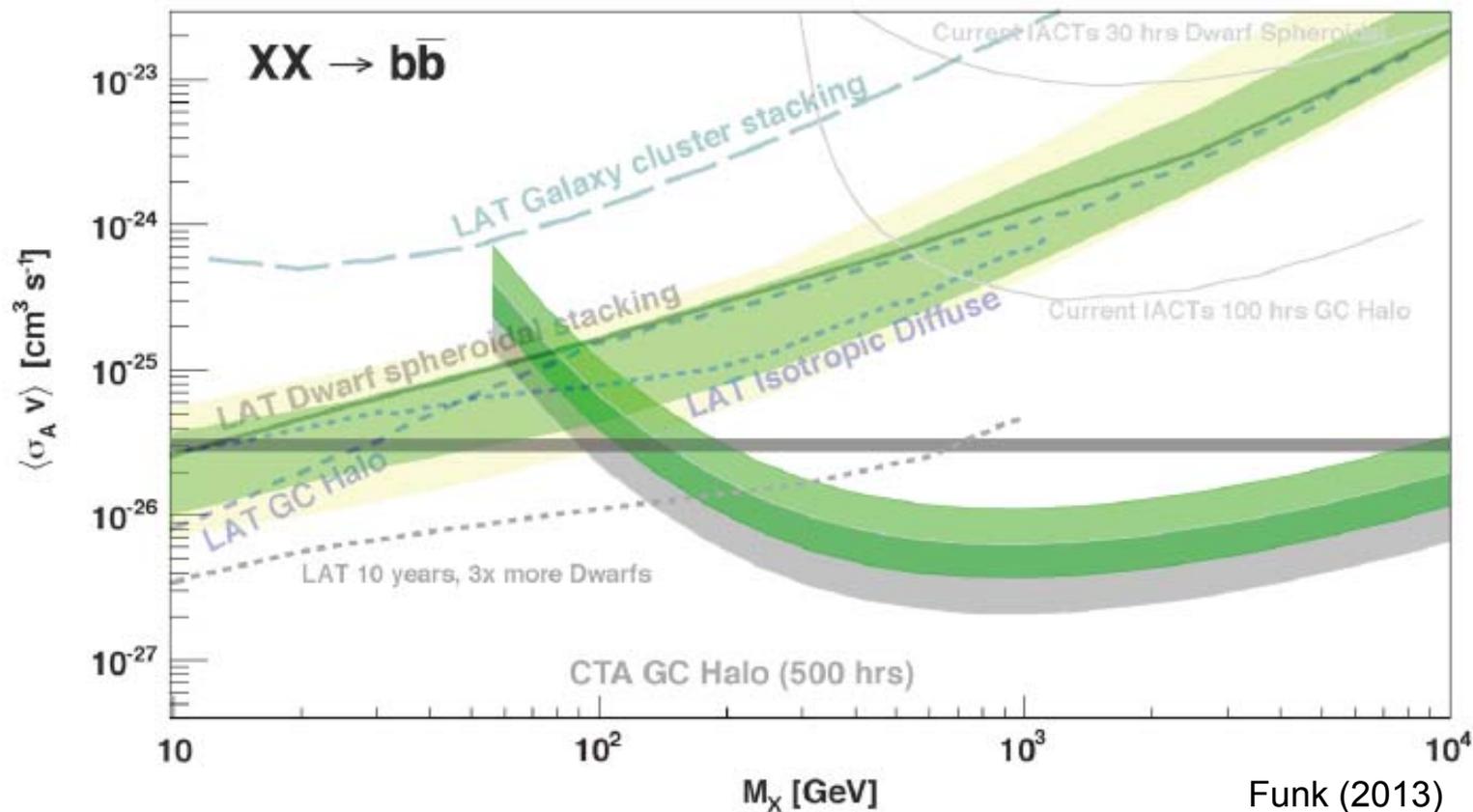
23 x 12 m tel. (MST)  
FOV: 7-8 degrees  
best sensitivity  
in the 100 GeV–10 TeV  
domain

### High-energy section:

30-70 x 4-6 m tel. (SST)  
FOV: ~10 degrees  
10 km<sup>2</sup> area at  
multi-TeV energies

First Science: ~2016  
Completion: ~2019

# PHOTONS: STATUS AND PROSPECTS

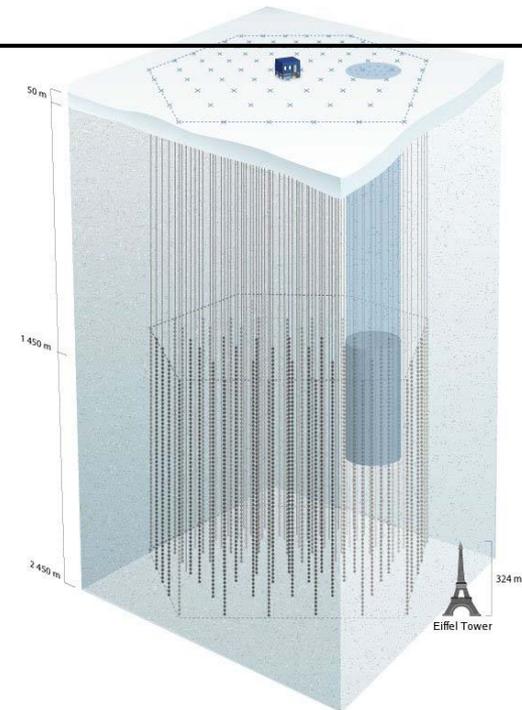
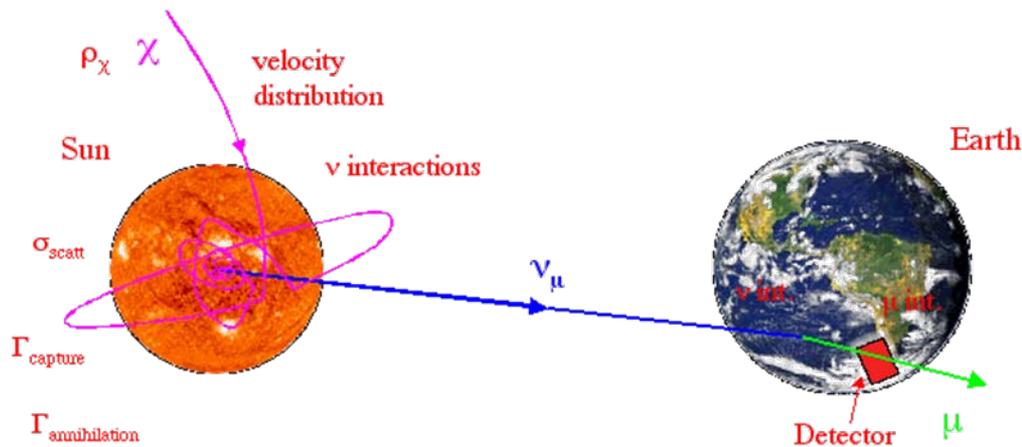


- Fermi-LAT has excluded a light WIMP with the target annihilation cross section for certain annihilation channels
- CTA extends the reach to WIMP masses  $\sim 10$  TeV

# INDIRECT DETECTION: NEUTRINOS

Dark Matter annihilates in the center of the Sun to  
a place

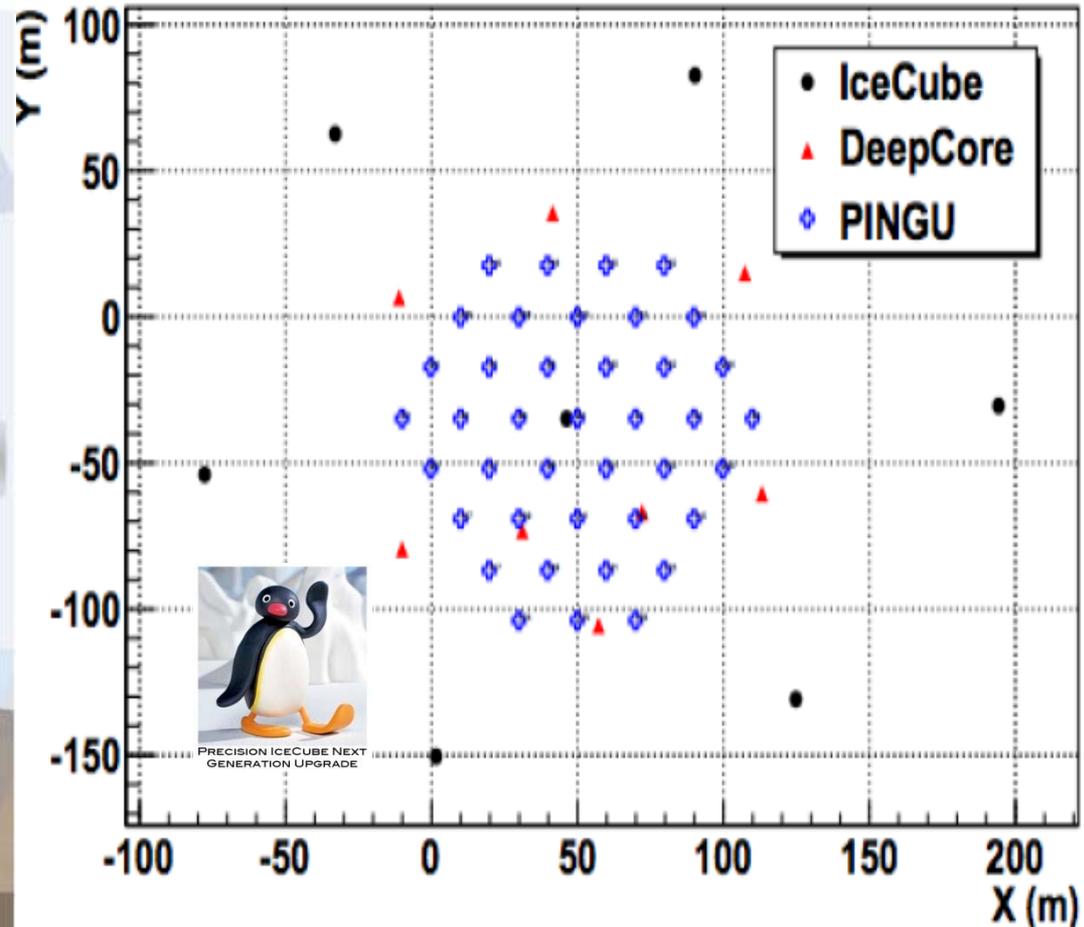
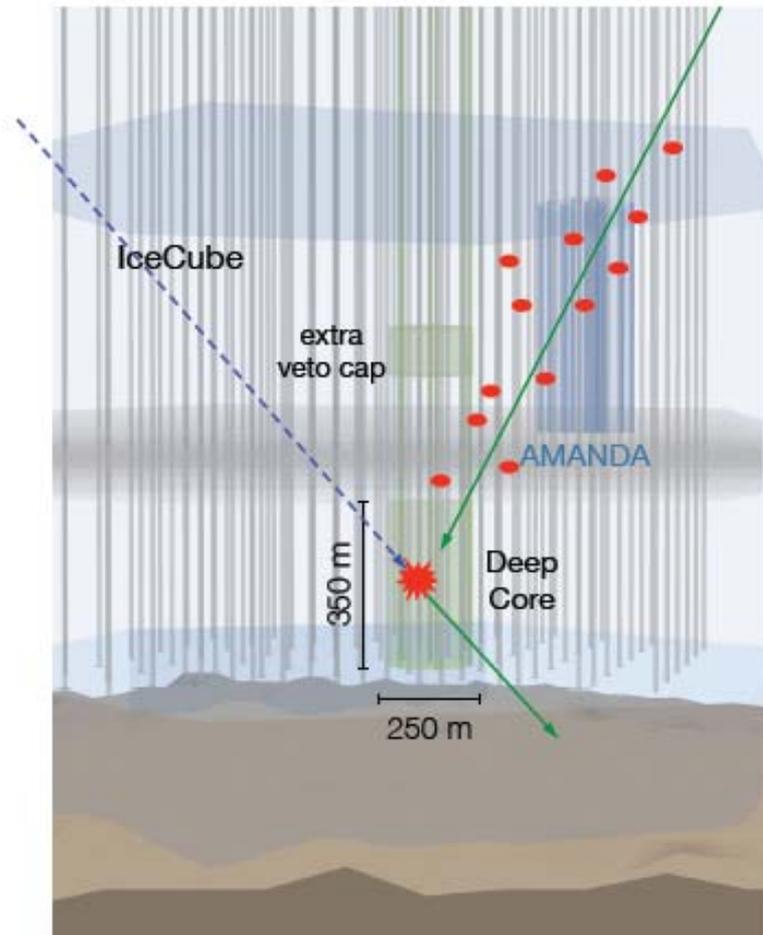
neutrinos, which are detected by ANTARES / PINGU.  
some particles an experiment



# NEUTRINOS: EXPERIMENTS

Current: IceCube/DeepCore,  
ANTARES

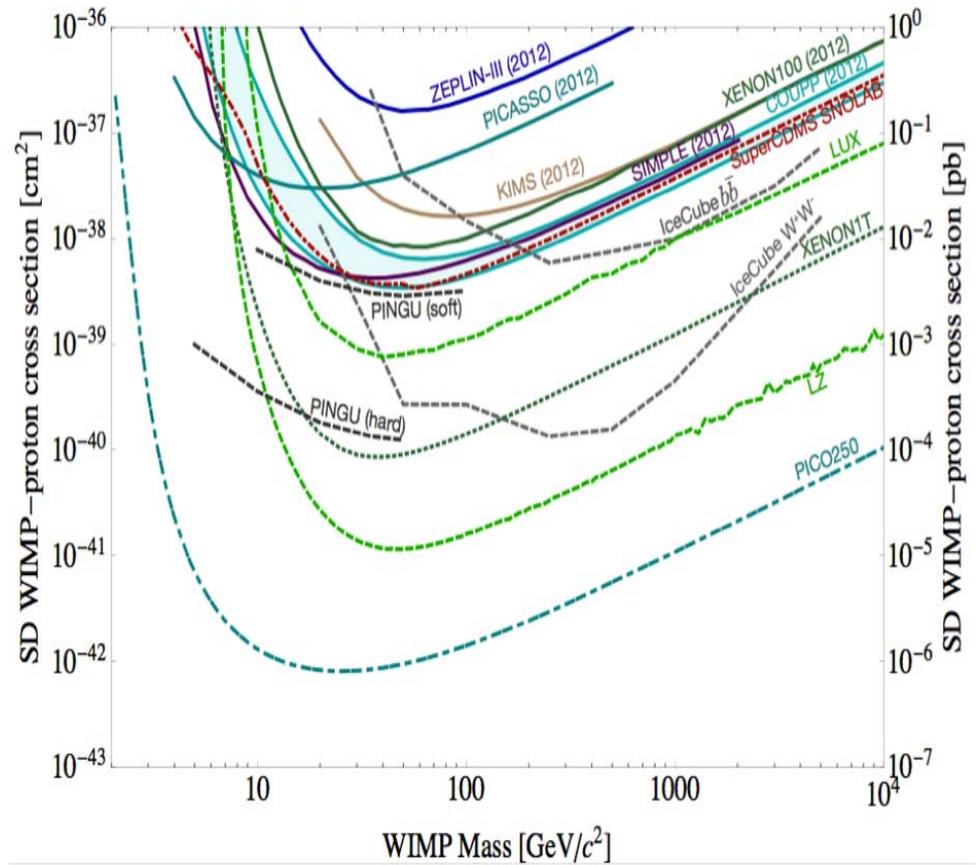
Future: PINGU



# NEUTRINOS: STATUS AND PROSPECTS

The Sun is typically in equilibrium

- Spin-dependent scattering off hydrogen  $\rightarrow$  capture rate  $\rightarrow$  annihilation rate
- Neutrino indirect detection results are typically plotted in the  $(m_\chi, \sigma_{SD})$  plane, compared with direct detection experiments



Future experiments like PINGU may discover the smoking-gun signal of HE neutrinos from the Sun, or set stringent  $\sigma_{SD}$  limits, extending the reach of IceCube/DeepCore

# INDIRECT DETECTION: ANTI-MATTER

Dark Matter annihilates in the halo to  
a place  
positrons, which are detected by Fermi/AMS/....  
some particles an experiment

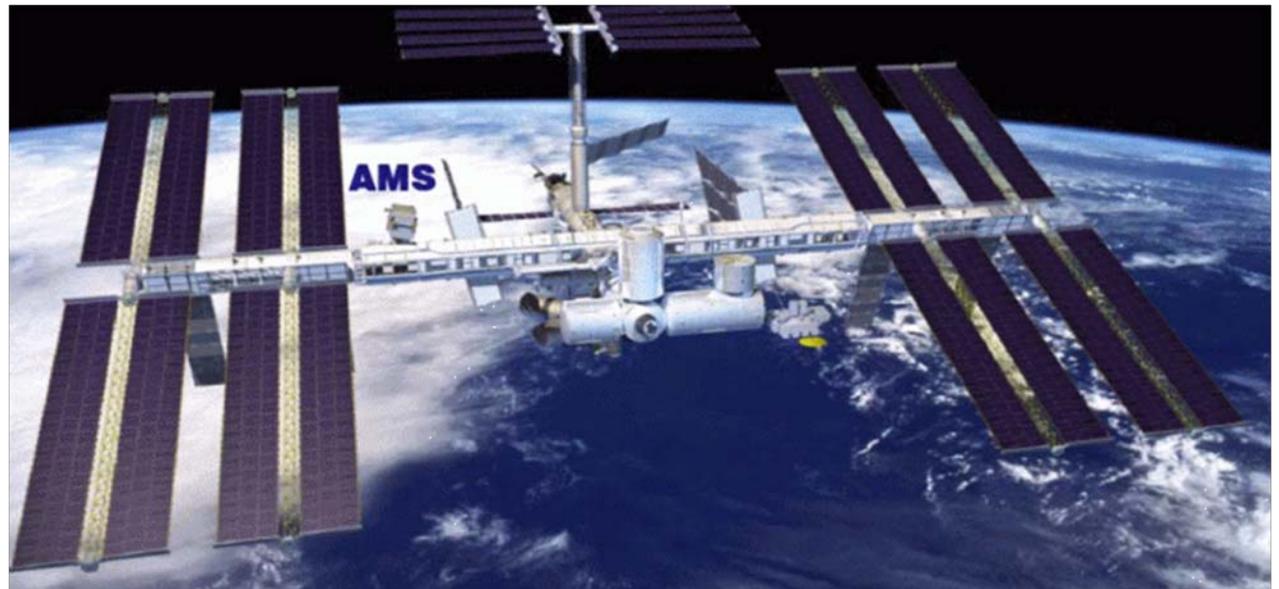
In contrast to photons and neutrinos, anti-matter does not travel in straight lines

- bumps around the local halo before arriving in our detectors
- for example, positrons, created with energy  $E_0$ , detected with energy  $E$

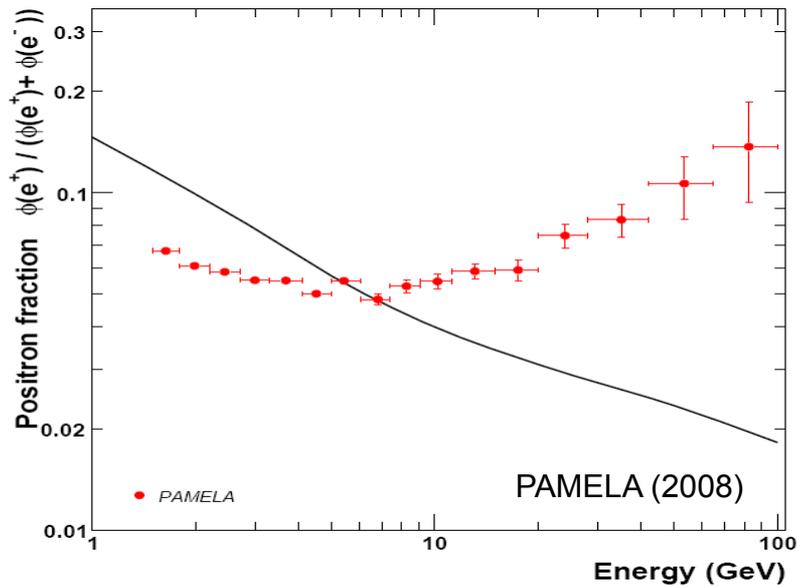
$$\frac{d\Phi_{e^+}}{d\Omega dE} = \frac{\rho_\chi^2}{m_\chi^2} \sum_i \sigma_i v B_{e^+}^i \int dE_0 f_i(E_0) G(E_0, E)$$

# ANTI-MATTER: EXPERIMENTS

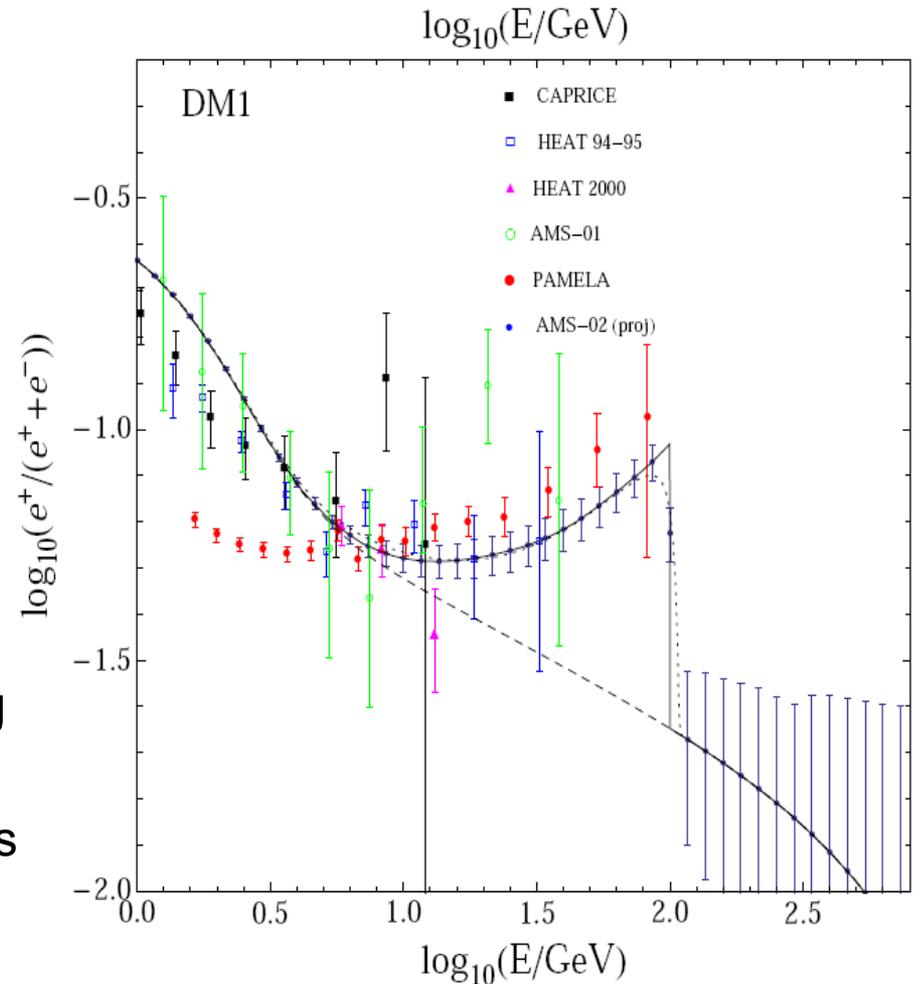
- Positrons (PAMELA, Fermi-LAT, AMS, CALET)
- Anti-Protons (PAMELA, AMS)
- Anti-Deuterons (GAPS)



# POSITRONS: STATUS AND PROSPECTS

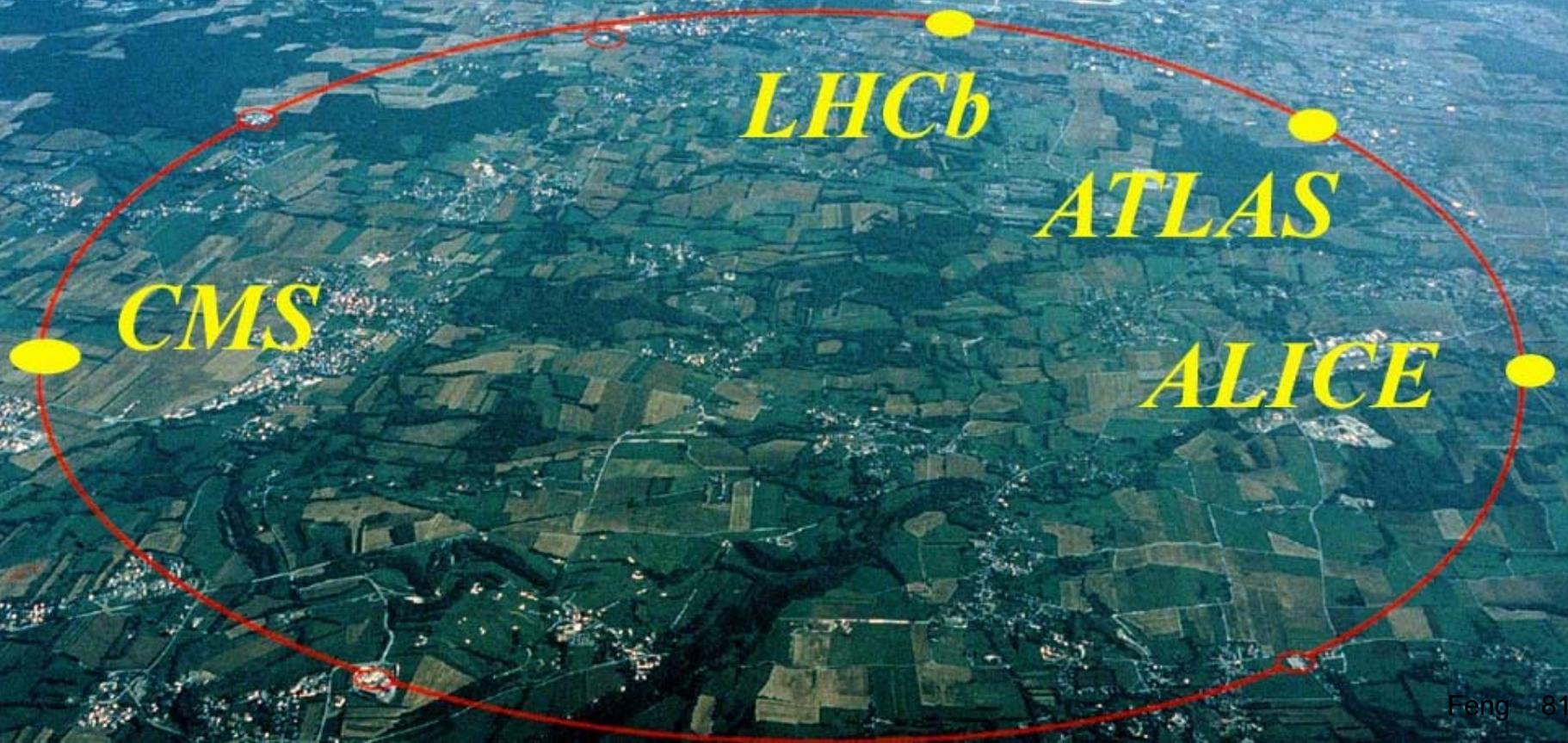


- Flux is a factor of 100-1000 too big for a thermal relic; requires
  - Enhancement from particle physics
  - Alternative production mechanism
- Difficult to distinguish from pulsars



Pato, Lattanzi, Bertone (2010)

# PARTICLE COLLIDERS

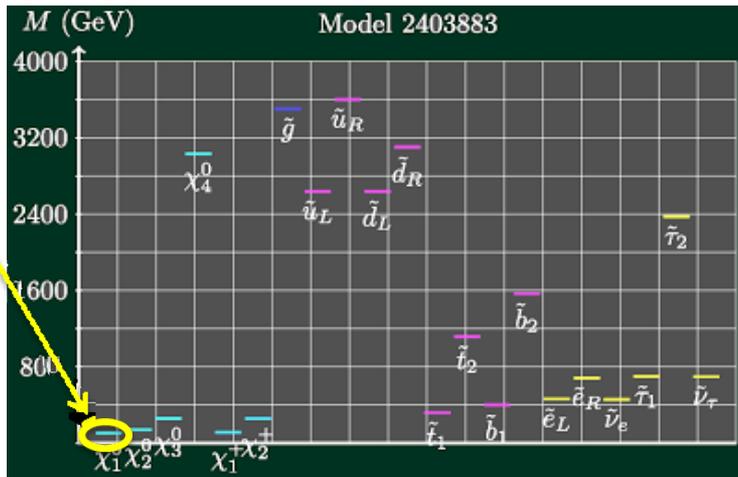




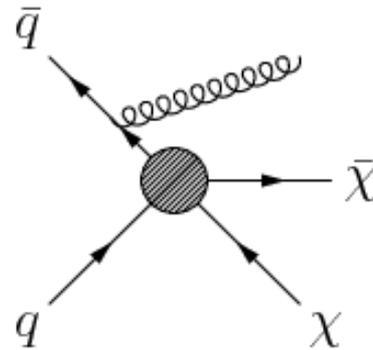
# DARK MATTER AT COLLIDERS

DM Effective Theories  
(Bare Bones Dark Matter)

Now systematically classify  
all possible 4-pt interactions



Produce DM directly,  
but in association with  
something else so it  
can be seen:  
Mono- $\gamma$ , jet, W, Z, h, b, t



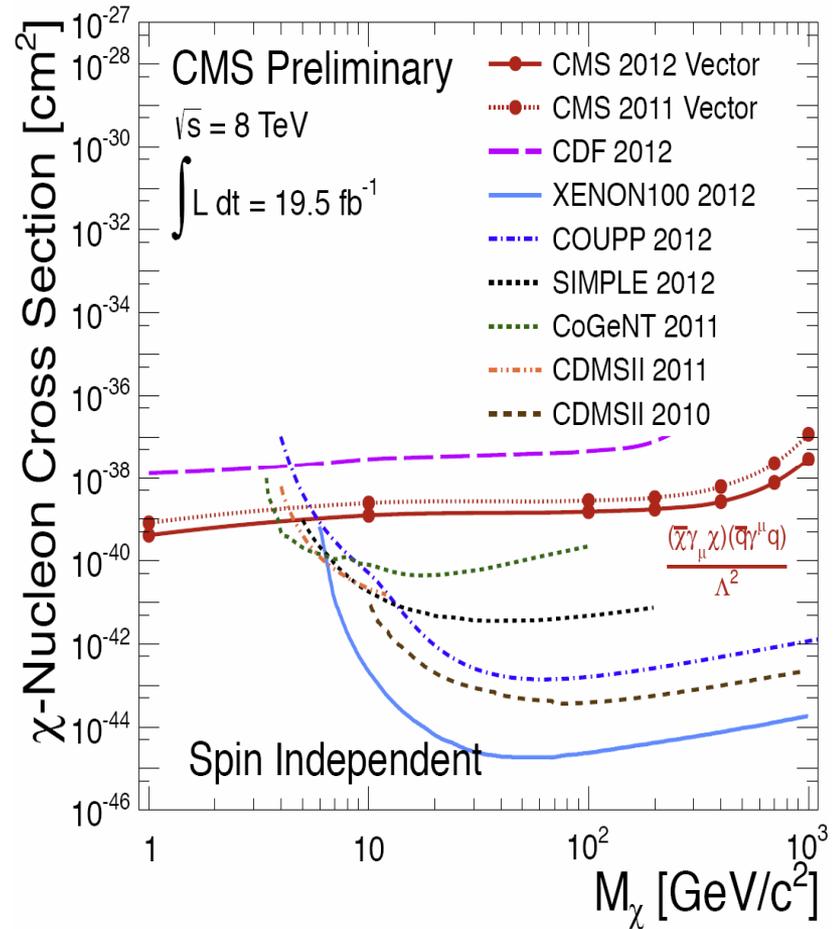
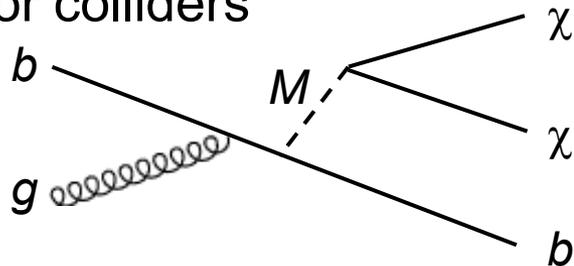
Birkedal, Matchev, Perelstein (2004)  
Feng, Su, Takayama (2005)

Name	Operator	Coefficient
D1	$\bar{\chi}\chi\bar{q}q$	$m_q/M_*^3$
D2	$\bar{\chi}\gamma^5\chi\bar{q}q$	$im_q/M_*^3$
D3	$\bar{\chi}\chi\bar{q}\gamma^5q$	$im_q/M_*^3$
D4	$\bar{\chi}\gamma^5\chi\bar{q}\gamma^5q$	$m_q/M_*^3$
D5	$\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu q$	$1/M_*^2$
D6	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu q$	$1/M_*^2$
D7	$\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu\gamma^5q$	$1/M_*^2$
D8	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu\gamma^5q$	$1/M_*^2$
D9	$\bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma_{\mu\nu}q$	$1/M_*^2$
D10	$\bar{\chi}\sigma_{\mu\nu}\gamma^5\chi\bar{q}\sigma_{\alpha\beta}q$	$i/M_*^2$
D11	$\bar{\chi}\chi G_{\mu\nu}G^{\mu\nu}$	$\alpha_s/4M_*^3$
D12	$\bar{\chi}\gamma^5\chi G_{\mu\nu}G^{\mu\nu}$	$i\alpha_s/4M_*^3$
D13	$\bar{\chi}\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$i\alpha_s/4M_*^3$
D14	$\bar{\chi}\gamma^5\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$\alpha_s/4M_*^3$

Goodman, Ibe, Rajaraman, Shepherd, Tait, Yu (2010)  
Bai, Fox, Harnik (2010)

# WIMP EFFECTIVE THEORY

- One operator can correspond to many channels. E.g.,  $bb\chi\chi$  leads to
  - $bb \rightarrow \chi\chi + X$ : monophoton, monojet channel
  - $bg \rightarrow b\chi\chi$ : mono- $b$  channel
  - $gg \rightarrow bb\chi\chi$ : sbottom pair channel
- WIMP effective theory allows comparison to indirect, direct search results; colliders do very well for some operators, low masses
- This assumes the mediators are heavy compared to the WIMPs and the energies involved, which is not always true for colliders

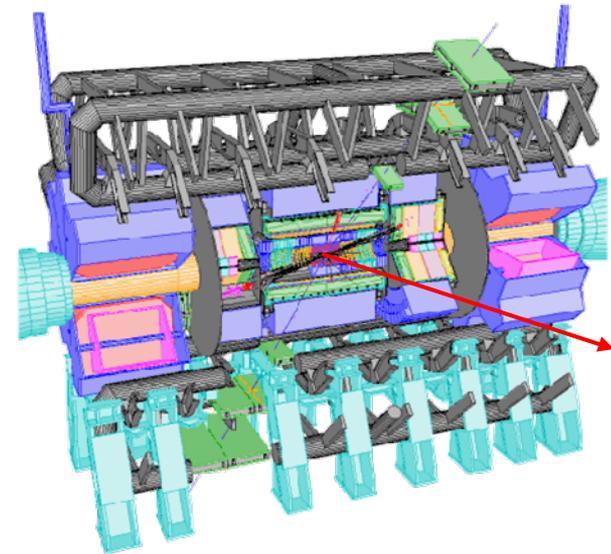
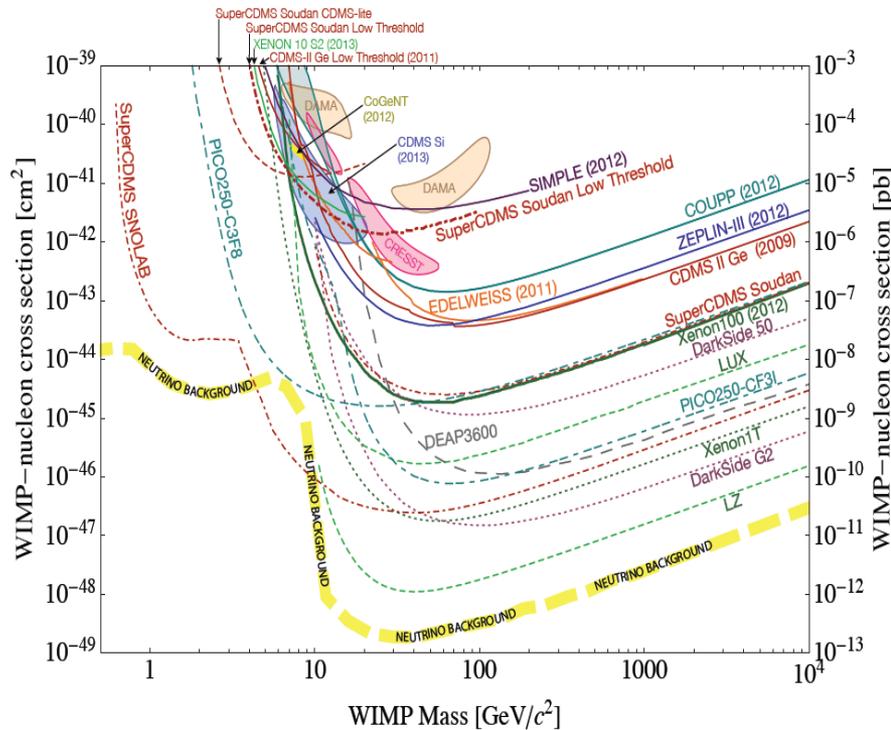


# THE FUTURE

If there is a signal, what do we learn?

- Cosmology and dark matter searches can't identify the particle nature

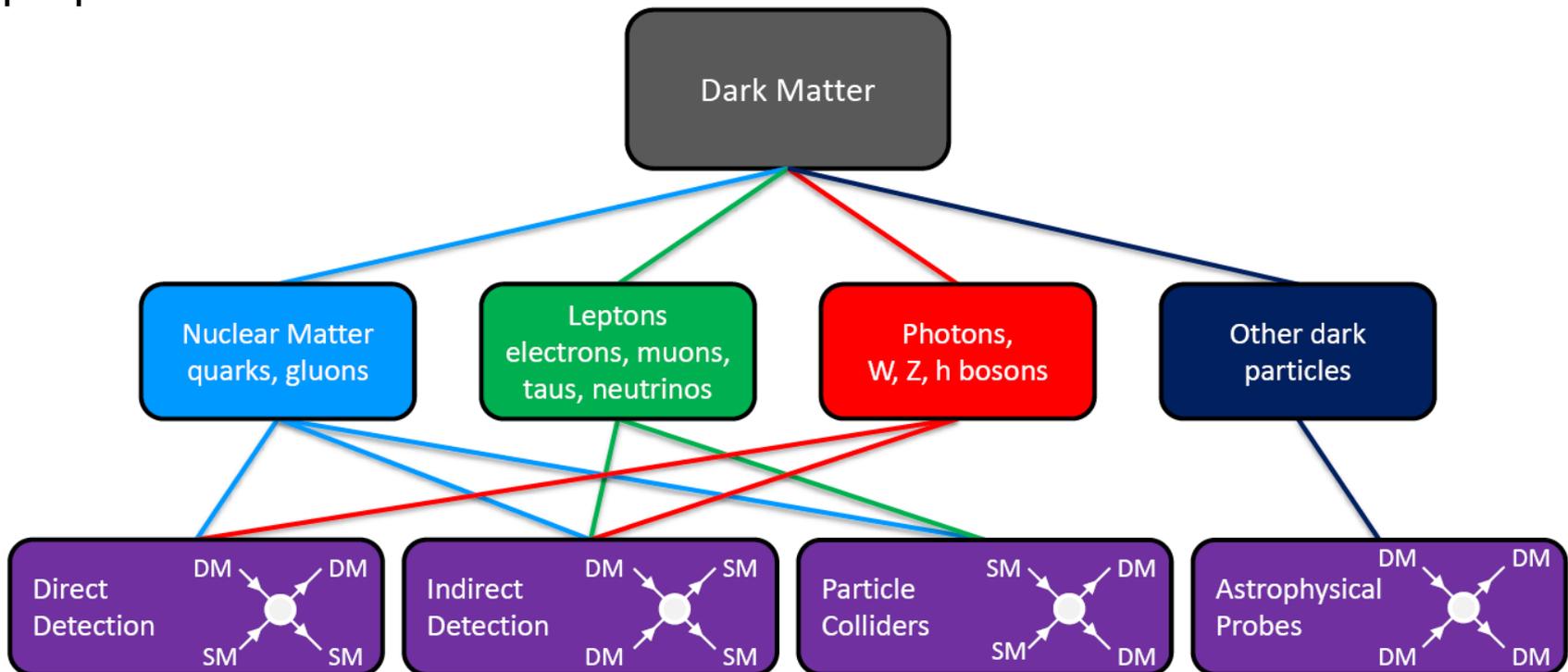
- Particle colliders can't prove it's dark matter



Lifetime  $> 10^{-7} \text{ s} \rightarrow 10^{17} \text{ s} ?$

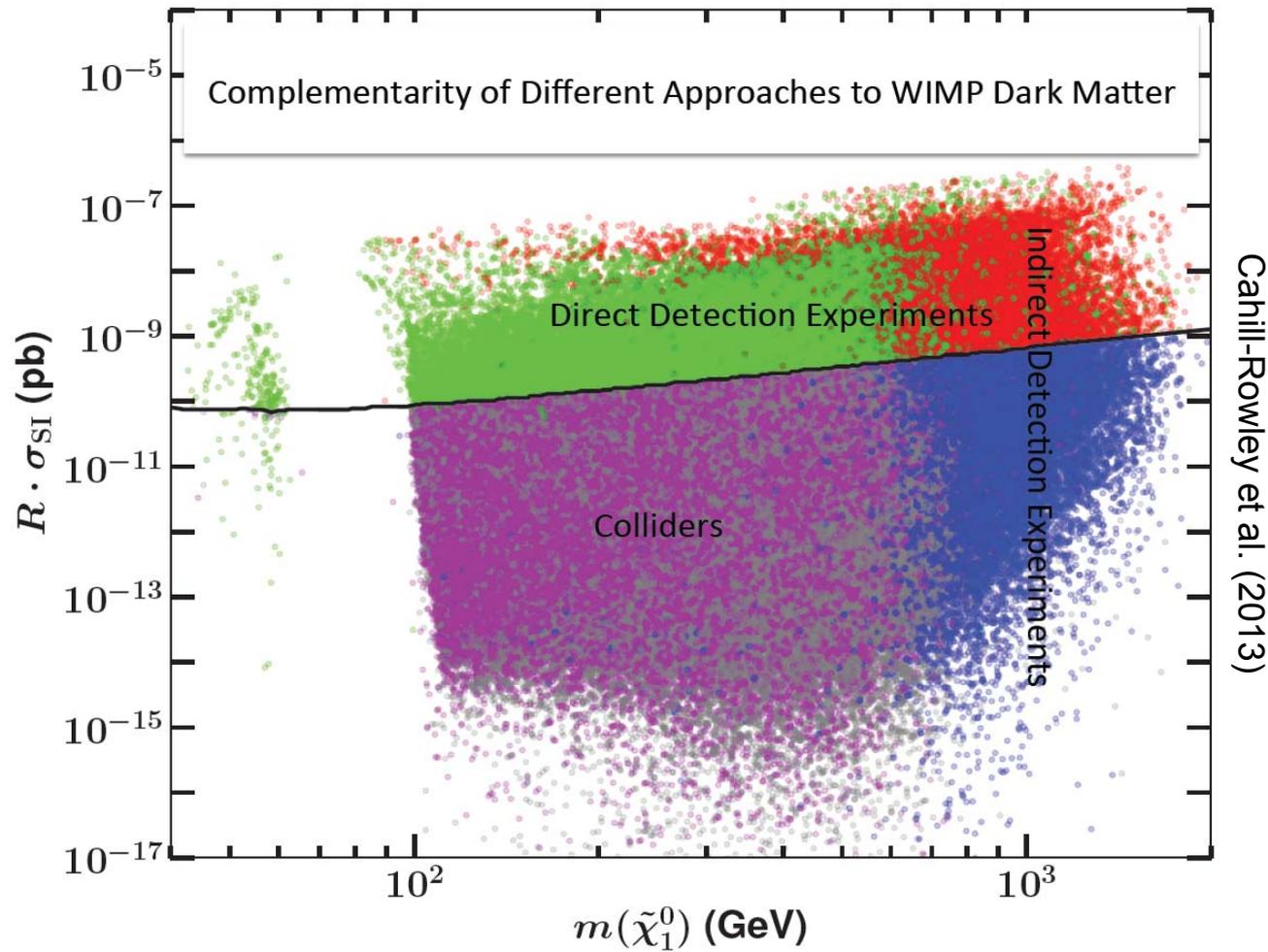
# DARK MATTER COMPLEMENTARITY

- Before a signal: Different experimental approaches are sensitive to different dark matter candidates with different characteristics, and provide us with different types of information – complementarity!
- After a signal: we are trying to identify a quarter of the Universe: need high standards to claim discovery and follow-up studies to measure properties



# COMPLEMENTARITY: FULL MODELS

pMSSM 19-parameter scan of SUSY parameter space



Different expts probe different models, provide cross-checks

# LECTURE 2 SUMMARY

- WIMPs are natural dark matter candidates in many models of BSM physics
- The relic density implies significant rates for direct detection, indirect detection, and colliders
- A time of rapid experimental advances on all fronts
- Definitive dark matter detection and understanding will require signals in several types of experiments

# OUTLINE

## LECTURE 1

Essential Cosmology: Contents and History of the Universe

## LECTURE 2

WIMP Dark Matter: Candidates and Methods of Detection

## LECTURE 3

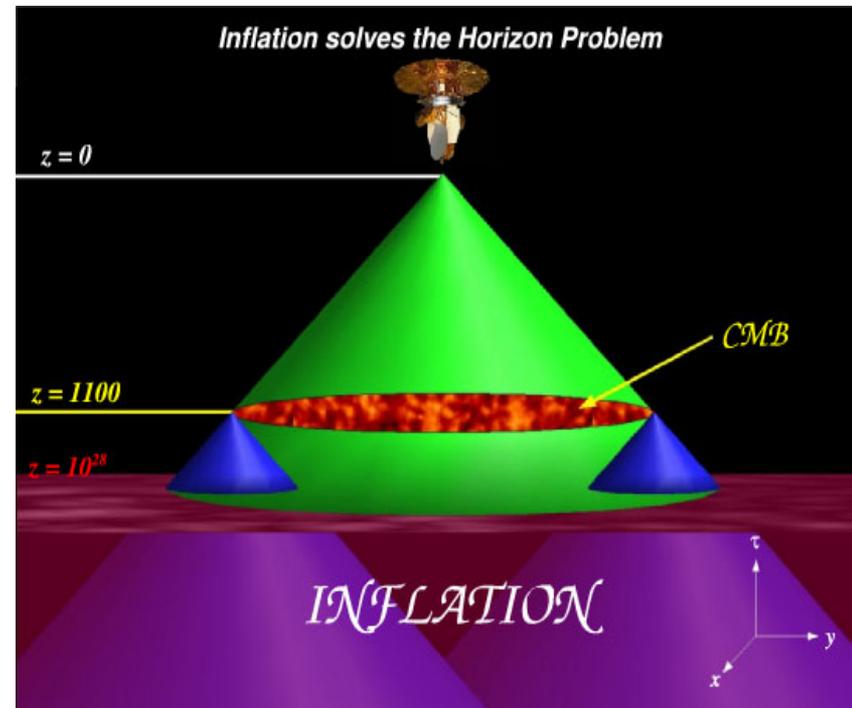
Inflation, Gravitinos, and Hidden Sectors

# INFLATION

- The standard model of cosmology includes not just the hot Big Bang we have described, but also an earlier period of inflation with vacuum-dominated expansion:

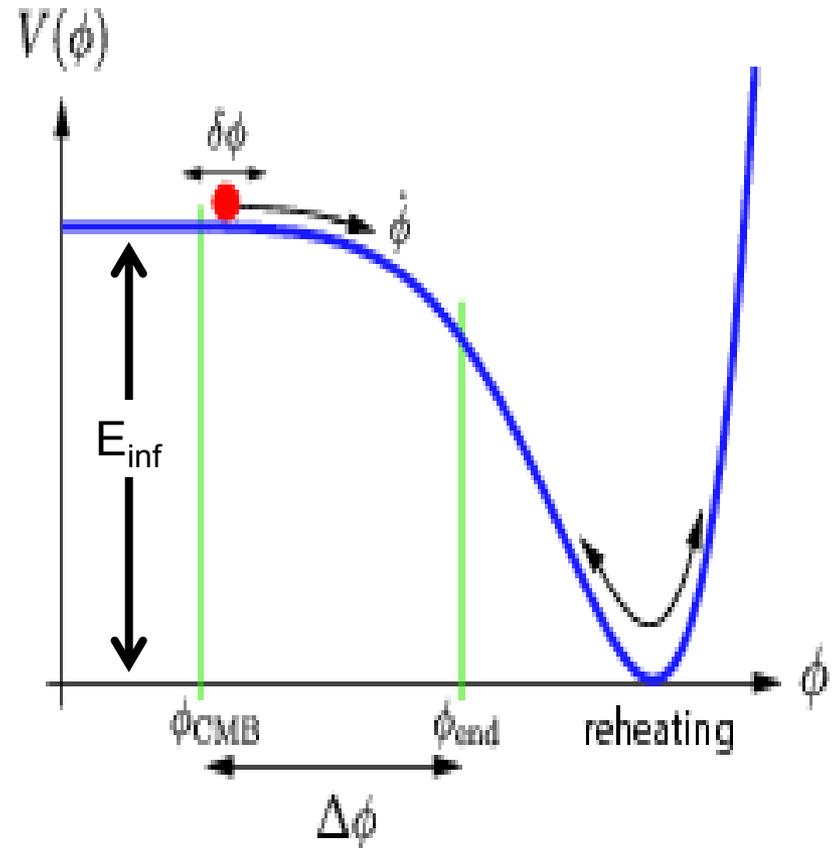
$$\text{VD} : \rho \propto a^0 \Rightarrow \dot{a}^2 \propto a^2 \Rightarrow a \propto e^{ct}$$

- Inflation has many motivations. One is the horizon problem: Why do causally-disconnected parts of the CMB have the same temperature?
- With inflation, these regions of the Universe had the same origin, are causally connected



# INFLATION

- There are many models of inflation, but the basic picture is simple:
- Initially, the inflaton stays at high potential energy  $E_{\text{inf}}$  and the Universe expands exponentially
- Eventually the scalar field rolls down, its potential energy is transferred to the SM particles
- The hot Big Bang begins with *reheat temperature*  $T_{\text{RH}} < E_{\text{inf}}$



# GRAVITINO DARK MATTER

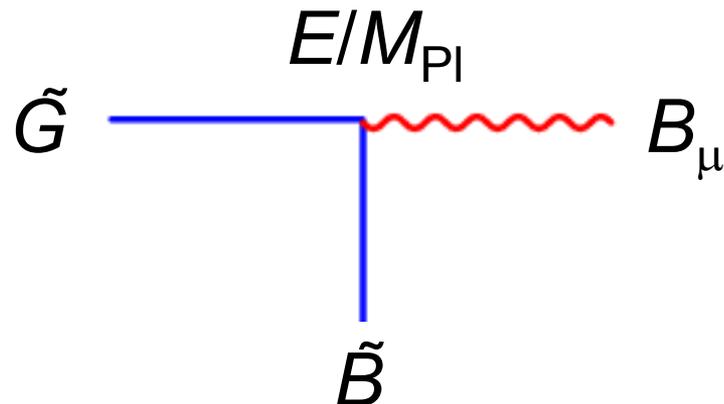
- WIMPs are not the only DM candidates; they are not even the only ones predicted by SUSY: gravitinos provide a nice case study of *very* weakly interacting dark matter
- SUSY: graviton  $G \rightarrow$  gravitino  $\tilde{G}$ , spin 3/2
- Mass  $m_{\tilde{G}} \sim F/M_{\text{Pl}}$ , where  $F^{1/2}$  is the scale of SUSY breaking
  - Ultra-light (GMSB):  $F \sim (100 \text{ TeV})^2$ ,  $m_{\tilde{G}} \sim \text{eV}$
  - Light (GMSB):  $F \sim (10^7 \text{ GeV})^2$ ,  $m_{\tilde{G}} \sim \text{keV}$
  - Heavy (SUGRA):  $F \sim (10^{11} \text{ GeV})^2$ ,  $m_{\tilde{G}} \sim \text{TeV}$
  - Obese (AMSB):  $F \sim (10^{12} \text{ GeV})^2$ ,  $m_{\tilde{G}} \sim 100 \text{ TeV}$
- The gravitino interaction strength  $\sim 1/F$
- A huge range of implications for cosmology and HEP

# HEAVY GRAVITINOS

- $m_{\tilde{G}} \sim F/M_{\text{Pl}} \sim \text{TeV}$ , same scale as the other superpartners

- $\tilde{G}$  interactions: 
$$-\frac{i}{8M_{\text{Pl}}}\tilde{G}_{\mu}[\gamma^{\nu},\gamma^{\rho}]\gamma^{\mu}\tilde{B}F_{\nu\rho}$$

Couplings grow with energy, but are typically extremely weak



# OPTION 1: GRAVITINOS FROM REHEATING

- Inflation dilutes all pre-existing particle densities. But at the end of inflation, the Universe reheats and can regenerate particles. Assume the reheat temperature is between the TeV and Planck scales.
- What happens? A question of rates:

$$\sigma_{\text{SM}n} \sim T \gg H \sim \frac{T^2}{M_{\text{Pl}}} \gg \sigma_{\tilde{G}n} \sim \frac{T^3}{M_{\text{Pl}}^2}$$

SM interaction rate  $\gg$  expansion rate  $\gg$   $\tilde{G}$  interaction rate

- Thermal bath of MSSM particles  $X$ : occasionally they interact to produce a gravitino:  $X X \rightarrow X \tilde{G}$

# GRAVITINO RELIC DENSITY

- The Boltzmann equation:

$$\frac{dn}{dt} = -3Hn - \langle \sigma v \rangle \left[ n^2 - n_{\text{eq}}^2 \right]$$

↑
↑
↑

Dilution from expansion
  $f \tilde{G} \rightarrow f \bar{f}$ 
 $f \bar{f} \rightarrow f \tilde{G}$

0

- Change variables:  
Entropy density  $s \sim T^3$

$$t \rightarrow T \quad n \rightarrow Y \equiv \frac{n}{s}$$

- New Boltzmann equation:

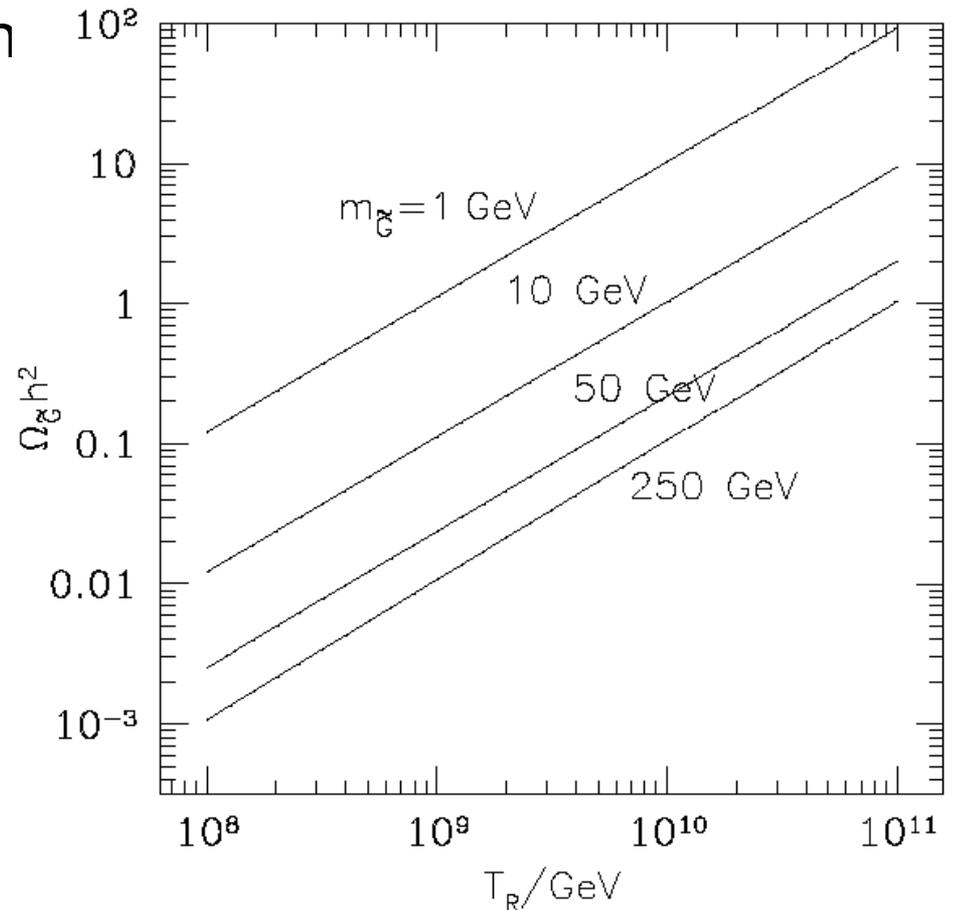
$$\frac{dY}{dT} = -\frac{\langle \sigma_{\tilde{G}v} \rangle}{HTs} n^2 \sim \langle \sigma_{\tilde{G}v} \rangle \frac{T^3 T^3}{T^2 T T^3}$$

- Simple:  $Y \sim$  reheat temperature  $T_{\text{RH}}$

# BOUNDS ON $T_{RH}$

- $\langle \sigma v \rangle$  for important production processes:

	process $i$	$ \mathcal{M}_i ^2 / M^2 \left(1 + \frac{m_{\tilde{G}}^2}{3m_{\tilde{G}}^2}\right)$
A	$g^a + g^b \rightarrow \tilde{g}^c + \tilde{G}$	$4(s + 2t + 2\frac{t^2}{s}) f^{abc} ^2$
B	$g^a + \tilde{g}^b \rightarrow g^c + \tilde{G}$	$-4(t + 2s + 2\frac{s^2}{t}) f^{abc} ^2$
C	$\tilde{q}_i + g^a \rightarrow q_j + \tilde{G}$	$2s T_{ji}^a ^2$
D	$g^a + q_i \rightarrow \tilde{q}_j + \tilde{G}$	$-2t T_{ji}^a ^2$
E	$\tilde{q}_i + q_j \rightarrow g^a + \tilde{G}$	$-2t T_{ji}^a ^2$
F	$\tilde{g}^a + \tilde{g}^b \rightarrow \tilde{g}^c + \tilde{G}$	$-8\frac{(s^2+st+t^2)^2}{st(s+t)} f^{abc} ^2$
G	$q_i + \tilde{g}^a \rightarrow q_j + \tilde{G}$	$-4(s + \frac{s^2}{t}) T_{ji}^a ^2$
H	$\tilde{q}_i + \tilde{g}^a \rightarrow \tilde{q}_j + \tilde{G}$	$-2(t + 2s + 2\frac{s^2}{t}) T_{ji}^a ^2$
I	$q_i + \tilde{q}_j \rightarrow \tilde{g}^a + \tilde{G}$	$-4(t + \frac{t^2}{s}) T_{ji}^a ^2$
J	$\tilde{q}_i + \tilde{q}_j \rightarrow \tilde{g}^a + \tilde{G}$	$2(s + 2t + 2\frac{t^2}{s}) T_{ji}^a ^2$



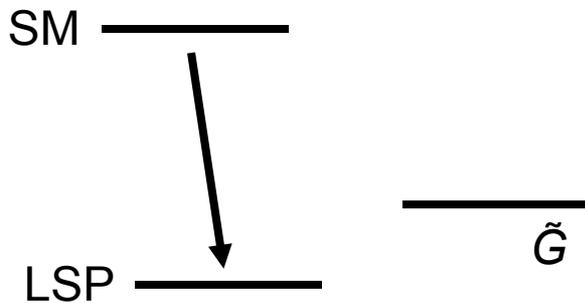
Bolz, Brandenburg, Buchmuller (2001)

- $T_{RH} < 10^8 - 10^{10}$  GeV;  
constrains inflation
- $\tilde{G}$  may be all of DM if bound saturated

# OPTION 2: GRAVITINOS FROM LATE DECAYS

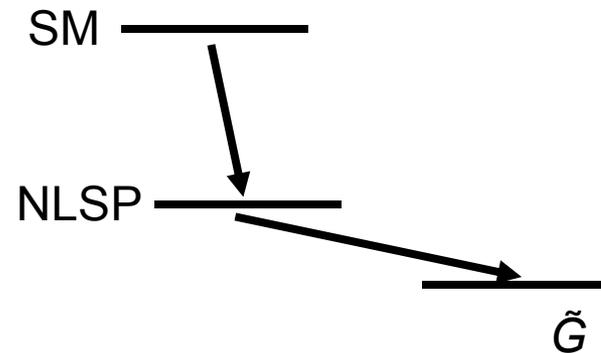
- What if gravitinos are diluted by inflation, and the universe reheats to low temperature? No “primordial” relic density

- $\tilde{G}$  not LSP



- No impact – implicit assumption of most of the literature

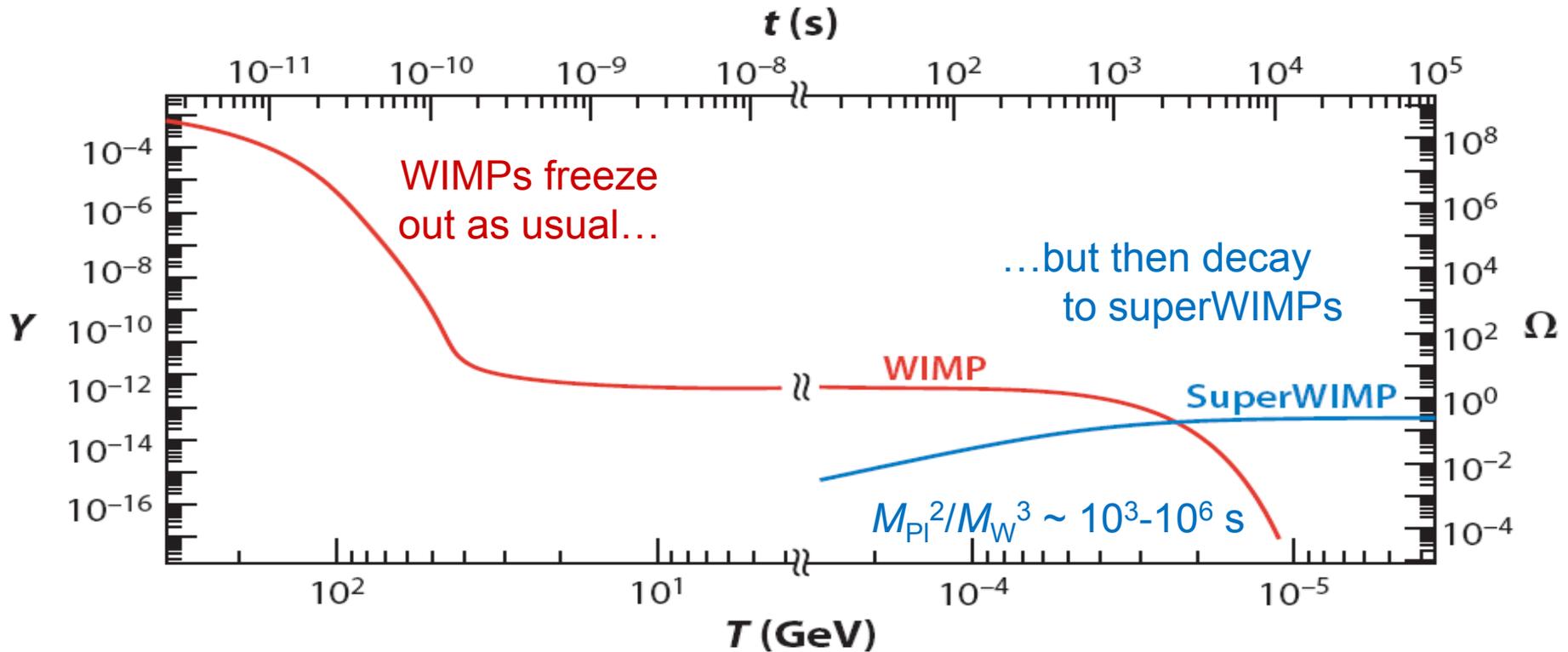
- $\tilde{G}$  LSP



- Completely different particle physics and cosmology

# FREEZE OUT WITH SUPERWIMPS

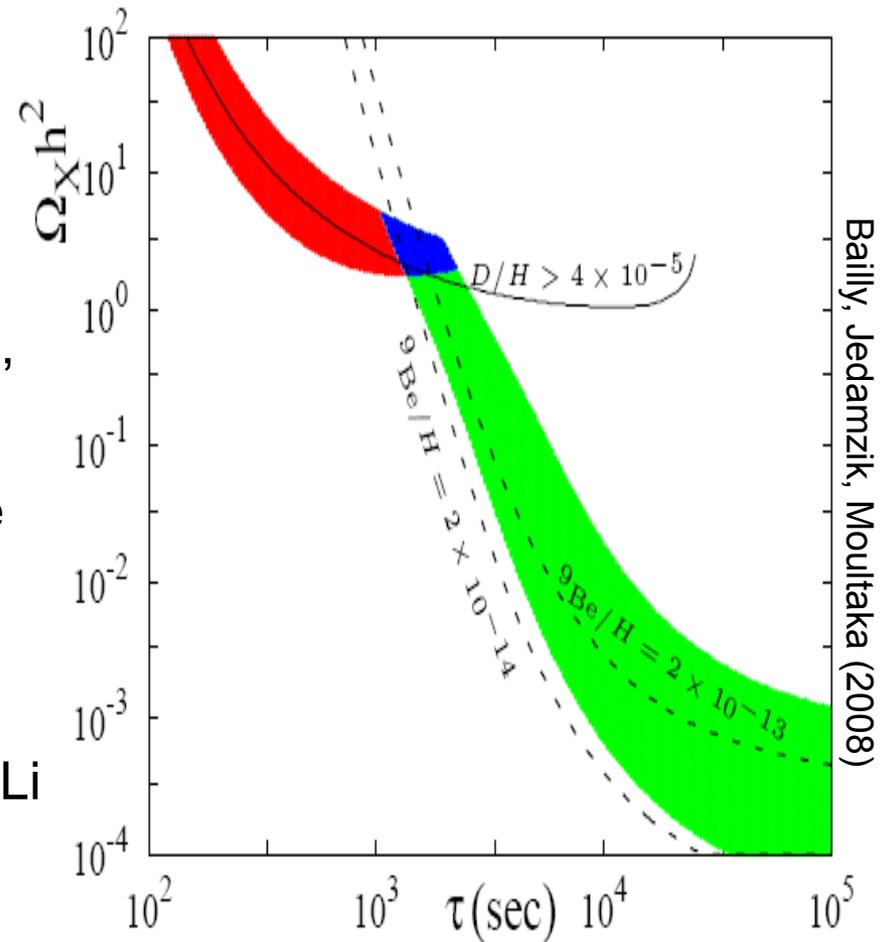
Feng, Rajaraman, Takayama (2003)



SuperWIMPs naturally inherit the right density (WIMP miracle), share all the motivations of WIMPs, but are superweakly interacting

# LATE DECAYS AND BBN

- Late decays deposit energy into the Universe, potentially destroy the light elements
- Simple way around this is to make decays before  $T \sim \text{MeV}$ ,  $t \sim 1\text{s}$
- More ambitious: as we saw previously,  ${}^7\text{Li}$  does not agree with standard BBN prediction
  - Too low by factor of 3,  $\sim 5\sigma$  at face value
  - May be solved by convection in stars, but then why so uniform?
- Also the standard BBN prediction for  ${}^6\text{Li}$  may be too low
- Decays after 1 s can possibly fix both



# COSMIC MICROWAVE BACKGROUND

- Late decays may also distort the black body CMB spectrum

- For  $10^5 \text{ s} < \tau < 10^7 \text{ s}$ , get “ $\mu$  distortions”:

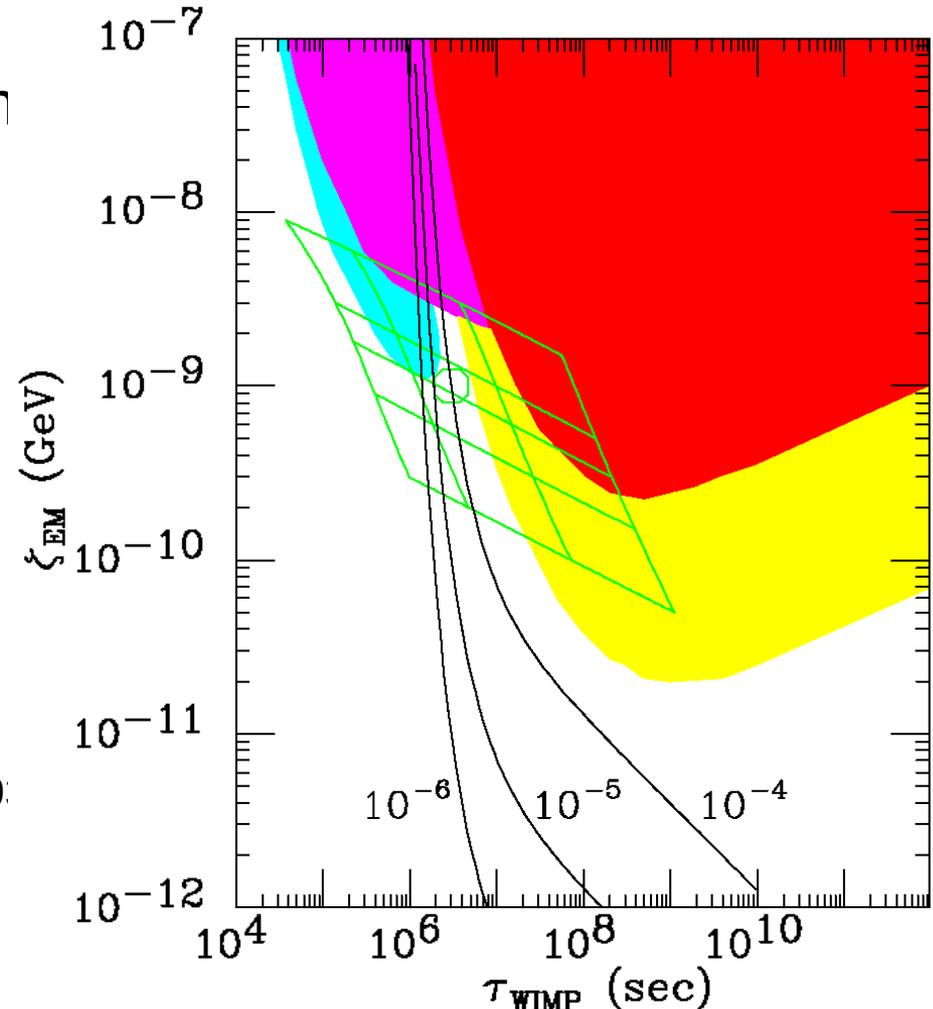
$$\frac{1}{e^{E/(kT)+\mu} - 1}$$

$\mu=0$ : Planckian spectrum

$\mu \neq 0$ : Bose-Einstein spectrum

Hu, Silk (199)

- Current bound:  $|\mu| < 9 \times 10^{-5}$   
Future: possibly  $|\mu| \sim 5 \times 10^{-8}$



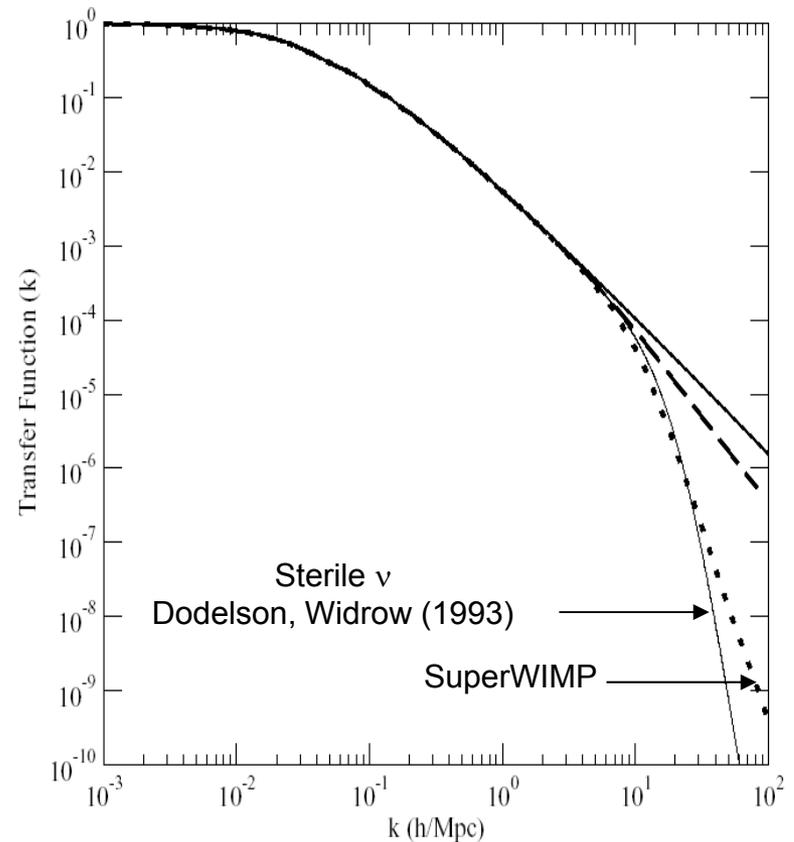
Feng, Rajaraman, Takayama (2003)

# WARM DARK MATTER

- SuperWIMPs are produced in late decays with large velocity ( $0.1c - c$ )
- This motion prevents them from forming potential wells, suppresses small scale structure
- Hot DM, like active neutrinos, is excluded, but SuperWIMPs could be warm. This is quantified by the free-streaming scale

$$\lambda_{\text{FS}} = \int_{\tau_X}^{t_{\text{EQ}}} \frac{v(t) dt}{a(t)}$$

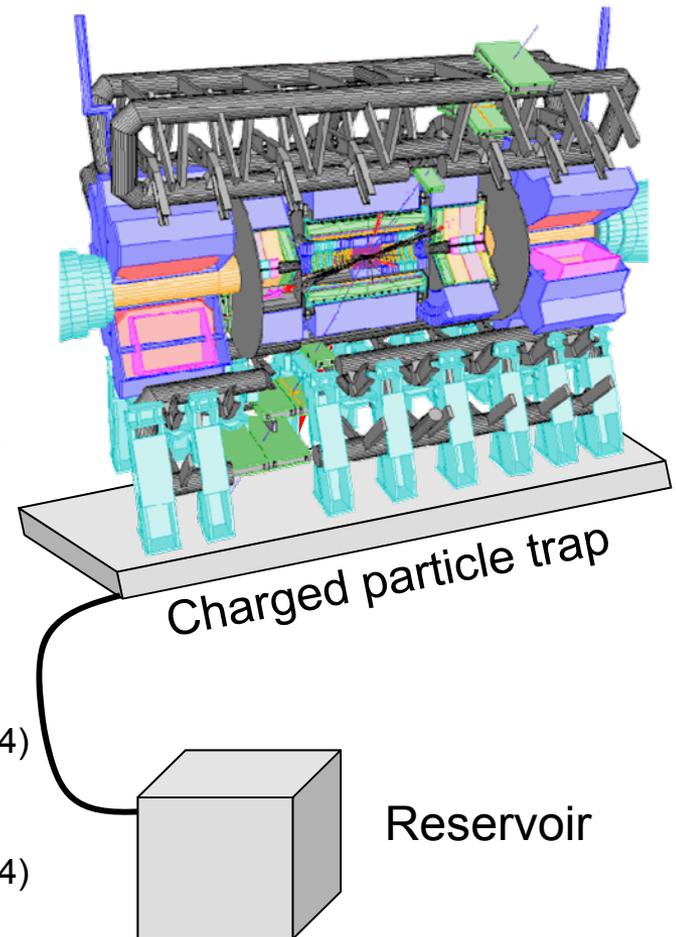
- Warm DM with cold DM pedigree



Kaplinghat (2005)

# IMPLICATIONS FOR THE LHC

- SuperWIMP DM  $\rightarrow$  metastable particles, may be charged
- Signature of new physics is “stable”, charged, massive particles, not missing  $E_T$
- If stable on timescales of s to months, can collect these particles and study their decays. Several ideas
  - Catch sleptons in a 1m thick water tank  
Feng, Smith (2004)
  - Catch sleptons in LHC detectors  
Hamaguchi, Kuno, Nakawa, Nojiri (2004)
  - Dig sleptons out of detector hall walls  
De Roeck et al. (2005)



# WHAT WE COULD LEARN FROM CHARGED PARTICLE DECAYS

$$\tau(\tilde{l} \rightarrow l\tilde{G}) = \frac{6}{G_N} \frac{m_{\tilde{G}}^2}{m_{\tilde{l}}^5} \left[ 1 - \frac{m_{\tilde{G}}^2}{m_{\tilde{l}}^2} \right]^{-4}$$

- Measurement of  $\tau$ ,  $m_{\tilde{l}}$  and  $E_l \rightarrow m_{\tilde{G}}$  and  $G_N$ 
  - Probes gravity in a particle physics experiment
  - Measurement of  $G_N$  on fundamental particle scale
  - Precise test of supergravity: gravitino is graviton partner
  - Determines  $\Omega_{\tilde{G}}$ : SuperWIMP contribution to dark matter
  - Determines  $F$ : supersymmetry breaking scale, contribution of SUSY breaking to dark energy, cosmological constant

# LIGHT GRAVITINO DM

- The original SUSY DM scenario
  - Universe cools from high temperature
  - Gravitinos decouple while relativistic,  $\Omega_{\tilde{G}} h^2 \approx m_{\tilde{G}} / 800 \text{ eV}$
  - Favored mass range: keV gravitinos

Pagels, Primack (1982)

- This minimal scenario is now excluded
  - $\Omega_{\tilde{G}} h^2 < 0.1 \rightarrow m_{\tilde{G}} < 80 \text{ eV}$
  - Gravitinos not too hot  $\rightarrow m_{\tilde{G}} > \text{few keV}$
  - keV gravitinos are now the most disfavored

Viel, Lesgourgues, Haehnelt, Matarrese, Riotto (2005)  
Seljak, Makarov, McDonald, Trac (2006)

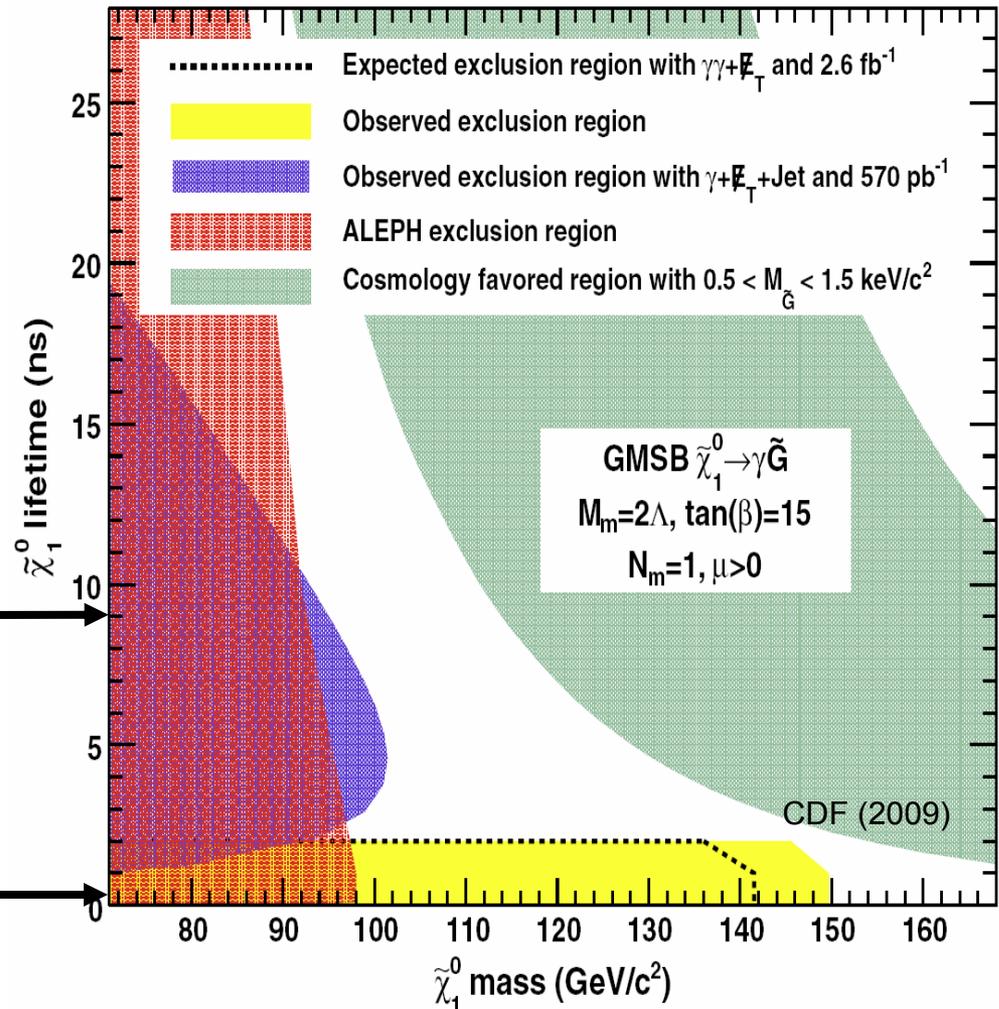
- Two ways out
  - $\Lambda$ WDM:  $m_{\tilde{G}} > \text{few keV}$ . Gravitinos are all the DM, but thermal density is diluted, e.g., by low reheating temperature
  - $\Lambda$ WCDM:  $m_{\tilde{G}} < 16 \text{ eV}$ . Gravitinos are only part of the DM, mixed warm-cold scenario

# CURRENT BOUNDS

- Remarkably, this lifetime difference is observable at colliders!

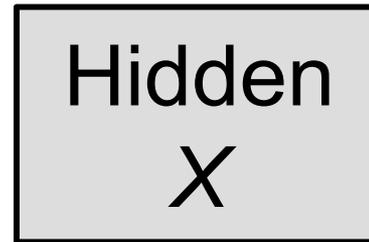
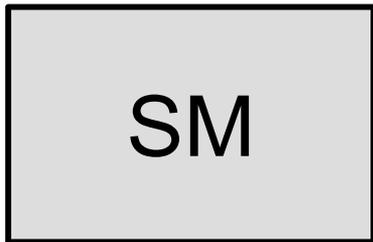
$$c\tau_{\text{NLSP}} \approx 50 \text{ cm} \left( \frac{200 \text{ GeV}}{m_{\text{NLSP}}} \right)^5 \left( \frac{m_{\tilde{G}}}{\text{keV}} \right)^2$$

- $m_{\tilde{G}} > \text{few keV}$ :  
Delayed photon signatures
- $m_{\tilde{G}} < 16 \text{ eV}$ :  
Prompt photon signatures



# HIDDEN SECTORS

- All current evidence for DM is gravitational. Perhaps DM is in a hidden sector, composed of particles with no SM strong, weak, or electromagnetic interactions



- *A priori* there are both pros and cons
  - Lots of freedom: can have interesting new phenomena
  - Too much freedom: no connections to the problems of particle physics we would like to solve, WIMP miracle, ...

# HIDDEN SECTOR INTERACTIONS

- There are many ways the hidden particles could couple to us. How should we think about this?
- Use effective operators as an organizing principle:

$$\mathcal{L} = \mathcal{O}_4 + \frac{1}{M}\mathcal{O}_5 + \frac{1}{M^2}\mathcal{O}_6 + \dots$$

where the operators are grouped by their mass dimension, with  $[\text{scalar}] = 1$ ,  $[\text{fermion}] = 3/2$ ,  $[F_{\mu\nu}] = 2$

- $M$  is a (presumably) large “mediator mass,” so we expect high-dimension operators to be suppressed. There are not too many possibilities at dimension 4.

# HIGGS PORTAL

Patt, Wilczek (2006)

- One possibility is

$$h^\dagger h \phi_h^\dagger \phi_h$$

where the  $h$  subscript denotes “hidden”

- When EW symmetry is broken,  $h \rightarrow \nu + h$ , this leads to invisible Higgs decays
- A leading motivation for precision Higgs studies and future colliders, such as ILC, CLIC, FCC

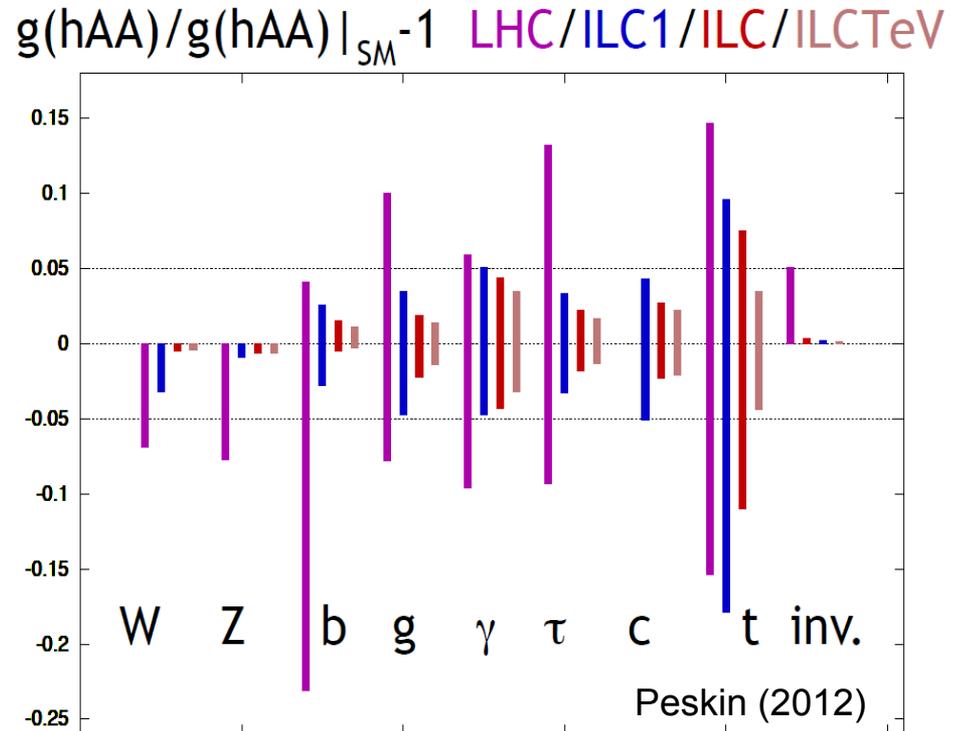


Figure 2: Comparison of the capabilities of LHC and ILC for model-independent measurements of Higgs boson couplings. The plot shows (from left to right in each set of error bars)  $1\sigma$  confidence intervals for LHC at 14 TeV with  $300\text{ fb}^{-1}$ , for ILC at 250 GeV and  $250\text{ fb}^{-1}$  (‘ILC1’), for the full ILC program up to 500 GeV with  $500\text{ fb}^{-1}$  (‘ILC’), and for a program with  $1000\text{ fb}^{-1}$  for an upgraded ILC at 1 TeV (‘ILCTeV’). More details of the presentation are given in the caption of Fig. 1. The marked horizontal band represents a 5% deviation from the Standard Model prediction for the coupling.

# HIDDEN PHOTONS

Holdom (1986)

Another possibility is

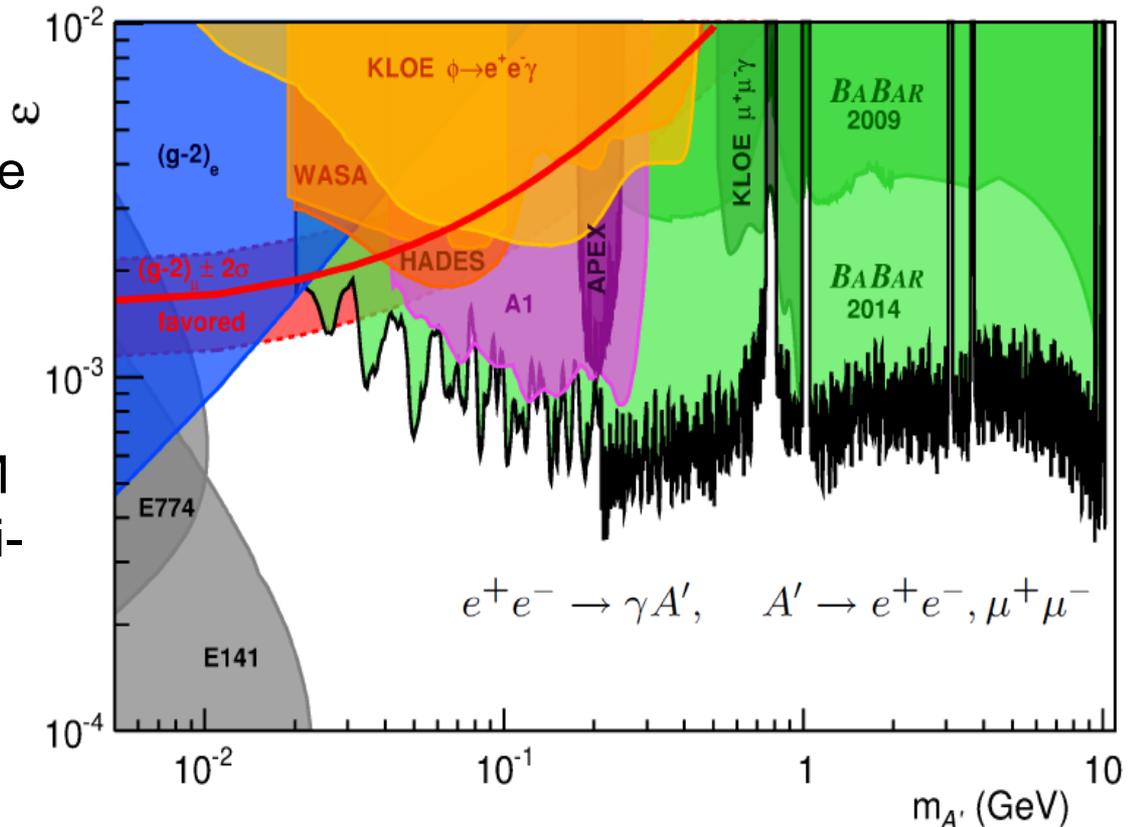
$$\epsilon F_{\mu\nu} F_h^{\mu\nu}$$

which leads to mixing between the SM photon  $\gamma$  and a hidden photon  $A'$ , which must have a mass

The hidden photon cannot be the DM, but may be a portal to the dark sector

Diagonalizing the mass matrix, one finds that the SM particles have a hidden “milli-charge” proportional to  $\epsilon$

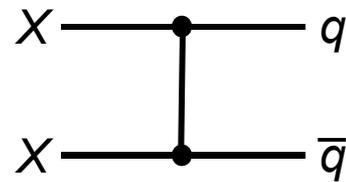
Motivates searches at the “intensity frontier”



# HIDDEN SECTOR FREEZEOUT

- The thermal relic density

$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4}$$

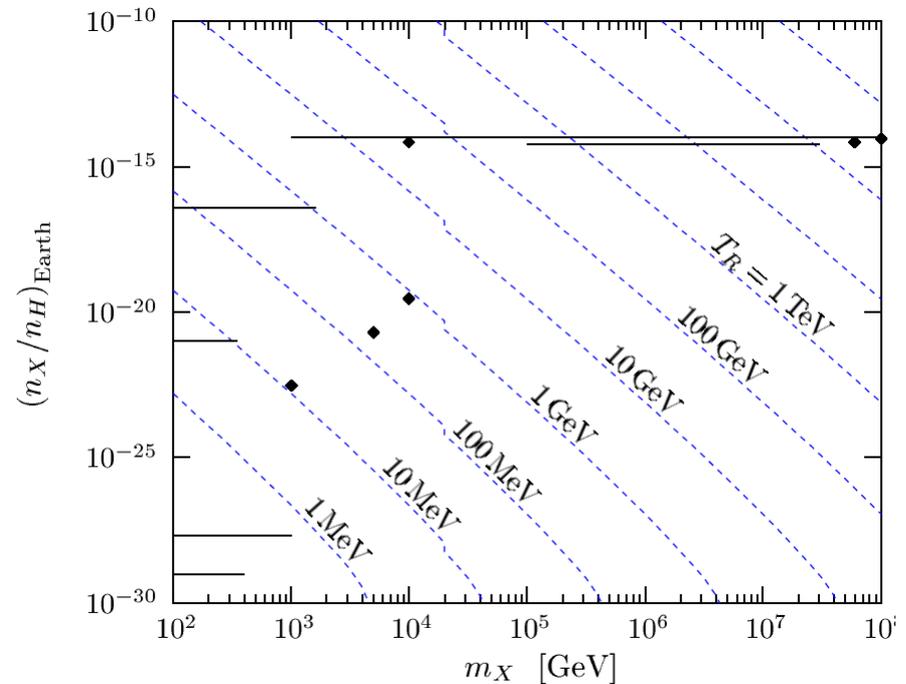


constrains only one combination of mass and coupling

- In the SM, however, we only have a few choices
  - Weak coupling:  $m_X \sim 100$  GeV,  $g_X \sim 0.6 \rightarrow \Omega_X \sim 0.1$
  - EM and strong: highly constrained

# CHARGED STABLE RELICS

- Charged stable relics create anomalously heavy isotopes
- Severe bounds from sea water searches
- Inflation can dilute this away, but there is an upper bound on the reheating temperature



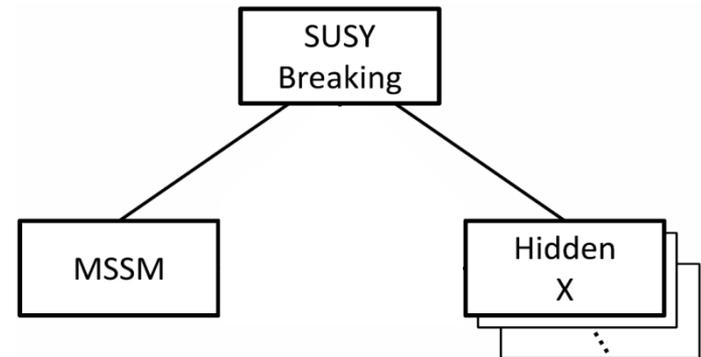
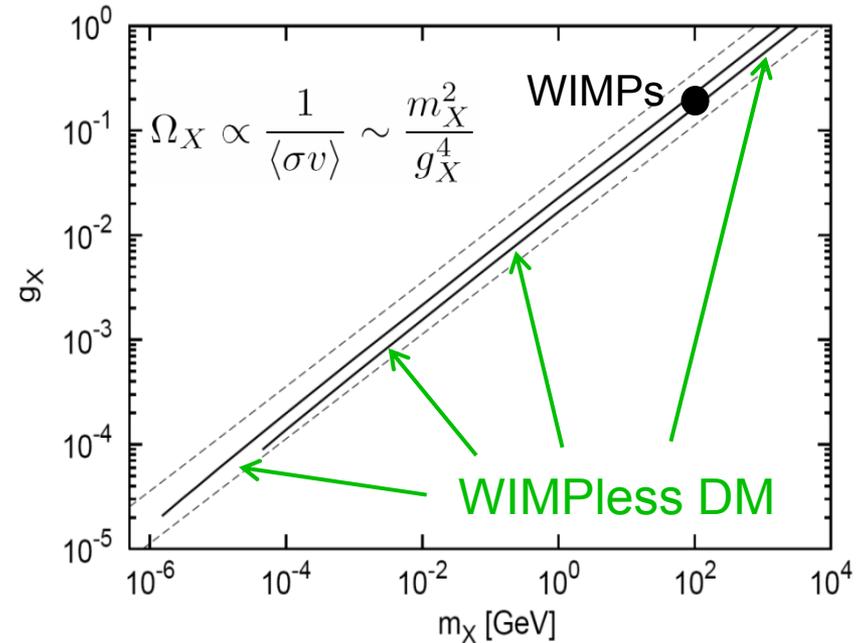
Kudo, Yamaguchi (2001)

Masses  $< \text{TeV}$  are excluded by  $T_{\text{RH}} > 1 \text{ MeV}$ ,  
but masses  $> \text{TeV}$  are allowed

# THE WIMPLESS MIRACLE

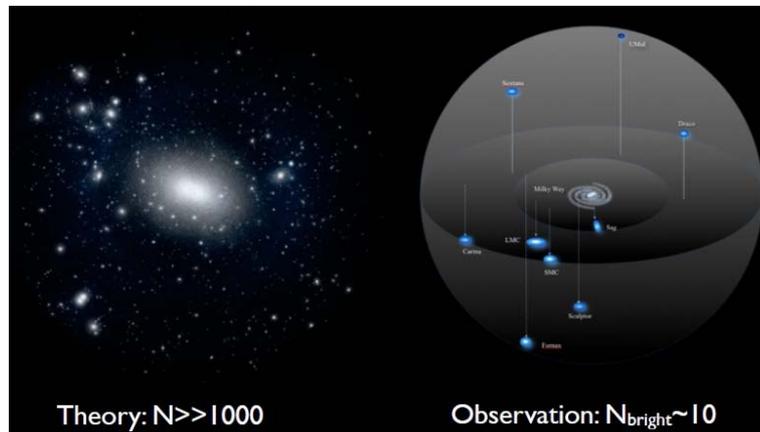
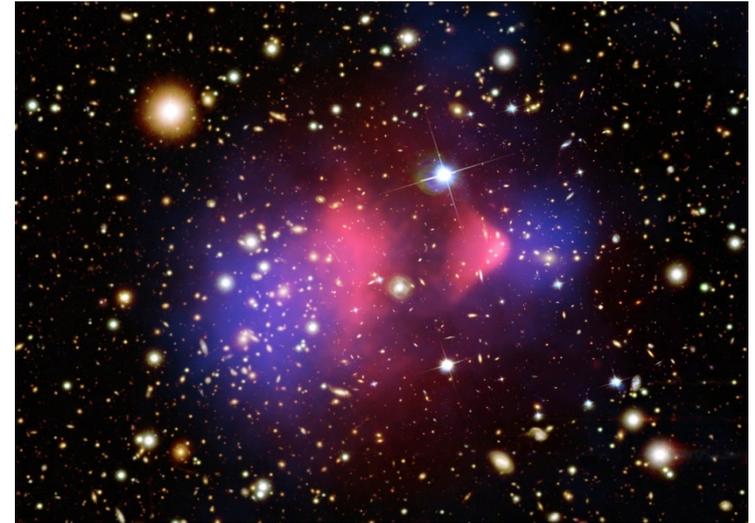
Feng, Kumar (2008); Feng, Tu, Yu (2009); Feng, Shadmi (2011)

- In a hidden sector, we can have other couplings
- In fact, in many SUSY models, to avoid unseen flavor effects, superpartner masses satisfy
 
$$m_X \sim g_X^2$$
- If this holds in a hidden sector, we have a “WIMPlless Miracle”: hidden sectors of these theories automatically have DM with the right  $\Omega$  (but they aren’t WIMPs)
- Is this what the new physics flavor problem is telling us?



# SELF-INTERACTING DARK MATTER

- If dark matter is completely hidden, can we learn anything about it?
- The Bullet Cluster provided evidence for dark matter. But the fact that dark matter passed through unperturbed  $\rightarrow$   
 $\sigma_T/m < 1 \text{ cm}^2/\text{g}$  (or barn/GeV)
- But there are indications that the self-interactions may be near this limit
  - Cusps vs. cores
  - Number of visible dwarf galaxies

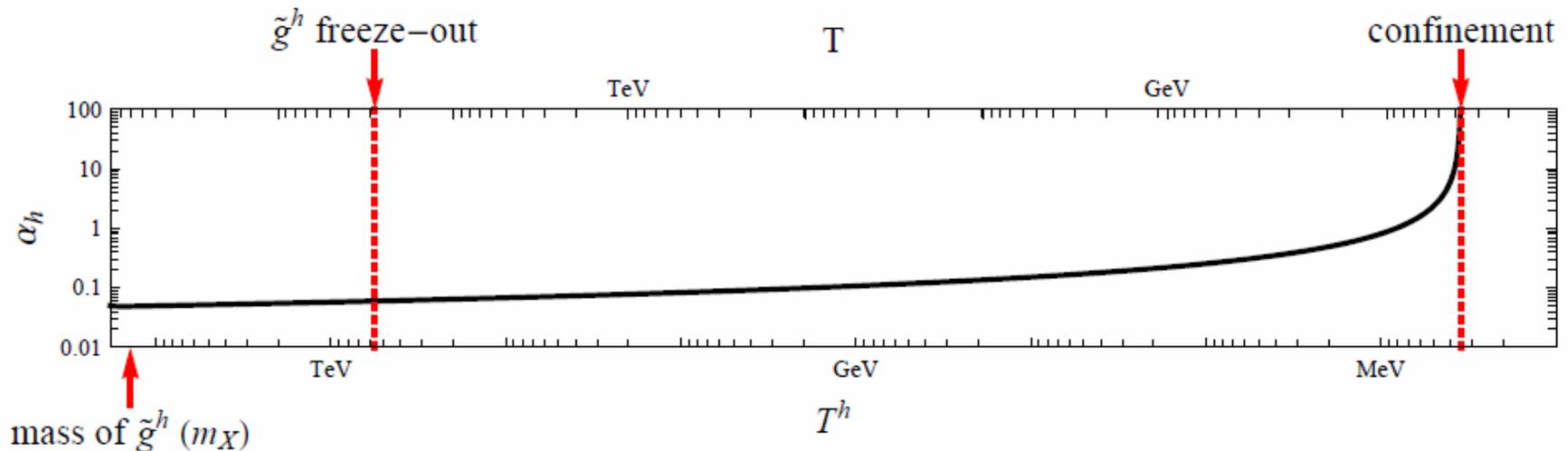


# DARK MATTER FROM HIDDEN QCD

Feng, Shadmi (2011), Boddy, Feng, Kaplinghat, Tait (2014)

- A simple example: pure SU(N) with hidden gluons  $g$  and gluinos  $\tilde{g}$
- At early times, interaction is weak,  $\sim 10$  TeV  $\tilde{g}$  freezeout with correct  $\Omega$

At late times, interaction is strong, glueballs ( $gg$ ) and glueballinos ( $g\tilde{g}$ ) form and self-interact with  $\sigma_T/m \sim 1 \text{ cm}^2/\text{g} \sim 1 \text{ barn}/\text{GeV}$



- WIMP-like: TeV-masses with correct thermal relic density
- But completely different: self-interacting, multi-component dark matter

# LECTURE 3 SUMMARY

- In addition to WIMPs, there are many other attractive DM candidates with similar motivations, but completely different implications for cosmology and HEP
- Examples: long-lived charged particles, prompt photons, invisible Higgs decays, hidden photons, ...
- Is any of this right? LHC will be running soon, direct and indirect detection, astrophysical probes are improving rapidly – we will see soon