NATURALNESS AND THE STATUS OF SUPERSYMMETRY

Jonathan Feng University of California, Irvine May 2012

SUPERSYMMETRY

- Weak-scale SUSY has long been the dominant paradigm for new particle physics
- Longstanding and strong motivations
 - A natural solution to the gauge hierarchy problem
 - Gauge coupling unification
 - An excellent DM candidate
- This is now being challenged by the LHC
 - Null results from superpartner searches
 - Results from Higgs boson searches

SUPERPARTNER SEARCHES

- An example: squark and gluino searches
 - pp $\rightarrow \tilde{g}\tilde{g} \ \tilde{g}\tilde{q}$, $\tilde{q}\tilde{q}$
 - Each squark and gluino instantaneously cascade decays, ending in a neutralino χ
 - The 2 χ 's escape the detector and are seen as missing momentum
- In tens (hundreds?) of analyses, no excess over predicted background → bounds
 - u, d, c, s squarks > 1400 GeV
 - gluinos > 900 GeV
 - top squarks > 350 GeV
 - Winos > 200 GeV
 - sleptons > 150 GeV
- Significant variations possible for other decay possibilities





REACTIONS

- These LHC results have led to many interesting statements that I disagree with. The Top 10:
 - 10. SUSY is now excluded
 - 9. Weak-scale SUSY is now excluded
 - 8. The CMSSM is now excluded
 - 7. Naturalness requires light top squarks
 - 6. It's time to stop thinking about naturalness
 - 5. The 125 GeV Higgs requires physics beyond the MSSM
 - 4. Particle physics is in trouble
 - 3. We should all be depressed
 - 2. We shouldn't be depressed, but we should start preparing to be depressed
 - 1. String theory predicts a 125 GeV Higgs

MOTIVATIONS

- Recall the three primary motivations for SUSY
 - A natural solution to the gauge hierarchy problem

Maiani (1981); Witten (1981); Veltman (1981); Kaul (1982); ...

- Gauge coupling unification

Dimopoulos, Raby, Wilczek (1981); Ibanez, Ross (1981); Einhorn, Jones (1982); ...

- An excellent DM candidate

Goldberg (1983); Ellis, Hagelin, Nanopoulos, Olive, Srednicki (1984); ...

- These motivations have been explored and developed by many people over time, but they have persisted in more or less their original form for three decades
- What do they require of the superpartner masses?

GAUGE COUPLING UNIFICATION

- The SM particles beautifully unify in SU(5) multplets, but the SU(3), SU(2), and U(1) gauge couplings do not meet at any scale
- They do unify in the MSSM
 - At a value (α < 1) that is perturbative
 - At a scale high enough (> 10¹⁶ GeV) to suppress proton decay
 - At a scale low enough (< 10¹⁸ GeV) to avoid strong gravity
- This is, however, only logarithmically sensitive to the superpartner mass scale
- Also, it has been known for decades that full SU(5) multiplets (e.g., all squarks/sleptons) can decouple without impacting unification





DARK MATTER



- SUSY contains an excellent thermal relic candidate, the neutralino
- Ω_X and annihilation strength are inversely related, so overclosure \rightarrow upper bound on DM mass

$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4}$$

$$X \longrightarrow q$$

$$X \longrightarrow \overline{q}$$

- Unfortunately, for Wino (Higgsino) DM, this bound is 3 TeV (1 TeV)
- Also, DM bound doesn't tell us anything about collider signals

NATURALNESS



• For $\Lambda \sim m_{GUT}(m_W)$, f = top, $N_f = 6$, 1% fine-tuning $\rightarrow m_{\tilde{t}} < 1$ (5) TeV

• Also, bounds on other sfermions are much weaker: $m_{\tilde{f}} < 10 (50) \text{ TeV}$ Drees (1986); Dimopoulos, Giudice (1995); Pomoral, Tomasini (1996)

FLAVOR AND CP CONSTRAINTS

- Grand unification, dark matter, and naturalness do not forbid super-TeV superpartners
- But there are also strong reasons to expect them: flavor and CP violation
- My personal favorites: electron and neutron electric dipole moments. These violate CP, but not flavor, are so are generically large even in GMSB, AMSB



 Bottom line: so far, null results from superpartner searches do not lessen the appeal of SUSY (note that this is a relative statement); those who were surprised simply haven't appreciated these constraints

EFFECTIVE SUSY, 2-1 SUSY, SUPERHEAVY SUSY

Drees (1986); Dine, Kagan, Samuel (1990); Dimopoulos, Giudice (1995); Pomoral, Tomasini (1996); Cohen, Kaplan, Nelson (1996); Dvali, Pomarol (1996); Mohapatra, Riotto (1997); Zhang (1997); Bagger, Feng, Kolda, Polonsky (1999); Agashe, Graesser (1999); Hisano, Kurosawa, Nomura (1999); ...

Transparencies from Fermilab Wine & Cheese Seminar, October 1999		
NATURALNESS RE-EXAMINED		<u>CONCLUSIONS</u>
Implications for SUSY		
at the		mSUGRA has a H_u focus point at the weak scale. Robust to variations in $M_{1/2}$, A , $\tan \beta$, m_t , Q_0 .
Tevatron and Beyond		
Jonathan Feng Institute for Advanced Study, Princeton		Naturalness limits on all scalars are greatly relaxed. Gauginos/Higgsinos still bounded by TeV. (Note: multi-TeV scalars are favored by EDMs, proton decay, gauge coupling unification)
October 1999		The discovery of all superpartners at LHC, NLC may be extremely challenging. Muon collider, VLHC?

HIGGS BOSONS

- Higgs results from the LHC and Tevatron are more challenging
- Searches for gg \rightarrow h $\rightarrow \gamma\gamma$ at the LHC and many other channels



- ~3σ (local significance) signals at 126 GeV (ATLAS), 124 GeV (CMS)
- Light Higgs windows: 117.5 118.5 GeV and 122.5 127.5 GeV
- No strong hints for non-SM Higgs couplings

HIGGS RESULTS AND SUSY

- 30,000 foot view: great for SUSY
- Closer view: challenging for SUSY
 - Tree-level: $m_h < m_Z$
 - Higgs mass requires large loop-level corrections from heavy top squarks





- But naturalness requires light top squarks. This tension is much more direct than the tension created by bounds from superpartner searches
- *Note*: expt, theory, and parametric uncertainties are each ~ 2 GeV or more

CONSTRAINTS ON SUSY

[Assumes gaugino and Higgsino masses at 1 TeV or below; rough, incomplete, other assumptions, some of which I will try to clarify]



NATURALNESS

- To understand the Higgs implications, must delve into naturalness a bit more. Two approaches:
- Option 1: "I know it when I see it." Justice Potter Stewart
- Option 2: Quantify with some well-defined naturalness prescription
- Option 1 acknowledges that naturalness is subjective, but is a non-starter. Option 2 provides an opportunity for discussion and insights, as long as its limitations are appreciated.

A NATURALNESS PRESCRIPTION

 Step 1: Choose a framework with input parameters. E.g., mSUGRA with

 $\left\{P_{\mathsf{input}}\right\} = \left\{m_0, M_{1/2}, A_0, \tan\beta, \mathsf{sign}(\mu)\right\}$

 Step 2: Fix all remaining parameters with RGEs, low energy constraints.
 E.g., at the weak scale, tree-level,

$$\frac{1}{2}m_Z^2 = \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2\beta}{\tan^2\beta - 1} - \mu^2$$

 Step 3: Choose a set of parameters as free, independent, and fundamental. E.g., mSUGRA with

 $\{a_i\} = \{m_0, M_{1/2}, A_0, B_0, \mu_0\}$

• Step 4: Define sensitivity parameters

$$c_i \equiv \left| \frac{\partial \ln m_Z^2}{\partial \ln a_i^2} \right|$$

Ellis, Enqvist, Nanopoulos, Zwirner (1986) Barbieri, Giudice (1988)

• Step 5: Define the fine-tuning parameter

$$c = \max\{c_i\}$$

Step 1: Choose a framework with input parameters. E.g., mSUGRA/CMSSM with

$$\left\{P_{\text{input}}\right\} = \left\{m_0, M_{1/2}, A_0, \tan\beta, \operatorname{sign}(\mu)\right\}$$

This is absolutely crucial. Generic SUSY-breaking is excluded, and there must be structure leading to correlated parameters. But the correlations impact naturalness; there is no model-independent measure of naturalness.

• Step 2: Fix all remaining parameters with RGEs, low energy constraints. E.g., at the weak scale

$$\frac{1}{2}m_Z^2 = \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2\beta}{\tan^2\beta - 1} - \mu^2$$

Important to refine this to include 2-loop RGEs, 1-loop threshold corrections, decouple superpartners at their mass, and minimize the potential at some appropriate scale (typically, the geometric mean of stop masses) so that quadratic contributions are included.

• Step 3: Choose a set of parameters as free, independent, and fundamental. E.g., mSUGRA with $\{a_i\} = \{m_0, M_{1/2}, A_0, B_0, \mu_0\}$

A popular choice is $\{a_i\} = \{\mu_0\}$, which leads to $c = 2\mu^2/m_Z^2$. This is a simple, but completely deficient and misleading, measure of naturalness.

Should we include other parameters, like y_t?

- No Ellis, Enqvist, Nanopoulos, Zwirner (1986); Ciafaloni, Strumia (1996), Bhattacharyya, Romanino (1996); Chan, Chattopadhyay, Nath (1997); Barbieri, Strumia (1998); Giusti, Romanino, Strumia (1998); Chankowski, Ellis, Olechowski, Pokorski (1998); …
- Yes Barbieri, Giudice (1988); Ross, Roberts (1992); de Carlos, Casas (1993); Anderson, Castano (1994); Romanino, Strumia (1999); …

No – we are trying understand the naturalness of the superpartner mass "cutoff," so include only dimensionful SUSY breaking parameters. Fine-tuning with respect to the top mass is better viewed as non-genericity.

Note: this is not an issue of what is measured and what isn't: with our current understanding, if μ were measured to be 1 PeV ± 1 eV, it will be precisely measured, but completely unnatural.

• Step 4: Define sensitivity parameters $c_i \equiv \left| \frac{\partial \ln m_Z^2}{\partial \ln a_i^2} \right|$.

Ellis, Enqvist, Nanopoulos, Zwirner (1986) Barbieri, Giudice (1988)

Why not
$$c_i \equiv \left| \frac{\partial \ln m_Z^2}{\partial \ln a_i} \right|$$
 (original definition) or $c_i \equiv \left| \frac{\partial \ln m_Z}{\partial \ln a_i^2} \right|$?

m² is more fundamental than m (it can be negative), but in any case, factors of 2 or 4 are insignificant.

• Step 5: Define the fine-tuning parameter $c = \max\{c_i\}$

Why not add in quadrature? What if c is large for all possible parameter choices (cf. Λ_{QCD})?

De Carlos, Casas (1993) Anderson, Castano (1994)

And finally, what is the maximal natural value for c: 10, 100, 1000, ... ? Some studies impose c < 10, but this is extreme. If SUSY is found and reduces c from 10^{32} to 100 or 1000, will we still be looking for a solution to the gauge hierarchy problem?





WAYS FORWARD

- Explore Higgs boson predictions, non-SM Higgs properties Carena, Gori, Shah, Wagner (2011); Heinemeyer, Stal, Weiglein (2011); Christensen, Han, Su (2012); ...
- Light SUSY with Exotic Decays: Introduce new decay modes to make light superpartners compatible with collider constraints
 Strassler, Zurek (2006), Fan, Reece, Ruderman (2011), Csaki, Grossman, Heidenreich (2011); ...
- Hidden Higgs, Buried Higgs: Make m_h < 115 GeV compatible with collider constraints
 Dermisek, Gunion (2005); Bellazzini, Csaki, Falkowski, Weiler (2009); ...
- Beyond the MSSM (NMSSM, Effective SUSY, ...): Increase particle content to raise m_h naturally, accommodate non-SM Higgs properties
 Hall, Pinner, Ruderman (2011); Ellwanger (2011); Arvanitaki, Villadoro (2011);

Gunion, Jiang, Kraml (2011); Perez (2012); King, Muhlleitner, Nevzorov (2012); Kang, Li, Li (2012);...

• Focus Point SUSY: Dynamically generated naturalness

Feng, Matchev, Moroi (1999); Feng, Matchev, Wilczek (2000); Kitano, Nomura (2005); Abe, Kobayashi, Omura (2007); Horton, Ross (2009); Asano, Moroi, Sato, Yanagida (2011); Akula, Liu, Nath, Peim (2011); Younkin, Martin (2012); ...

LIGHT SUSY WITH EXOTIC DECAYS

New decays (R-parity, hidden sectors, ...) soften LHC constraints



HIDDEN HIGGS, BURIED HIGGS

Exotic Higgs decays (h \rightarrow aa \rightarrow bbbb, ...) allow m_h < 115 GeV



BEYOND THE MSSM: NMSSM,...

Introduce new particles to raise m_h



BEYOND THE MSSM: EFFECTIVE SUSY

Like old Effective SUSY, but introduce new particles to raise m_h



FOCUS POINT SUSY

Correlations make large stop masses natural



FOCUS POINT SUSY

 RGEs play a crucial role in almost all of the main motivations for weak-scale SUSY: coupling constant unification, radiative EWSB, neutralino DM, top quark quasi-fixed point. What about naturalness?



FP SUSY: GRAPHICAL EXPLANATION

• Focus on m_{Hu}:

$$\frac{1}{2}m_Z^2 = -\mu^2 + \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2\beta}{\tan^2\beta - 1}$$
$$\approx -\mu^2 - m_{H_u}^2$$

- Insensitivity to GUT-scale parameters

 → a family of RG trajectories focus to a
 point at the weak scale
- Dynamically-generated hierarchy between the stop masses and the weak scale
- Removes large log-enhanced contributions: $\frac{2N_f}{16\pi^2}\lambda^2(m_{\tilde{f}}^2-m_f^2)\ln(\Lambda/m_h)$
- Recall: $\Lambda \sim m_{GUT} (m_W)$, and f = top, 1% fine-tuning $\rightarrow m_{\tilde{t}} < 1$ (3) TeV
- Theories with heavy stops are natural if they are focus point theories May 2012





FP SUSY: ANALYTIC EXPLANATION

Schematic form of the RGEs:
 Ass

• Assume m, A >> M_{1/2}

- Focus point if $m_{H_u}^2: m_{U_3}^2: m_{Q_3}^2: A_t^2 = 1: 1+x-3y: 1-x: 9y$ for any x, y, independent of all other SUSY breaking parameters
- CMSSM is x=y=0: this generalizes CMSSM to other natural possibilities

FP SUSY PARAMETER SPACE

- This analysis contains
 - CMSSM: (x,y) = (0,0)
 - Previous work: y=0
 - GUT models: blue line
- Provides new FP SUSY models with large stop mixing, possibly light stops within reach of LHC

Feng, Sanford (2012)



FP SUSY: NUMERICAL EXPLANATION

 By dimensional analysis, can write m_{Hu} in the following form and see the FP numerically:

$$-2m_{Hu}^{2}(M_{z}) = 5.45M_{3}^{2} + 0.0677M_{3}M_{1} - 0.00975M_{1}^{2} +0.470M_{2}M_{3} + 0.0135M_{1}M_{2} - 0.433M_{2}^{2} +0.773A_{t}M_{3} + 0.168A_{t}M_{2} + 0.0271A_{t}M_{1} +0.214A_{t}^{2} - 1.31m_{Hu}^{2} + 0.690m_{Q_{3}}^{2} + 0.690m_{U_{3}}^{2}$$

Abe, Kobayashi, Omura (2007)

 In fact, special cases of FP SUSY can be seen in the results of some early (pre-top quark) studies

Alvarez-Gaume, Polchinski, Wise (1983); Barbieri, Giudice (1988)

 The underlying structure is obscured by the numerical calculations, but this is also a way forward to find new FP possibilities, e.g., involving non-universal gaugino masses

Abe, Kobayashi, Omura (2007); Horton, Ross (2009); Younkin, Martin (2012)

IMPLICATIONS

- All scalars may be heavy, but naturalness is preserved
- Naturalness is useful if it leads us toward theories that describe data. Let's assume all scalars are heavy and at the same scale. How does such a theory fare?
- FP SUSY fits all the data so far
 - Higgs boson mass
 - Coupling constant unification and proton decay
 - Natural suppression of EDMs
 - LHC: gluinos with top- and bottom-rich decays
 - Excellent dark matter candidate (mixed Bino-Higgsino)

Feng, Matchev (2000); Feng, Matchev, Wilczek (2000)

OTHER HEAVY STOP MODELS

- FP SUSY has naturally heavy stops; they can also be unnaturally heavy
- Split SUSY

Arkani-Hamed, Dimopoulos (2004); Giudice, Romanino (2004)

- Extremely heavy scalars; if above 1 PeV, possibly long-lived gluinos, otherwise, phenomenology essentially identical to FP SUSY
- Manifestly unnatural, motivated by the anthropic principle
- String-inspired Models

Feldman, Kane, Kuflik, Lu (2011); Kane, Kumar, Lu, Zheng (2011)

- "String theory is already or soon being tested in several ways, including correctly predicting the recently observed Higgs boson properties and mass"
- 30 TeV squarks, phenomenology essentially identical to FP SUSY, but extremely fine-tuned: low μ , but large fine-tuning in m_{Hu}
- For $tan\beta > 2$, $m_h = 100-127 \text{ GeV}$



LHC

- Commonly heard statements: SUSY is in trouble, CMSSM is excluded
- Actually, the CMSSM has never been more useful and likely to be *effectively* correct
- The region of interest
- Custom-built for analysis: Higgs results, etc. suggest that SUSY is already a simplified model, with just a few parameters (μ, M_{1/2}, tanβ)
- Generalize to (μ, M₁, M₂, M₃, tanβ); may use Ω to removes one, collider results probably insensitive to tanβ



DARK MATTER

- The neutralino is the classic WIMP
 - ~ 50 GeV 1 TeV
 - weakly-interacting
 - Naturally the lightest standard model superpartner in many models



• So many SUSY models and parameters. Can we say anything interesting? Generically, no.

NEUTRALINO DM



Jungman, Kamionkowski, Griest (1995)

NEUTRALINO DM SIMPLIFIED

• But there essentially two classes of diagrams:



If all scalars are at the same scale, the LHC has eliminated the 2nd one.

- If M₂ > M₁, no special cases (co-annihilation, resonances), this fixes the neutralino's coupling to Ws as a function of its mass.
- But this also fixes the DM scattering cross section as a function of its mass, predictions collapse to a band.



NEUTRALINO DETECTION PROSPECTS



- Direct detection cross section: strong dependence on strange content
- Predicted cross sections not excluded, but very close to current bounds; a signal should be seen soon (e.g., this summer at IDM2012)

SUMMARY

- LHC superpartner null results do not exclude weak-scale SUSY; the main motivations remain intact
 - Naturalness
 - Gauge coupling unification
 - Dark matter
- Higgs boson results are more challenging for naturalness
- Straightforward interpretation of all data so far: multi-TeV scalars, most naturally realized in focus point theories
 - Simple: minimal field content, standard decay modes
 - Expect discovery of SM-like 125 GeV Higgs soon
 - LHC: promising signals include gluinos with t- and b-rich cascade decays, chargino and neutralino searches, stop searches
 - EDMs very promising
 - DM: neutralino WIMPs with large scattering cross section, exciting prospects for direct and indirect detection