ASTRO AND PARTICLE CONNECTIONS

Theoretical Advanced Studies Institute (TASI) University of Colorado, Boulder Jonathan Feng UC Irvine 20-22 June 2011

TASI 2011: THE DARK SECRETS OF THE TERASCALE

- This TASI anticipates the coming revolution in terascale particle physics
- We are living through a period of scientific revolution in the closely allied field of cosmology
- These 3 lectures are devoted to explaining how the terascale and cosmology might be related

TASI 2011: The Dark Secrets of the Terascale

Week 1:	June 6-10	Tutorial: CalcHEP/CompHEP				
	Monday	Tuesday	Wednesday	Thursday	Friday	
9:00-10:15 AM		Ramond	Reina	Ramond	Ligeti	
10:15-10:45 AM	coffee break	coffee break	coffee break	coffee break	coffee break	
10:45-12:00 PM	Ramond	Reina	Ligeti	Ligeti	Ramond	
2:00-3:15 PM	Reina	Kong	Ramond	Kong	Campbell	
3:15-3:45 PM	coffee break	coffee break	coffee break	coffee break	coffee break	
3:45-5:00 PM	Kong		Kong			
Evening 7:30 PM				Public lecture		
G1B30 Duane				P. Ramond		

Week 2:	June 13-17	Tutorial: PYTHI/	A+PGS		
9:00-10:15 AM	Martin	Campbell	Conway	Martin	Martin
10:15-10:45 AM	coffee break	coffee break	coffee break	coffee break	coffee break
10:45-12:00 PM	Campbell	Martin	Martin	Kong	Kong
2:00-3:15 PM	Kong	Kong	Conway	Conway (PGS)	
3:15-3:45 PM	coffee break	coffee break	coffee break	coffee break	
3:45-5:00 PM	Campbell				

	Week	3:	June 20-24
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June 2	20-24	
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9:00-10:15 AM		Ponton	Wang	Everett	Wacker
10:15-10:45 AM	coffee break	coffee break	coffee break	coffee break	coffee break
10:45-12:00 PM	Ponton	Feng	Feng	Ponton	Everett
2:00-3:15 PM	Feng	Wang	Everett	Wacker	Ponton
3:15-3:45 PM	coffee break	coffee break	coffee break	coffee break	coffee break
3:45-5:00 PM	Wang		Wacker	Wang	
Evening 7:30 PM		Public lecture			
G1B30 Duane		J. Feng			

Week 4:

June 27-July 1 Tutorial: MicrOMEGAs

9:00-10:15 AM	Chung	Lester	Chung	Lykken	Lester
10:15-10:45 AM	coffee break				
10:45-12:00 PM	Lester	Chung	Lester	Lester	Lykken
2:00-3:15 PM	Murgia	Murgia	Saab	Saab	
3:15-3:45 PM	coffee break	coffee break	coffee break	coffee break	
3:45-5:00 PM	Pukhov	Pukhov	Pukhov	Pukhov	

OUTLINE

LECTURE 1

Essential Cosmology, Dark Energy, WIMP Miracle

LECTURE 2

WIMP Detection, WIMPs at Colliders

LECTURE 3

Other Terascale Dark Matter Possibilities

ESSENTIAL COSMOLOGY

- For the first time in history, we now have a complete *picture* of the Universe
- How did this come about?
- Here review the standard model of cosmology and some of the key observational evidence leading to it
- Little knowledge of cosmology assumed; focus on heuristic derivations, order-of-magnitude estimates, intuitive arguments

COSMOLOGY BASICS

- The evolution of the Universe is dominated by gravity, described by the Einstein equations $R_{\mu\nu} \frac{1}{2}Rg_{\mu\nu} = 8\pi GT_{\mu\nu}$
- The (flat, k=0) Friedmann-Lemaitre-Robertson-Walker metric is $ds^{2} = dt^{2} - a^{2}(t) \left[dr^{2} + r^{2} d\theta^{2} + r^{2} \sin^{2} \theta d\phi^{2} \right]$
- The stress-energy tensor is $T^{\mu}{}_{\nu} = \text{diag} \left[\rho(t), -p(t), -p(t), -p(t)\right]$ We may parameterize various materials by w, where $p = w\rho$
- Stress-energy conservation $T^{\mu\nu}_{;\nu} = 0 \rightarrow \rho \sim a^{-3(1+w)}$
- The Einstein equations imply the Friedmann equation

$$H^2 \equiv \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho$$

$$MD: \rho \propto a^{-3} \Rightarrow \dot{a}^2 \propto \frac{1}{a} \Rightarrow a \propto t^{2/3}$$
$$RD: \rho \propto a^{-4} \Rightarrow \dot{a}^2 \propto \frac{1}{a^2} \Rightarrow a \propto t^{1/2}$$
$$VD: \rho \propto a^0 \Rightarrow \dot{a}^2 \propto a^2 \Rightarrow a \propto e^{ct}$$

ROTATION CURVES OF GALAXIES

Sa NGC 4594 350 300 ROTATIONAL VELOCITY (km s⁻⁴) Sa NGC 4378 Sab-Sb NGC 7212 Sb NGC 2590 Sbc NGC 3145 250 Sbc NGC 1620 Sbc-Sc NGC 7664 200 Rubin, Ford, Thonnard (1978) 5 10 15 20 25 DISTANCE FROM NUCLEUS (kpc)

Rubin, Ford (1970); Bosma (1978)

- Rotational velocity v_c as function of distance from center r
 - $v_c \sim O(300) \text{ km/s} \sim O(10^{-3}) \text{ c}$

-
$$r \sim few kpc (pc = 3.26 ly)$$

 Expect v_c ~ r^{-1/2} beyond luminous region

$$\frac{mv_c^2}{r} = G_N \frac{mM}{r^2}$$

Instead find $v_c \sim constant$

• The discrepancy may be resolved by missing mass and is classic (but not the first) evidence for dark matter

AN EXAMPLE: NGC 2403





- v_c from HI line
- Fit mass-to-light ratio, dark halo model; this tells us about ρ(r)
- For Milky Way, get ρ~0.2-0.5 GeV/cm³





MISSING MASS IN CLUSTERS OF GALAXIES

Zwicky (1933)



- ~10-1000 galaxies, the largest gravitationally-bound structures;
- Intracluster gas mass, total mass constrained by X-rays from bremsstrahlung, lensing, etc.
- Gas mass fraction f_{gas} as function of distance from center

-
$$f_{gas} = \rho_B / \rho_M$$

• r₂₅₀₀ ~ Mpc

• Extrapolating from clusters to the whole Universe, this constrains $\Omega_{\rm M} = \Omega_{\rm B} \rho_{\rm M} / \rho_{\rm B}$, where $\Omega = \rho / \rho_{\rm c}$ is energy density in units of the critical density and $\Omega_{\rm B}$ is determined independently

RECESSIONAL VELOCITIES



Velocity-Distance Relation among Extra-Galactic Nebulae.



- The original evidence that the universe is expanding
- Now carried out to far larger distances with supernovae
- Constrains the acceleration of expansion:

$$\label{eq:Olympicture} \begin{split} \Omega_{\Lambda} & - \,\Omega_{\mathsf{M}} \\ \text{``Attractive matter vs.} \\ \text{repulsive dark energy''} \end{split}$$

COSMIC MICROWAVE BACKGROUND



 δT/T << 1: The universe is isotropic and homogeneous on large scales



- Constrains the geometry of the universe: $\Omega_{\Lambda} + \Omega_{M}$ "total energy density"

BIG BANG NUCLEOSYNTHESIS



- At T ~ 1 MeV, the universe cooled enough for light elements to start forming
- The abundance of each light species is fixed by η, the baryon-to-photon ratio
- These determinations are consistent* and constrain (with the CMB) the density in baryons: Ω_B

SYNTHESIS



Remarkable agreement

Dark Matter: $23\% \pm 4\%$ Dark Energy: $73\% \pm 4\%$ Baryons: $4\% \pm 0.4\%$ [vs: 0.2% for Σ m = 0.1 eV]

Remarkable precision (~10%)

Remarkable results

STANDARD COSMOLOGICAL HISTORY

- For many applications, temperature is a better clock than time. We would like to find the time-temperature correspondence.
- For radiation, $\rho \propto a^{-4}$
- But by dimensional analysis, $\rho \propto T^4 \Rightarrow T \propto \frac{1}{a}$
- The relations in the matter- and radiation-dominated eras are therefore

MD :
$$T \propto t^{-2/3}$$

$$\mathsf{RD}$$
 : $T \propto t^{-1/2}$

WHAT DOMINATES WHEN?

• We know $\Omega_{\Lambda} \approx 0.73$, $\Omega_{M} \approx 0.27$. We can also determine

$$\begin{split} \Omega_{\text{CMB}} &\equiv \frac{\rho_{\text{CMB}}}{\rho_c} \sim \frac{T_{\text{CMB}}^4}{\frac{3H^2}{8\pi G}} \sim \frac{(2.7 \text{ K})^4 (14 \text{ Gyr})^2}{(10^{19} \text{ GeV})^2} \\ &\sim \frac{(10^{-4} \text{ eV})^4 (14\pi \times 10^{16} \text{ s})^2}{(10^{-16} \text{ eV} \text{ s})^2 (10^{28} \text{ eV})^2} \sim 10^{-4} \end{split}$$

- Matter-radiation equality $- T \sim 10^4 T_0 \sim eV$ $- t \sim 10^{-6} t_0 \sim 10^{12} s$
- Vacuum-matter equality
 yesterday (roughly)



THERMAL HISTORY OF THE UNIVERSE



DECOUPLING

• Decoupling of particle species is an essential concept for particle cosmology. It is described by the Boltzmann equation

$$\frac{dn}{dt} = -3Hn - \langle \sigma v \rangle \begin{bmatrix} n^2 - n_{eq}^2 \\ \uparrow & \checkmark \end{bmatrix}$$
Dilution from $XX \rightarrow f\overline{f} \qquad f\overline{f} \rightarrow XX$
expansion

- Particles decouple (or freeze out) when $n_{
 m eq} \langle \sigma v \rangle \sim H$
- An example: neutrino decoupling. By dimensional analysis,

$$n_{\rm eq} \sim T^3 \qquad \langle \sigma v \rangle \sim G_F^2 T^2 \qquad H \sim T^2 / M_{\rm Pl}$$

 $T^3 \sim M_W^4 / M_{\rm Pl} \Rightarrow T \sim {\rm MeV}$

THERMAL HISTORY OF THE UNIVERSE



PROBLEMS

The standard model of cosmology answers many questions, but also highlights many others:

- What is dark matter?
- What is the distribution of dark matter?
- How did structure form?
- What is dark energy?
- Why is the cosmological constant so small?
- Why matter and no anti-matter?
- Why are all energy densities roughly comparable now?
- How did the universe begin?
- •

Particle physics is required to answer these, not least because it is required to understand the hot early Universe

DARK ENERGY

- $\Omega_{\Lambda} \approx 0.73 \rightarrow \rho_{\Lambda} \sim (meV)^4$: tiny, but all fields contribute
- Quantum mechanics:

 $\pm \frac{1}{2}\hbar \omega$, $\omega^2 = k^2 + m^2$

• Quantum field theory:

$$\pm \frac{1}{2} \int^{E} d^{3}k \, \hbar \, \omega \sim \pm E^{4},$$

where E is the energy scale where the theory breaks down

• We expect

 $(M_{\text{Planck}})^4 \sim 10^{120} \rho_{\Lambda}$ $(M_{\text{GUT}})^4 \sim 10^{108} \rho_{\Lambda}$

 $(M_{\rm SUSY})^4 \sim 10^{60} - 10^{90} \rho_{\Lambda}$ $(M_{\rm weak})^4 \sim 10^{60} \rho_{\Lambda}$

ONE APPROACH

Small numbers ↔ broken symmetry

 $\rho_{\Lambda} \sim M_{\rm Pl}^{4}$



ANOTHER APPROACH

Many densely-spaced

eternal inflation, etc.)

vacua (string landscape,

Anthropic principle: $-1 < \Omega_{\Lambda} < 100$

 $\rho_{\Lambda} \sim M_{\rm Pl}^4$

Weinberg (1989)

DARK ENERGY PROSPECTS

- These approaches are very different. Their only similarity is that the more you think about either one, the more you think the other one must be more promising.
- Terascale prospects:
 - Worst case imaginable: we discover only the minimal Higgs boson
 - Best case imaginable: we discover the minimal Higgs boson. At least we'll know that fundamental scalars exist!
- Challenge: identify a concrete scenario in which the LHC will shed light on dark energy (crazy is ok)

DARK MATTER



Known DM properties

- Gravitationally
 interacting
- Not short-lived
- Not hot
- Not baryonic

Unambiguous evidence for new particles

DARK MATTER CANDIDATES

- There are many
- Masses and interaction strengths span many, many orders of magnitude, but the gauge hierarchy problem especially motivates Terascale masses



HEPAP/AAAC DMSAG Subpanel (2007)

FREEZE OUT: QUALITATIVE

(1) Assume a new heavy particle X is initially in thermal equilibrium:

$$XX \leftrightarrow \bar{q}q$$

(2) Universe cools:

$$XX \stackrel{-}{\leftrightarrow} \bar{q}q$$

(3) Universe expands:

$$XX \notin \bar{q}q$$



FREEZE OUT: MORE QUANTITATIVE

 The Boltzmann equation:

 $\frac{dn}{dt} = -3Hn - \langle \sigma v \rangle \left[n^2 - n_{\rm eq}^2 \right]$ **Dilution from** expansion

 $\chi \chi \to f \,\overline{f} \qquad f \,\overline{f} \to \chi \chi$

 n ≈ n_{ea} until interaction rate drops below expansion rate:

$$\frac{n_{\rm eq} \langle \sigma v \rangle \sim H}{(mT)^{3/2} e^{-m/T} m^{-2} T^2/M_{\rm Pl}}$$

Might expect freeze out at $T \sim m$, but the universe expands slowly! First guess: m/T ~ ln (M_{PI}/m_W) ~ 40



THE WIMP MIRACLE

• The relation between Ω_X and annihilation strength is wonderfully simple:

$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4}$$



• $m_X \sim 100 \text{ GeV}, g_X \sim 0.6 \rightarrow \Omega_X \sim 0.1$



LHC/ILC HEPAP, Matchev et al. (2005)

• Remarkable coincidence: particle physics independently predicts particles with the right density to be dark matter

STABILITY

New Particle States

 This all assumes the WIMP is stable

• How natural is this?



LEP'S COSMOLOGICAL LEGACY



• Simple solution: impose a discrete parity, so all interactions require pairs of new particles. This also makes the lightest new particle stable:

LEP constraints \leftrightarrow Discrete Symmetry \leftrightarrow Stability

Cheng, Low (2003); Wudka (2003)

• The result: dark matter is easier to explain than no dark matter, and the WIMP paradigm is more natural than ever before, leading to a proliferation of candidates

WIMP EXAMPLES

- Weakly-interacting massive particles: many examples, broadly similar, but different in detail
- The prototypical WIMP: neutralinos in supersymmetry

Goldberg (1983)

• KK B¹ ("KK photons") in universal extra dimensions

Servant, Tait (2002); Cheng, Feng, Matchev (2002)

NEUTRAL SUSY PARTICLES

	U(1)	SU(2)	Up-type	Down-type		
Spin	<i>M</i> ₁	<i>M</i> ₂	μ	μ	$m_{ ilde{ u}}$	<i>m</i> _{3/2}
2						G
						graviton
3/2		Nlaute				Ĝ
		Neutr	alinos: {χ⊧	$\equiv \chi_1, \chi_2, \chi_3, \gamma$	$\{4\}$	gravitino
1	В	W ^o				
1/2	Ĩ	Ŵ ⁰	$ ilde{H}_u$	$ ilde{H_d}$	ν	
	Bino	Wino	Higgsino	Higgsino		
0			H _u	H _d	ĩ	
					sneutrino	

R-PARITY AND STABLE LSPS

• One problem: proton decay



- Forbid this with R-parity conservation: R_ρ = (-1)^{3(B-L)+2S}

 SM particles have R_ρ = 1, SUSY particles have R_ρ = -1
 Require Π R_ρ = 1 at all vertices
- Consequence: the lightest SUSY particle (LSP) is stable!

WHAT'S THE LSP?

- High-scale → weak scale through RGEs.
- Gauge couplings increase masses;
 Yukawa couplings decrease masses
- "typical" LSPs: χ , $\tilde{\tau}_R$



Particle physics alone \rightarrow neutral, stable, cold dark matter

RELIC DENSITY

Neutralinos annihilate through *many* processes. [→]
 But there are typically two dominant classes:



- χ are Majorana fermions, so Pauli exclusion $\rightarrow S_{in} = 0$, *L* conservation \rightarrow
 - *P*-wave suppression: $\sigma v \sim \sigma_0 + \sigma_1 v^2$,
 - $mv^2/2 = 3T/2 \rightarrow v^2 \sim 3T/m \sim 0.1$
 - m_f/m_W suppression
- Gauge boson diagrams suppressed for χ ≈ Bino

Bottom line: annihilation is typically suppressed, $\Omega_{DM}h^2$ is typically high

NEUTRALINO ANNIHILATION



Jungman, Kamionkowski, Griest (1995)
COSMOLOGICALLY PREFERRED SUPERSYMMETRY

Typically get too much DM, but there are mechanisms for reducing it



KK DARK MATTER

 Consider 1 extra spatial dimensions curled up in a small circle



• Particles moving in extra dimensions appear as a set of copies of normal particles.



 A problem: many extra 4D fields; some with mass n/R, but some are massless! E.g., 5D gauge field:

$$V_{\mu}(x^{\mu}, y) = \underbrace{V_{\mu}(x^{\mu})}_{\text{good}} + \sum_{n} V_{\mu}^{n}(x^{\mu})\cos(ny/R) + \sum_{m} V_{\mu}^{m}(x^{\mu})\sin(my/R)$$
$$V_{5}(x^{\mu}, y) = \underbrace{V_{5}(x^{\mu})}_{\text{bad}} + \sum_{n} V_{5}^{n}(x^{\mu})\cos(ny/R) + \sum_{m} V_{5}^{m}(x^{\mu})\sin(my/R)$$

• A solution...

• Compactify on S^1/Z_2 instead (orbifold); require

 $y \rightarrow -y$: $V_{\mu} \rightarrow V_{\mu}$ $V_5 \rightarrow -V_5$

• Unwanted scalar is projected out:

$$V_{\mu}(x^{\mu}, y) = \underbrace{V_{\mu}(x^{\mu})}_{\text{good}} + \sum_{n} V_{\mu}^{n}(x^{\mu}) \cos(ny/R) + \underbrace{\sum_{m} V_{\mu}^{m}(x^{\mu}) \sin(my/R)}_{m}$$
$$V_{5}(x^{\mu}, y) = \underbrace{V_{5}(x^{\mu})}_{\text{bad}} + \sum_{n} \frac{V_{5}^{n}(x^{\mu}) \cos(ny/R)}_{5} + \sum_{m} V_{5}^{m}(x^{\mu}) \sin(my/R)$$

• Similar projection on fermions → chiral 4D theory, …

Appelquist, Cheng, Dobrescu (2001)

KK-PARITY

- A consequence: KK-parity (-1)^{KK} conserved: interactions require an even number of odd KK modes
- 1st KK modes must be pair-produced at colliders
 Appelquist, Cheng, Dobrescu (200

Appelquist, Cheng, Dobrescu (2001) Macesanu, McMullen, Nandi (2002)

 LKP (lightest KK particle) is stable – dark matter!

B¹ ANNIHILATION

- The level-1 KK hypercharge gauge boson B¹ is often the LKP, is neutral, and so is a natural DM candidate
- It's a massive gauge boson, annihilates through S-wave processes, so preferred masses are larger than in SUSY



MORE B¹ ANNIHILATION

 Minimal UED has a compressed spectrum, so coannihilation is natural. In contrast to SUSY, these typically add to the relic density



• Level-2 KK resonances



Servant, Tait (2002); Burnell, Kribs (2005) Kong, Matchev (2005); Kakizaki, Matsumoto, Sato, Senami (2005)

KK DARK MATTER RELIC DENSITY



Mass of Dark Matter Particle from Extra Dimensions (TeV)

Prediction for $\Omega_{B^{(1)}}h^2$ The solid line is the case for $B^{(1)}$ alone, and the dashed and dotted lines correspond to the case in which there are one (three) flavors of nearly degenerate $e_R^{(1)}$. For each case, the black curves (upper of each pair) denote the case $\Delta = 0.01$ and the red curves (lower of each pair) $\Delta = 0.05$.

LECTURE 1 SUMMARY

- The revolution in cosmology has produced remarkable progress and highlights remarkable problems
- Cosmology and particle physics both point to the Terascale for new particles, with viable WIMP candidates from SUSY, UED, etc.
- Next time: what are the implications for dark matter searches?

OUTLINE

LECTURE 1

Essential Cosmology, Dark Energy, WIMP Miracle

LECTURE 2

WIMP Detection, WIMPs at Colliders

LECTURE 3

Other Terascale Dark Matter Possibilities

WIMP DETECTION

Correct relic density \rightarrow Efficient annihilation then



Efficient scattering now (Direct detection)

DIRECT DETECTION

- Look for normal matter recoiling from DM collisions
- WIMP properties
 - m ~ 100 GeV
 - velocity ~ 10^{-3} c
 - Recoil energy ~ 1-100 keV
- Typically focus on ultrasensitive detectors placed deep underground
- But first, what range of interaction strengths are to be probed?



THE BIG PICTURE: UPPER BOUND

• What is the upper bound?

 Strongly-interacting window is now closed



THE BIG PICTURE: LOWER BOUND

- Is there (effectively) a lower bound?
- Solar, atmospheric, and diffuse supernova background neutrinos provide an "irreducible background"
- The limits of background-free, non-directional direct detection searches (and also the metric prefix system!) will be reached by ~10 ton experiments probing



SPIN-INDEPENDENT VS. SPIN-DEPENDENT SCATTERING

• Consider neutralinos with quark interactions

$$\mathcal{L} = \sum_{q=u,d,s,c,b,t} \left(\alpha_q^{\rm SD} \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q + \alpha_q^{\rm SI} \bar{\chi} \chi \bar{q} q \right)$$

- DM particles now have v ~ 10⁻³ c. In the nonrelativistic limit, the first terms reduce to a spin-spin interactions, and so are called spin-dependent interactions
- The second terms are spin-independent interactions; focus on these here

SPIN-INDEPENDENT THEORY

 Theories give DM-quark interactions, but experiments measure DMnucleus cross sections

$$\sigma_{\rm SI} = \frac{4}{\pi} \mu_N^2 \sum_q \alpha_q^{\rm SI2} \left[Z \frac{m_p}{m_q} f_{T_q}^p + (A - Z) \frac{m_n}{m_q} f_{T_q}^n \right]^2 ,$$

where $\mu_N = \frac{m_\chi m_N}{m_\chi + m_N}$ is the reduced mass, and $f_{T_q}^{p,n} = \frac{\langle p, n | m_q \bar{q}q | p, n \rangle}{m_{p,n}}$

is the fraction of the nucleon's mass carried by quark q, with

 $\begin{aligned} f_{T_u}^p &= 0.020 \pm 0.004 & f_{T_u}^n = 0.014 \pm 0.003 & f_{T_s}^p = 0.118 \pm 0.062 & f_{T_s}^n = 0.118 \pm 0.062 \\ f_{T_d}^p &= 0.026 \pm 0.005 & f_{T_d}^n = 0.036 \pm 0.008 & f_{T_{c,b,t}}^{p,n} = \frac{2}{27} f_{T_G}^{p,n} = \frac{2}{27} (1 - f_{T_u}^{p,n} - f_{T_d}^{p,n} - f_{T_s}^{p,n}) \end{aligned}$

The last one accounts for gluon couplings through heavy quark loops.

• This may be parameterized by $\sigma_A = \frac{\mu_A^2}{M_*^4} [f_p Z + f_n (A - Z)]^2$, where $f_{p,n}$ are the nucleon level couplings. Note that f_p and f_n are not necessarily equal.

SPIN-INDEPENDENT EXPERIMENT

• The rate observed in a detector is $R = \sigma_A I_A$, where



- Results are typically reported assuming $f_p = f_n$, so $\sigma_A \sim A^2$, and scaled to a single nucleon

SPIN-INDEPENDENT: CURRENT STATUS



LOW CROSS SECTION FRONTIER

- The excitement stems from the confrontation of experiment with theory
- What are the shaded regions?



SUPERSYMMETRY

- Ad hoc theoretical assumptions \rightarrow 4+1 parameters
- Assume $\Omega_x = 0.23 \rightarrow$ require efficient annihilation channel
- Now constrained by LHC searches



DIRECT DETECTION IMPLICATIONS



MODEL INDEPENDENCE

- Can relax unification
 assumptions
- There are exceptions from accidental mass degeneracies, leading to co-annihilation and resonances, but the generic conclusions are surprisingly robust
- The bottom line: the LHC is starting to eliminate models with poor direct detection prospects, but those with bright prospects remain





LOW MASS FRONTIER

Collision rate should change as Earth's velocity adds constructively/destructively with the Sun's → annual modulation

Drukier, Freese, Spergel (1986)



DAMA/LIBRA: 8.9 σ signal with T \approx 1 year, maximum \approx June 2



CURRENT STATUS

- DAMA is now supplemented by CoGeNT
- Most recently, the CoGeNT favored region has been further constrained, preliminary 2.8σ annual modulation signal presented
- Theoretical puzzles
 - Low mass and high σ
 - DAMA ≠ CoGeNT
 - Excluded by XENON, CDMS
- Many proposed explanations

Hooper, Collar, Hall, McKinsey (2010) Fitzgerald, Zurek (2010) Fox, Liu, Weiner (2010)



ISOSPIN-VIOLATING DARK MATTER

 Recall that DM scattering off nuclei is

- $\sigma_A \sim [f_p Z + f_n (A-Z)]^2$

• Typically assume

$$- f_n = f_p$$
$$- \sigma_A \sim A^2$$

- One simple possibility is to relax this assumption, introduce 1 extra parameter: f_n / f_p

Giuliani (2005)

Chang, Liu, Pierce, Weiner, Yavin (2010)

Feng, Kumar, Marfatia, Sanford (2011)

- Can decouple any given isotope by a suitable choice of f_n / f_p .
- Crucially important to account for isotope distributions

TABLE II. A_i for isotopes and their fractional number abundances η_i in percent for all isotopes with $\eta_i > 1\%$.

Xe	Ge	Si	Ca	W	Ne
128(1.9)	70(21.2)	28 (92.2)	40 (96.9)	182(26.5)	20 (90.5)
129(26.4)	72(27.7)	29(4.7)	44(2.1)	183(14.3)	22 (9.3)
130(4.1)	73(7.7)	30(3.1)		184(30.6)	
131(21.2)	74(35.9)			186(28.4)	
132 (26.9)	76(7.4)				
134(10.4)					
$136 \ (8.9)$					
		Lana Ku	mar Marf	atia Canta	-d (0011)

Feng, Kumar, Marfatia, Sanford (2011)

RECONCILING XENON/DAMA/COGENT



IMPLICATIONS OF THE IVDM RESOLUTION

- IVDM cannot resolve disagreements between identical targets; if correct, IVDM implies CDMS and CoGeNT are marginally consistent
- Predictions for all other elements are fixed. For example, as conventionally plotted (assuming f_p = f_n),

 $\sigma_p(\text{oxygen, carbon}) \approx 8.4 \sigma_p(\text{germanium})$ $\sigma_p(\text{flourine}) \approx 4.2 \sigma_p(\text{germanium})$

- XENON will see a signal soon; CRESST may have already
- Reverses σ ~ A² conventional wisdom. Need more than one target material and more than one experiment per material

INDIRECT DETECTION



INDIRECT DETECTION









CURRENT STATUS



Solid lines are the astrophysical bkgd from GALPROP (Moskalenko, Strong)

ARE THESE DARK MATTER?

 Energy spectrum shape consistent with WIMP dark matter candidates

 $\frac{d\Phi_{e^+}}{d\Omega dE} = \frac{\rho_{\chi}^2}{m_{\chi}^2} \sum_i \sigma_i v B_{e^+}^i \int dE_0 f_i(E_0) G(E_0, E)$

- Flux is a factor of 100-1000 too big for a thermal relic; requires
 - Enhancement from particle physics
 - Alternative production mechanism

Cirelli, Kadastik, Raidal, Strumia (2008) Arkani-Hamed, Finkbeiner, Slatyer, Weiner (2008) Feldman, Liu, Nath (2008); Ibe, Murayama, Yanagida (2008) Guo, Wu (2009); Arvanitaki et al. (2008)

Pulsars can explain PAMELA

Zhang, Cheng (2001); Hooper, Blasi, Serpico (2008) Yuksel, Kistler, Stanev (2008); Profumo (2008) Fermi-LAT Collaboration (2009)



ALPHA MAGNETIC SPECTROMETER

- Carried by the Space Shuttle on 16 May 2011 to the International Space Station
- Can AMS-02 disentangle dark matter from pulsars?





Pato, Lattanzi, Bertone (2010)





SPIN-DEPENDENT SCATTERING



Dark Matter annihilates in <u>the galactic center</u> to a place <u>photons</u>, which are detected by <u>Fermi, VERITAS, ...</u>. some particles an experiment

- Lines from XX $\rightarrow \gamma\gamma$, γ Z
- Continuum from XX \rightarrow ff $\rightarrow \gamma$

$$\frac{d\Phi_{\gamma}}{d\Omega dE} = \sum_{i} \underbrace{\frac{dN_{\gamma}^{i}}{dE}\sigma_{i}v\frac{1}{4\pi m_{\chi}^{2}}}_{Particle} \underbrace{\int_{\psi}^{\phi}\rho^{2}dl}_{Physics}$$

Halo profiles are poorly understood near the galactic center


PARTICLE COLLIDERS

AL BUT SHE

CMS



ATLAS



DIRECT PRODUCTION AT COLLIDERS

- Thermal relic WIMPs annihilate to SM particles, and so should be produced directly at colliders
- Pair production is invisible, so consider photon radiation

• Also mono-jets, mono-photons at Tevatron and LHC

Birkedal, Matchev, Perelstein (2004); Feng, Su, Takayama (2005) Konar, Kong, Matchev, Perelstein (2009)

WIMP EFFECTIVE THEORY

- This idea has recently been extended and studied systematically
- Assume WIMPs are light, integrate out all other particles, yielding a list of effective operators (motivated by DAMA, CoGeNT, for example)



Goodman, Ibe, Rajaraman, Shepherd, Tait, Yu (2010)

Name	Operator	Coefficient
D1	$\bar{\chi}\chi\bar{q}q$	m_q/M_*^3
D2	$\bar{\chi}\gamma^5\chi\bar{q}q$	im_q/M_*^3
D3	$\bar{\chi}\chi\bar{q}\gamma^5 q$	im_q/M_*^3
D4	$\bar{\chi}\gamma^5\chi\bar{q}\gamma^5q$	m_q/M_*^3
D5	$\bar{\chi}\gamma^{\mu}\chi\bar{q}\gamma_{\mu}q$	$1/M_{*}^{2}$
D6	$\bar{\chi}\gamma^{\mu}\gamma^{5}\chi\bar{q}\gamma_{\mu}q$	$1/M_{*}^{2}$
D7	$\bar{\chi}\gamma^{\mu}\chi\bar{q}\gamma_{\mu}\gamma^{5}q$	$1/M_{*}^{2}$
D8	$\bar{\chi}\gamma^{\mu}\gamma^{5}\chi\bar{q}\gamma_{\mu}\gamma^{5}q$	$1/M_{*}^{2}$
D9	$\bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma_{\mu\nu}q$	$1/M_{*}^{2}$
D10	$\bar{\chi}\sigma_{\mu\nu}\gamma^5\chi\bar{q}\sigma_{\alpha\beta}q$	i/M_*^2
D11	$\bar{\chi}\chi G_{\mu\nu}G^{\mu\nu}$	$\alpha_s/4M_*^3$
D12	$\bar{\chi}\gamma^5\chi G_{\mu\nu}G^{\mu\nu}$	$i\alpha_s/4M_*^3$
D13	$\bar{\chi}\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$i\alpha_s/4M_*^3$
D14	$\bar{\chi}\gamma^5\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$\alpha_s/4M_*^3$

PRECISION DM AT COLLIDERS

If there is a signal, what do we learn?

 Cosmology can't discover SUSY Particle colliders can't discover DM





Lifetime > 10^{-7} s \rightarrow 10^{17} s ?

DARK MATTER AT THE LHC

- What LHC actually sees:
 - E.g., $\tilde{q}\tilde{q}$ pair production
 - − Each \tilde{q} → neutralino χ
 - -2χ 's escape detector
 - missing momentum
- This is not the discovery of dark matter
 - Lifetime > 10^{-7} s \rightarrow 10^{17} s?



THE EXAMPLE OF BBN



- Nuclear physics → light element abundance predictions
- Compare to light element abundance observations
- Agreement → we understand the universe back to

t ~ 1 sec

DARK MATTER ANALOGUE



- Particle physics → dark matter abundance prediction
- Compare to dark
 matter abundance
 observation
- How well can we do?

WIMP ANNIHILATION PROCESSES



Jungman, Kamionkowski, Griest (1995)

RELIC DENSITY DETERMINATIONS



% level comparison of predicted Ω_{collider} with observed Ω_{cosmo}

IDENTIFYING DARK MATTER



LECTURE 2 SUMMARY

- Thermal relic WIMPs can be detected directly, indirectly, and at colliders, and the thermal relic density implies significant rates
- There are currently tantalizing anomalies
- Definitive dark matter detection and understanding will require signals in several types of experiments

OUTLINE

LECTURE 1

Essential Cosmology, Dark Energy, WIMP Miracle

LECTURE 2

WIMP Detection, WIMPs at Colliders

LECTURE 3

Other Terascale Dark Matter Possibilities

NEW DISSERTATION AWARD IN THEORETICAL PARTICLE PHYSICS

- Established in 2011 by the APS's Division of Particles and Fields
- The Award recognizes exceptional young scientists who have performed original doctoral thesis work of outstanding scientific quality and achievement in the area of theoretical particle physics. The annual Award consists of \$1,500, a certificate citing the accomplishments of the recipient, and an allowance of up to \$1,000 for travel to attend a meeting of the Division of Particles and Fields (DPF) or APS, where the Award will be presented.
- Nominations of 2011 PhDs due 1 October 2011. Questions? See http://www.aps.org/programs/honors/dissertation/particle.cfm or contact Vernon Barger, Michael Dine, Jonathan Feng, Ben Grinstein (chair), JoAnne Hewett (2011 Selection Committee)

MANY INTERESTING QUESTIONS AND TOPICS

- What about late decaying dark matter?
- What is warm dark matter?
- What about gravitinos, axinos, etc.?
- The thermal relic density only constrains one combination of coupling and mass. Why focus on WIMPs only?
- What are the most stringent bounds on dark matter self-interactions?
- What are the constraints on charged stable particles from sea water?
- What is your favorite dark matter candidate?
- Shouldn't we be working on LHC physics?

20-22 June 11

GRAVITINO DARK MATTER

- SUSY: graviton $G \rightarrow$ gravitino \tilde{G} , spin 3/2
- Mass $m_{\tilde{G}} \sim F/M_{Pl}$
 - Ultra-light (GMSB): F ~ (100 TeV)², $m_{\tilde{G}}$ ~ eV
 - Light (GMSB): F ~ $(10^7 \text{ GeV})^2$, $m_{\tilde{G}}$ ~ keV
 - Heavy (SUGRA): F ~ $(10^{11} \text{ GeV})^2$, $m_{\tilde{G}}$ ~ TeV
 - Obese (AMSB): F ~ $(10^{12} \text{ GeV})^2$, $m_{\tilde{G}}$ ~ 100 TeV
- The gravitino interaction strength ~ 1/F
- A huge range of scenarios, phenomena

HEAVY GRAVITINOS

• $m_{\tilde{G}} \sim F/M_{Pl} \sim TeV$, same scale as the other superpartners

• *Ĝ* interactions:

$$-\frac{i}{8M_{\rm Pl}}\bar{\tilde{G}}_{\mu}\left[\gamma^{\nu},\gamma^{\rho}\right]\gamma^{\mu}\tilde{B}F_{\nu\rho}$$

Couplings grow with energy, but are typically extremely weak



OPTION 1: GRAVITINOS FROM REHEATING

- Inflation dilutes relic densities. But at the end of inflation, the Universe reheats and can regenerate particles. Assume the reheat temperature is between the Planck and TeV scales.
- Gravitinos are produced in reheating. What happens?

$$\sigma_{\rm SM} n \sim T \gg H \sim \frac{T^2}{M_{\rm Pl}} \gg \sigma_{\tilde{G}} n \sim \frac{T^3}{M_{\rm Pl}^2}$$

SM interaction rate >> expansion rate >> G interaction rate

• Thermal bath of MSSM particles X: occasionally they interact to produce a gravitino: $X X \rightarrow X \tilde{G}$

GRAVITINO RELIC DENSITY

• The Boltzmann equation:

$$\frac{dn}{dt} = -3Hn - \langle \sigma v \rangle \begin{bmatrix} n^2 - n_{eq}^2 \end{bmatrix}$$

$$\uparrow$$
Dilution from $f \tilde{G} \to f \overline{f}$ $f \overline{f} \to f \tilde{G}$

Ω

• Change variables: $t \rightarrow$ Entropy density s ~ T³

$$T \qquad n \to Y \equiv \frac{n}{s}$$

- New Boltzmann $\frac{dY}{dT} = -\frac{\langle \sigma_{\tilde{G}} v \rangle}{HTs} n^2 \sim \langle \sigma_{\tilde{G}} v \rangle \frac{T^3 T^3}{T^2 TT^3}$
- Simple: $Y \sim$ reheat temperature T_{RH}

BOUNDS ON T_{RH}

 <σv> for important production processes:

	process i	$ \mathcal{M}_i ^2 / \frac{g^2}{M^2} \left(1 + \frac{m_{\tilde{g}}^2}{3m_{\tilde{G}}^2} \right)$
А	$g^a + g^b \rightarrow \tilde{g}^c + \tilde{G}$	$4(s+2t+2rac{t^2}{s}) f^{abc} ^2$
В	$g^a + \tilde{g}^b \rightarrow g^c + \tilde{G}$	$-4(t+2s+2\frac{s^2}{t}) f^{abc} ^2$
С	$\tilde{q}_i + g^a \to q_j + \tilde{G}$	$2s T^a_{ji} ^2$
D	$g^a + q_i \to \tilde{q}_j + \tilde{G}$	$-2t T^a_{ji} ^2$
Е	$\bar{\tilde{q}}_i + q_j \to g^a + \tilde{G}$	$-2t T^a_{ji} ^2$
F	$\tilde{g}^a + \tilde{g}^b \rightarrow \tilde{g}^c + \tilde{G}$	$-8 \frac{(s^2+st+t^2)^2}{st(s+t)} f^{abc} ^2$
G	$q_i + \tilde{g}^a \to q_j + \tilde{G}$	$-4(s+\tfrac{s^2}{t}) T^a_{ji} ^2$
Н	$\tilde{q}_i + \tilde{g}^a \to \tilde{q}_j + \tilde{G}$	$-2(t+2s+2\frac{s^2}{t}) T^a_{ji} ^2$
Ι	$q_i + \bar{q}_j \longrightarrow \tilde{g}^a + \tilde{G}$	$-4(t+\tfrac{t^2}{s}) T^a_{ji} ^2$
J	$\tilde{q}_i + \bar{\tilde{q}}_j \to \tilde{g}^a + \tilde{G}$	$2(s+2t+2\frac{t^2}{s}) T^a_{ji} ^2$

- $T_{\rm RH} < 10^8 10^{10} \, {\rm GeV};$ constrains inflation
- *Ĝ* may be all of DM if bound saturated



OPTION 2: GRAVITINOS FROM LATE DECAYS

- What if gravitinos are diluted by inflation, and the universe reheats to low temperature? No "primordial" relic density
- Ĝ not LSP
 Ĝ LSP





- No impact implicit assumption of most of the literature
- Completely different particle physics and cosmology

FREEZE OUT WITH SUPERWIMPS

Feng, Rajaraman, Takayama (2003)



SuperWIMPs naturally inherit the right density (WIMP miracle), share all the motivations of WIMPs, but are superweakly interacting

COSMOLOGY OF LATE DECAYS

Late decays impact light element abundances



- Complicated nucleocosmochemistry
- BBN typically excludes large lifetimes
- BBN excludes $\chi \rightarrow Z \tilde{G}$ (hadrons dangerous) but $\tilde{I} \rightarrow I \tilde{G}$ ok

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LATE DECAYS AND THE LITHIUM PROBLEM(S)



- ⁷Li does not agree with standard BBN prediction
 - Too low by factor of 3, $\sim 5\sigma$ at face value
 - May be solved by convection in stars, but then why so uniform?
- ⁶Li may also not agree
 - Too high
- Late decays can fix both

COSMIC MICROWAVE BACKGROUND

- Late decays may also distort the CMB spectrum
- For 10⁵ s < τ < 10⁷ s, get "μ distortions":

$$e^{E/(kT)+\mu} - 1$$

1

μ=0: Planckian spectrum μ≠0: Bose-Einstein spectrum Hu, Silk (1993)

Current bound: |μ| < 9 x 10⁻⁵
 Future: possibly |μ| ~ 5 x 10⁻⁸



WARM DARK MATTER

- SuperWIMPs are produced in late decays with large velocity (0.1c – c)
- Suppresses small scale structure, as determined by the free-streaming scale

$$\lambda_{\rm FS} = \int_{\tau_X}^{t_{\rm EQ}} \frac{v(t)dt}{a(t)}$$

• Warm DM with cold DM pedigree

Dalcanton, Hogan (2000)

Lin, Huang, Zhang, Brandenberger (2001)

Sigurdson, Kamionkowski (2003)

Profumo, Sigurdson, Ullio, Kamionkowski (2004)

Kaplinghat (2005)

Cembranos, Feng, Rajaraman, Takayama (2005)

Strigari, Kaplinghat, Bullock (2006)

Bringmann, Borzumati, Ullio (2006)



Kaplinghat (2005)

THE COMPLETE MSUGRA

If LSP = gravitino, then no 2000 • reason to exclude stau (N)LSP region Slepton 1500 Rajaraman, Smith (2005 NLSP Extend the mSUGRA **CHAMP** parameters to $\mathrm{M}_{1/\hat{i}}$ 1000 $m_0^2, M_{1/2}, A_0, \tan\beta, \text{ sign}(\mu), \text{ and } m_{3/2}$ χ (N)LSP and include negative MET Slepton 500 $m_0 \equiv \operatorname{sign}(m_0^2) \sqrt{|m_0^2|}$ < 100 GeV А Much of the new parameter ۲ space is viable with a slepton 0 -800 - 600 - 400 - 200200 400 600 800 0 NLSP and a gravitino LSP

 m_0

CHARGED PARTICLE TRAPPING

- SuperWIMP DM → metastable particles, may be charged, far more spectacular than misssing E_T
- Can collect these particles and study their decays
- Several ideas
 - Catch sleptons in a 1m thick water tank
 Feng, Smith (2004)
 - Catch sleptons in LHC detectors

Hamaguchi, Kuno, Nakawa, Nojiri (2004)

Dig sleptons out of detector hall walls

De Roeck et al. (2005)



WHAT WE COULD LEARN FROM CHARGED PARTICLE DECAYS

$$\tau(\tilde{l} \to l\tilde{G}) = \frac{6}{G_N} \frac{m_{\tilde{G}}^2}{m_{\tilde{l}}^5} \left[1 - \frac{m_{\tilde{G}}^2}{m_{\tilde{l}}^2} \right]^{-4}$$

- Measurement of τ , $\tilde{m_{l}}$ and $E_{l} \rightarrow m_{\tilde{G}}$ and G_{N}
 - Probes gravity in a particle physics experiment
 - Measurement of G_N on fundamental particle scale
 - Precise test of supergravity: gravitino is graviton partner
 - Determines $\Omega_{\tilde{G}}$: SuperWIMP contribution to dark matter
 - Determines F : supersymmetry breaking scale, contribution of SUSY breaking to dark energy, cosmological constant

Hamaguchi et al. (2004); Takayama et al. (2004)

LIGHT GRAVITINO DM

- The original SUSY DM scenario
 - Universe cools from high temperature
 - Gravitinos decouple while relativistic, $\Omega_{\tilde{G}} h^2 \approx m_{\tilde{G}} / 800 \text{ eV}$
 - Favored mass range: keV gravitinos

Pagels, Primack (1982)

- This minimal scenario is now excluded
 - Ω_{G̃} h^2 < 0.1 → m_{G̃} < 80 eV
 - Gravitinos not too hot $\rightarrow m_{\tilde{G}}$ > few keV
 - keV gravitinos are now the most disfavored

Viel, Lesgourgues, Haehnelt, Matarrese, Riotto (2005) Seljak, Makarov, McDonald, Trac (2006)

- Two ways out
 - Λ WDM: $m_{\tilde{G}}$ > few keV. Gravitinos are all the DM, but thermal density is diluted by low reheating temperature, late entropy production, ...
 - Λ WCDM: $m_{\tilde{G}}$ < 16 eV. Gravitinos are only part of the DM, mixed warm-cold scenario

CURRENT BOUNDS



WIMP MIRACLE REVISITED

• The thermal relic density

$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4} \qquad \begin{array}{c} \mathsf{x} & & \mathsf{p} \\ \mathsf{x} & & \mathsf{q} \\ \mathsf{x} & & \mathsf{q} \end{array}$$

constrains only one combination of mass and coupling

- In the SM, however, we only have a few choices – Weak coupling: $m_X \sim 100$ GeV, $g_X \sim 0.6 \Rightarrow \Omega_X \sim 0.1$
 - EM and strong: highly constrained

CHARGED STABLE RELICS

- Charged stable relics create anomalously heavy isotopes
- Severe bounds from sea water searches
- Inflation can dilute this away, but there is an upper bound on the reheating temperature



Kudo, Yamaguchi (2001)

Masses < TeV are excluded by T_{RH} > 1 MeV, but masses > TeV are allowed

HIDDEN DARK MATTER

 We can introduce hidden sectors composed of particles without SM interactions, but with their own interactions



- Dark matter may be in such a sector
 - Interesting self-interactions, astrophysics
 - Less obvious connections to particle physics
 - No WIMP miracle

Spergel, Steinhardt (1999); Foot (2001)

THE WIMPLESS MIRACLE

Feng, Kumar (2008); Feng, Tu, Yu (2009); Feng, Shadmi (2011)

- In SUSY, however, there may be additional structure. E.g., in GMSB, AMSB, the masses satisfy $m_X \sim g_X^2$
- This leaves the relic density invariant $\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4}$
- "WIMPless Miracle": hidden sectors of these theories automatically have DM with the right Ω (but they aren't WIMPs)
- Is this what the new physics flavor problem is telling us?!



WIMPLESS DM SIGNALS

 Hidden DM may have only gravitational effects, but still interesting: e.g., it may interact through "dark photons", selfinteract through Rutherford scattering

> Ackerman, Buckley, Carroll, Kamionkowski (2008) Feng, Kaplinghat, Tu, Yu (2009)

 Alternatively, hidden DM may interact with normal matter through connector particles, can explain DAMA and CoGeNT signals





LECTURE 3 SUMMARY

- WIMPs are not the only class of DM that naturally have the right relic density, nor are they the only DM candidate predicted by SUSY, extra dimensions, ...
- These other candidates may have completely different implications for cosmology, colliders
- Is any of this right? LHC is running, direct and indirect detection, astrophysical probes are improving rapidly – this field will be transformed soon